

Aaron				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

Blake				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

Denise				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

“Yeah, But How Do I Translate That to a Percentage?”  
 & Other Standards-Based Assessment FAQs

STA Convention • May 6, 2022

Hey, students!

Go to [student.desmos.com](https://student.desmos.com)  
and type in:

CW2 X3H

You can also share this invitation link with your students:

https://student.desmos.com/join/cw2x3h

Copy

Have all students joined this class?

[Deactivate this invite code](#)

This prevents additional students from joining. You can always reactivate the code.

Do additional students need to join the class?

New students can use the code to join until

**May 18, 2022.** [Change Date](#)



# Chris Hunter

K-12 Numeracy Helping Teacher

Surrey Schools

email: hunter\_c@surreyschools.ca

Twitter: @ChrisHunter36

blog: chrishunter.ca



**[chrishunter.ca/tag/standards-based/](https://chrishunter.ca/tag/standards-based/)**

## Traditional

Students accumulate **points**  
tied to **events**

e.g., “Quiz 2.3”

Compares students to **each  
other**

## Standards-Based

Students demonstrate  
**evidence** in relation to  
**learning standards**

e.g., “use ratios and rates to make  
comparisons between quantities”

Compares student learning  
against **proficiency levels**



*What letter grade or percentage would **you** assign to Aaron, Blake, and Denise?*

[illegible]



# FAQs

- *Why change?*
- *Why reinvent the wheel?*
- *Assess what?*
- *How many learning standards?*
- *What do **Emerging and Extending** mean?*
- *What does each proficiency level look like?*
- *How do I elicit evidence of learning?*
- *How do I keep track of data?*
- *Yeah, but how do I translate that to a percentage?*



# Menu Math

- Think about the following “design specifications” of quadratic functions
- You *could* build ten different quadratic functions to satisfy these ten different constraints
- Instead, build a set of as few quadratic functions as possible to satisfy each constraint at least once
- Write your functions in the form  $y = a(x - p)^2 + q$
- Describe how and why you built each function
- Be sure to identify which functions satisfy which constraints

Which constraints pair nicely?

		Vertex in quadrant II
		Vertex on the y-axis
		Positive y-intercept
G.	Never enters	
I.	Horizontally	

Which constraints cannot be paired?

at Banting

# Menu Math

A.	Two negative $x$ -intercepts	B.	Vertex in quadrant II
C.	Never enters quadrant III	D.	Vertex on the $y$ -axis
E.	Positive $y$ -intercept	F.	No $x$ -intercepts
G.	Never enters quadrant I	H.	Has a minimum value
I.	Horizontally stretched	J.	Line of symmetry enters quadrant IV





*Why change?*



# Standards-Based Learning in Action

## Moving From Theory to Practice



**Tom Schimmer   Garnet Hillman   Mandy Stalets**



“In this **traditional system**, experience has trained students to play the game of school. Schools dangle the carrot (the academic grade) in front of their faces and encourage students to chase it. With these practices, schools have created a **culture of compliance**.

Tom Schimmer

Becoming **standards based** is about changing to a **culture of learning**.  
‘Complete this assignment to get these points’ changes to ‘Complete this assignment to improve your learning.’ [...] Educators have trained learners to focus on the academic grade; they can coach them out of this assumption.”

Tom Schimmer



BUILDING  
**THINKING  
CLASSROOMS**  
in MATHEMATICS

GRADES K-12

14 TEACHING  
PRACTICES  
FOR ENHANCING  
LEARNING



PETER LILJEDAHN

FOREWORD BY TRACY JOHNSTON ZAGER

ILLUSTRATIONS BY LAURA WHEELER

CORWIN Mathematics

“If you want to start valuing day-to-day learning evidence or how students work in groups, you’ll have to make a **paradigm shift.**”

Peter Liljedahl

**Point-Gathering** —————→ **Data-Gathering**

*more accurate*

*more fair*

*more relevant*

*no less objective*



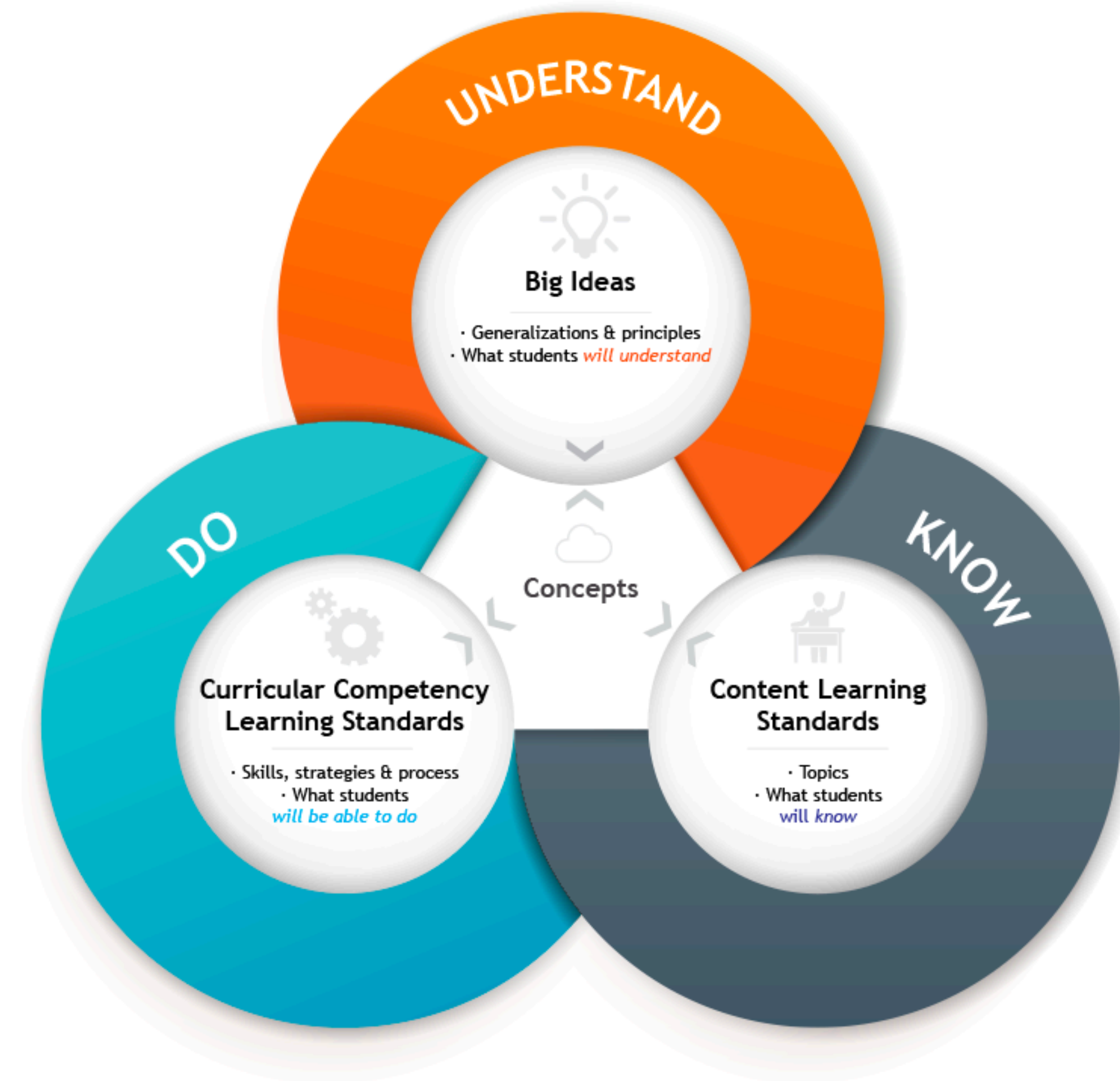
“Students start thinking about their learning rather than their grades and, as they do so, grading becomes a byproduct of learning rather than the objective of learning.”

Peter Liljedahl

*Why*



?





**Point-Gathering** —————→ **Data-Gathering**

*more accurate*

*more fair*

*more relevant*

*no less objective*



*Assess what?*



# Menu Math

- Think about the following “design specifications” of quadratic functions
- You *could* build ten different functions to satisfy these ten constraints
- Instead, build a set of as many functions as possible to satisfy each constraint at least once
- Write your functions in the form  $y = a(x - p)^2 + q$
- Describe how and why you built each function
- Be sure to identify which functions satisfy which constraints

*Which learning standards did you “bump into” as you solved the problem?*

		B.	Vertex in quadrant II
		D.	Vertex on the y-axis
		F.	No x-intercepts
		H.	Has a minimum value
I.	Horizontally stretched	J.	Line of symmetry enters quadrant IV

–Nat Banting

# Pre-calculus 11

## Learning Standards

### Curricular Competencies

- **analyze** and **apply** mathematical ideas using reason
- **explain** and **justify** mathematical ideas and decisions

### Content

- quadratic functions



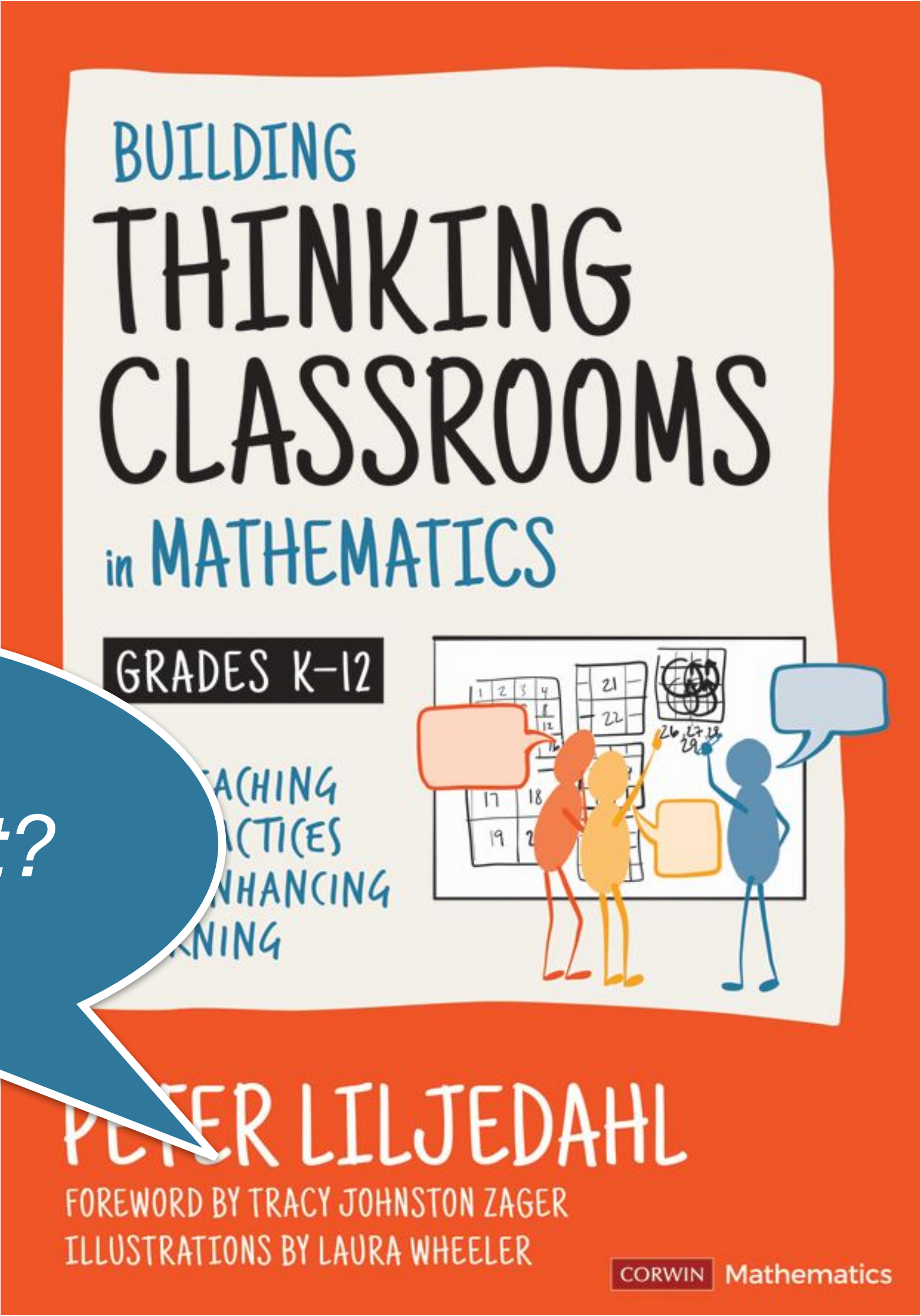


*How many learning  
standards?*

FRACTIONS	BASIC	INTERMEDIATE	ADVANCED
Definitions			
Add and subtract proper fractions			
Add and subtract mixed fractions			
Multiply and divide proper fractions			
Multiply and divide mixed fractions			
Solve order of operation tasks with proper and mixed fractions			
Solve contextual problems involving fractions			
Estimate solutions for problems involving fractions			

*What feels correct?*

*What doesn't?*





FRACTIONS	BASIC	INTERMEDIATE	ADVANCED
Definitions			
Add and subtract proper fractions			
Add and subtract mixed fractions			
Multiply and divide proper fractions			
Multiply and divide mixed fractions			
Solve order of operation tasks with proper and mixed fractions			
Solve contextual problems involving fractions			
Estimate solutions for problems involving fractions			

# Operations with Fractions

add and subtract fractions

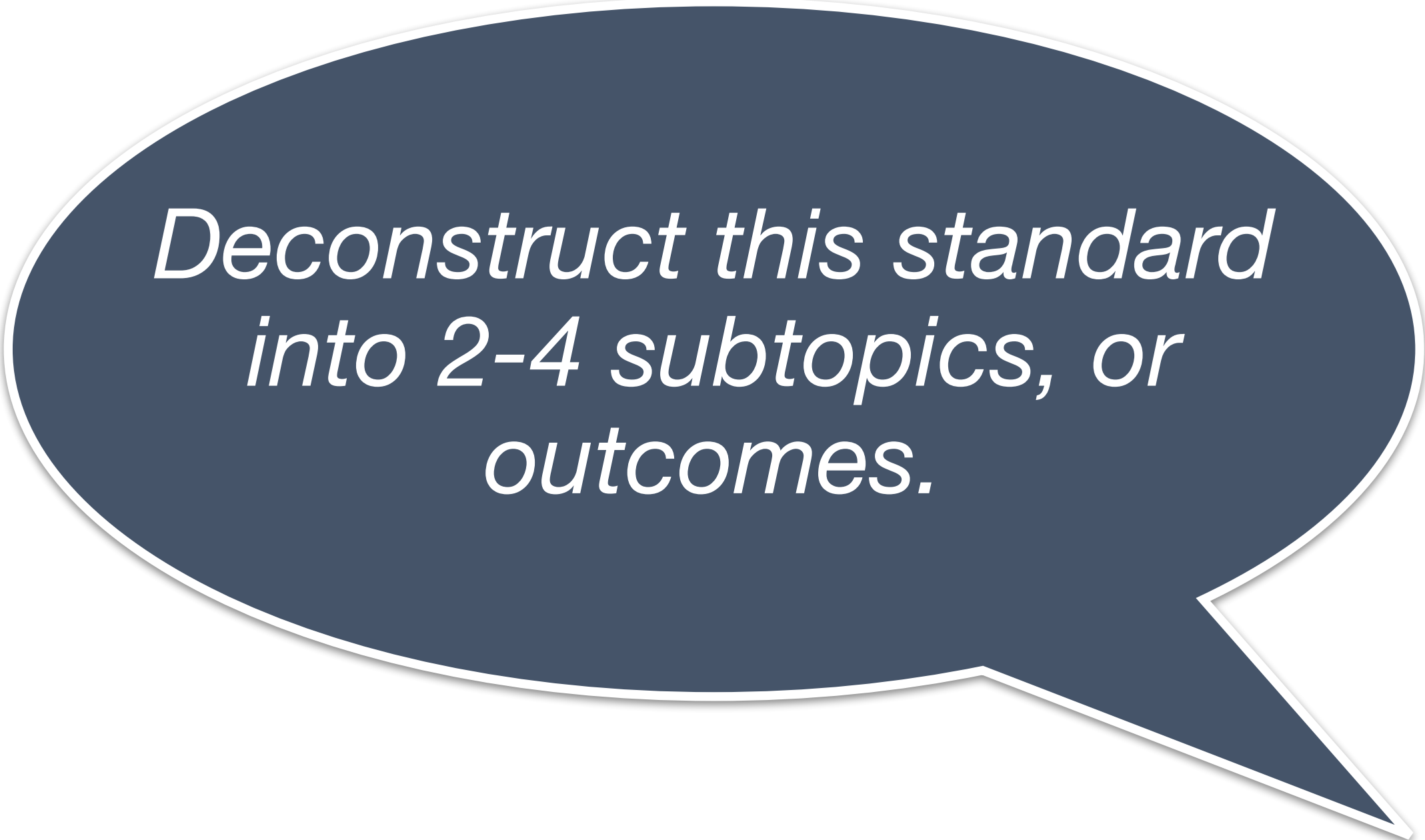
multiply and divide fractions

evaluate expressions with two or more operations on fractions

solve contextual problems involving fractions

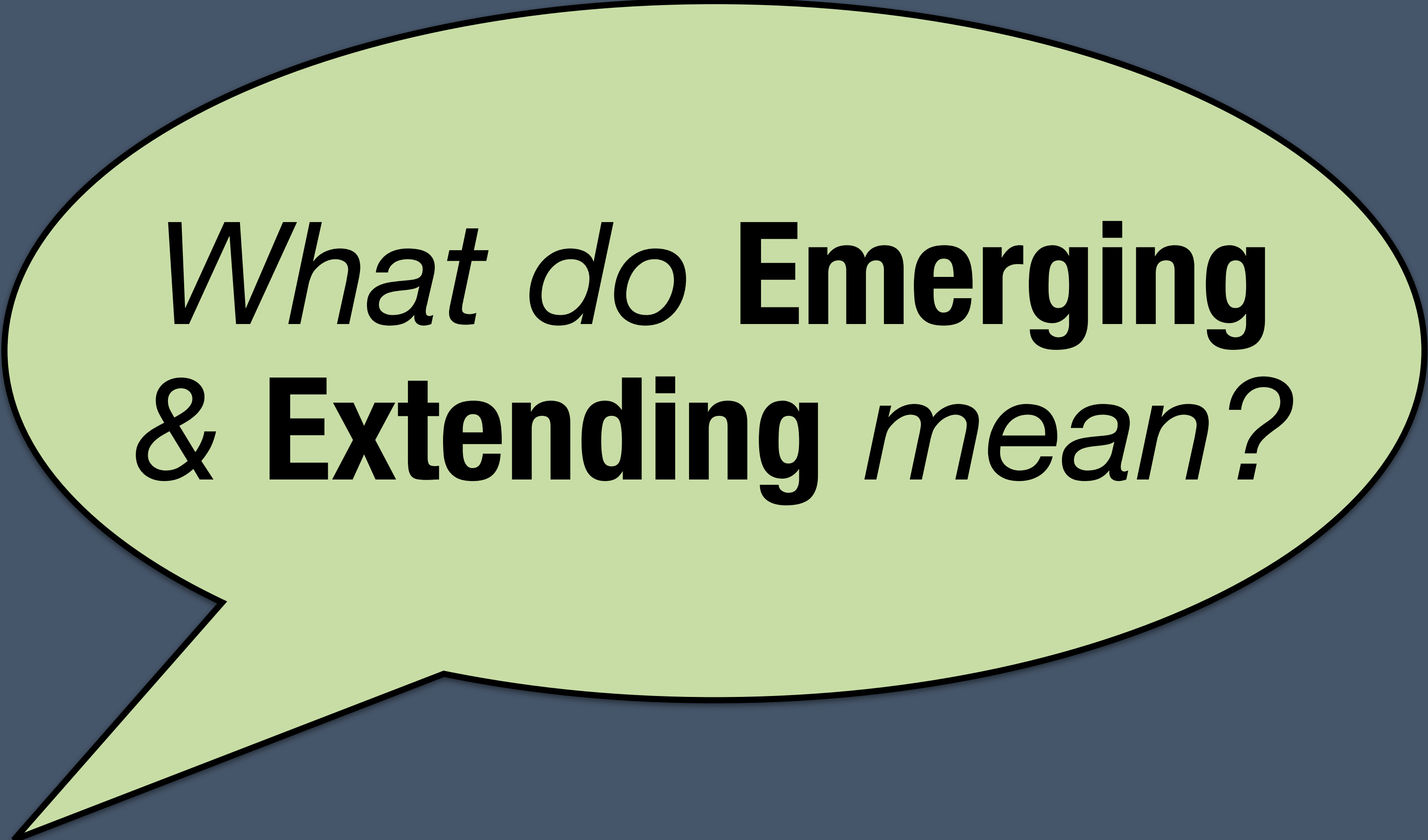


# Foundations of Mathematics and Pre-calculus 10

Learning Standard	Delineated Learning Standards
systems of linear equations	 <p><i>Deconstruct this standard into 2-4 subtopics, or outcomes.</i></p>

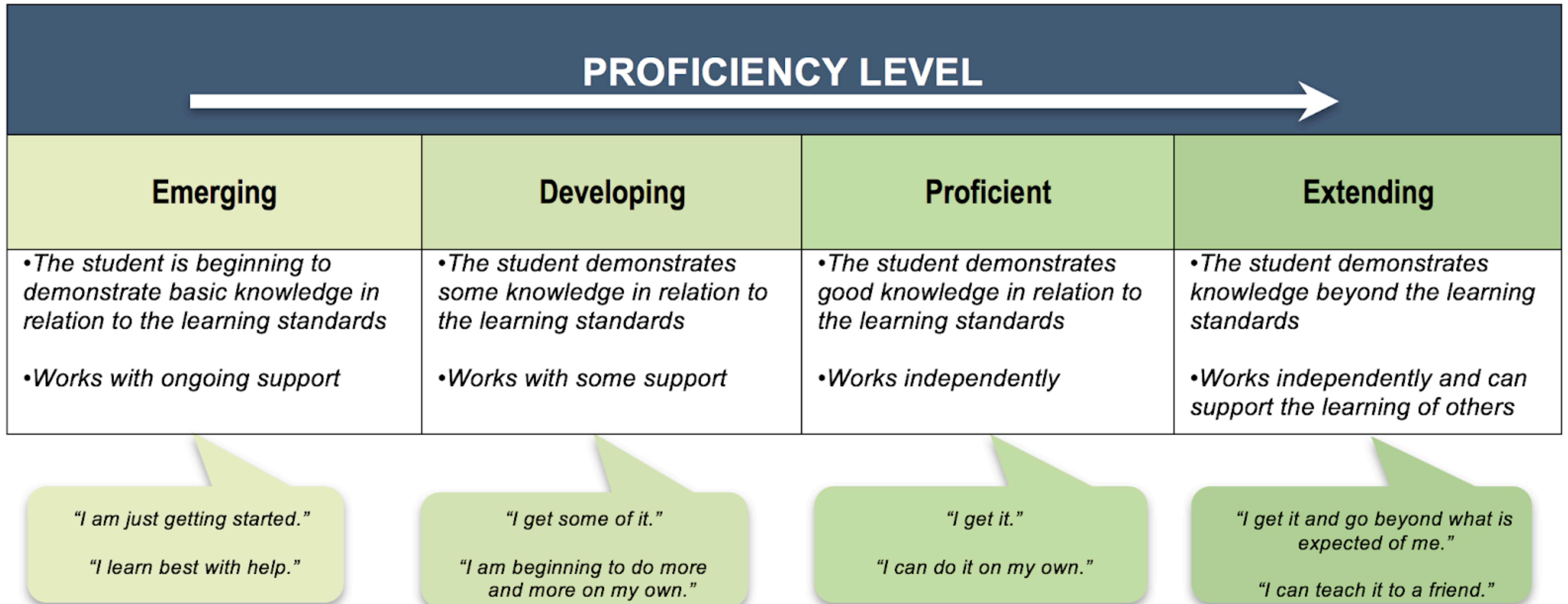
# Foundations of Mathematics and Pre-calculus 10

Learning Standard	Delineated Learning Standards
systems of linear equations	solve systems of linear equations graphically
	solve systems of linear equations algebraically
	model and solve contextual problems involving systems of linear equations




*What do **Emerging**  
& **Extending** mean?*





Source: Surrey Schools?

Proficiency Scale				
	Emerging	Developing	Proficient	Extending
	The student demonstrates an initial understanding of the concepts and competencies relevant to the expected learning.	The student demonstrates a partial understanding of the concepts and competencies relevant to the expected learning.	The student demonstrates a complete understanding of the concepts and competencies relevant to the expected learning.	The student demonstrates a sophisticated understanding of the concepts and competencies relevant to the expected learning.

Source: BC Ministry of Education (as of the 2018/19 school year)

PROFICIENCY LEVEL			
Emerging	Developing	Proficient	Extending
•The student is beginning to demonstrate basic knowledge in relation to the learning standards •Works with ongoing support	•The student demonstrates some knowledge in relation to the learning standards •Works with some support	•The student demonstrates good knowledge in relation to the learning standards •Works independently	•The student demonstrates knowledge beyond the learning standards •Works independently and can support the learning of others

"I am just getting started."  
"I learn best with help."

"I get some of it."  
"I am beginning to do more and more on my own."

"I get it."  
"I can do it on my own."

"I get it and go beyond what is expected of me."  
"I can teach it to a friend."

Proficiency Scale				
	Emerging	Developing	Proficient	Extending
	The student demonstrates an initial understanding of the concepts and competencies relevant to the expected learning.	The student demonstrates a partial understanding of the concepts and competencies relevant to the expected learning.	The student demonstrates a complete understanding of the concepts and competencies relevant to the expected learning.	The student demonstrates a sophisticated understanding of the concepts and competencies relevant to the expected learning.

*basic      some      good      beyond*

*initial   partial   complete   sophisticated*

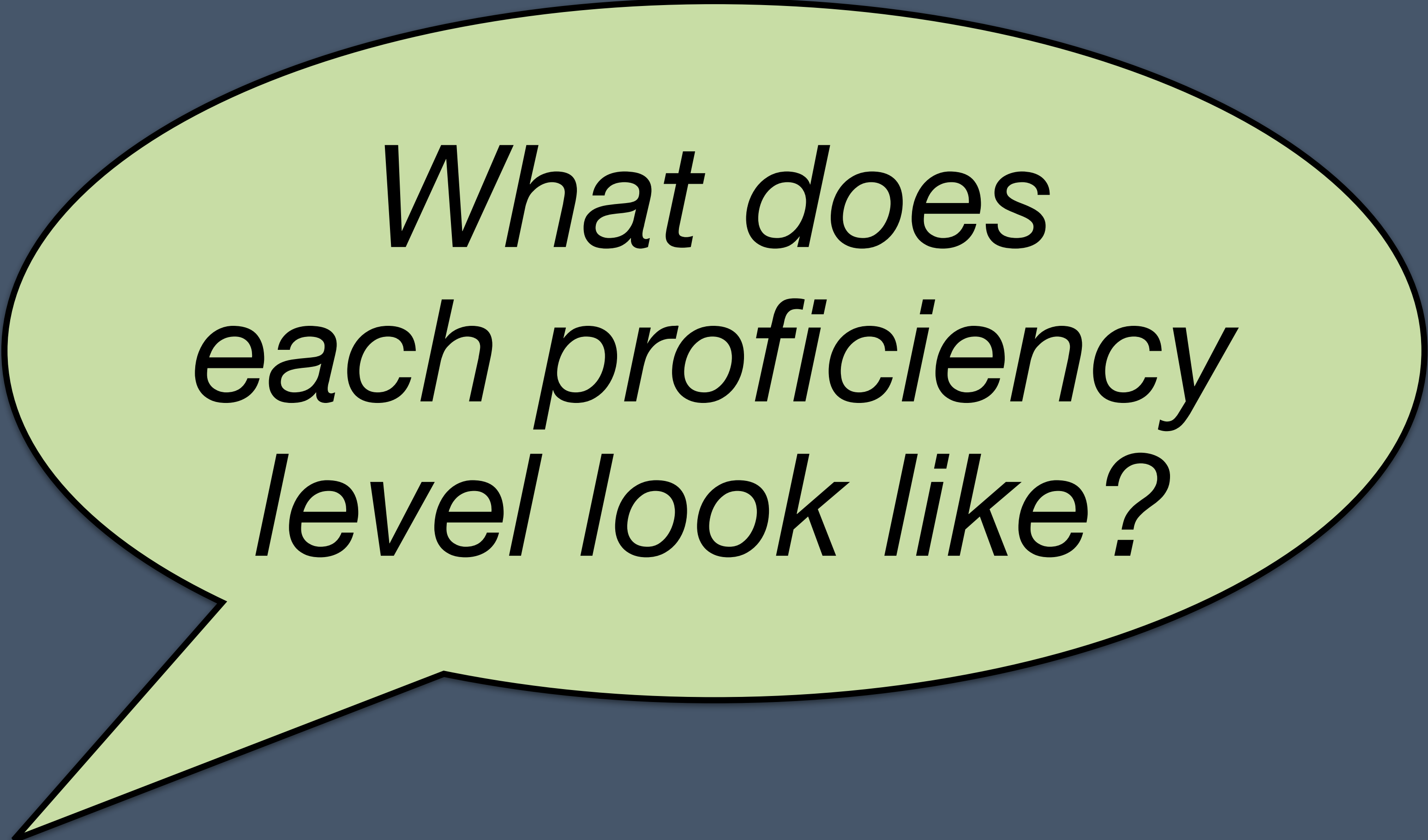
*with support      independence*

*depth*

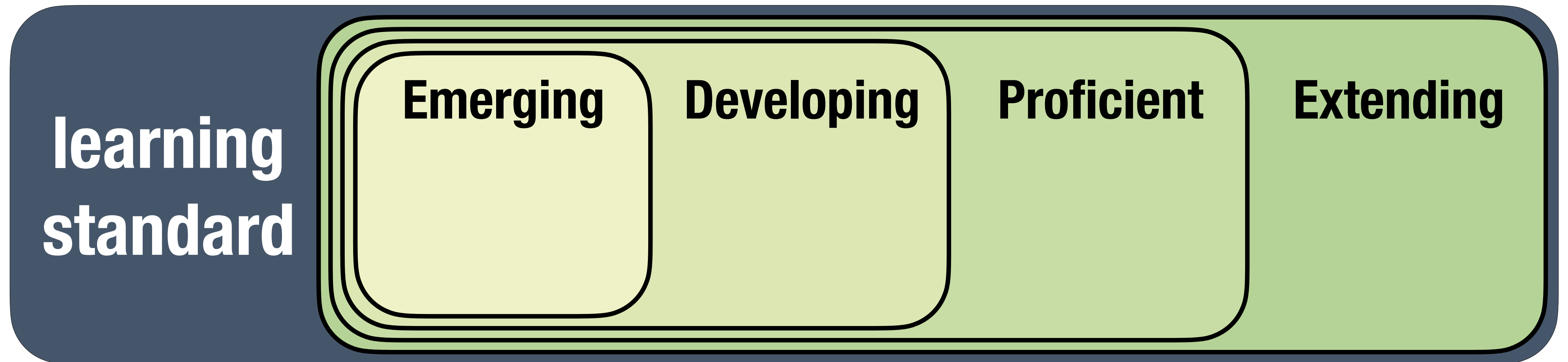
*teach*

*What are some implications?*





*What does  
each proficiency  
level look like?*



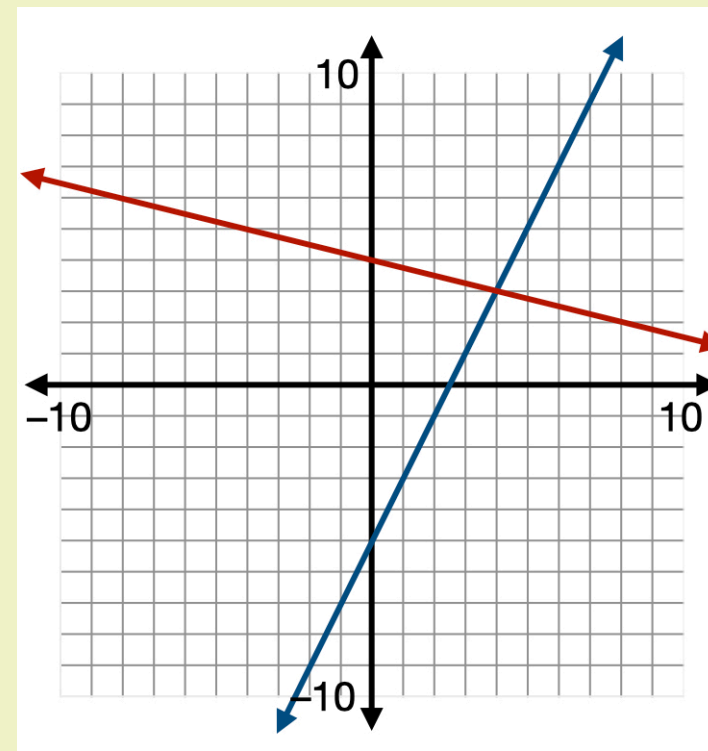
Descriptive · Positive · Progressive & Additive

# solve systems of linear equations graphically

## Emerging

identify the solution from a graph or table

What is the solution to the system represented by the graph?



## Developing

determine the solution given equations in slope-intercept form

Solve graphically:

$$y = 2x - 5$$

$$y = -\frac{1}{4}x + 4$$

## Proficient

determine the solution given equations in general form

Solve graphically:

$$2x + 5y + 25 = 0$$

$$4x - 2y + 14 = 0$$

determine the number of solutions

Analyze the system to determine whether it has one solution, no

## Extending

create a system given constraints

Create a system so that:

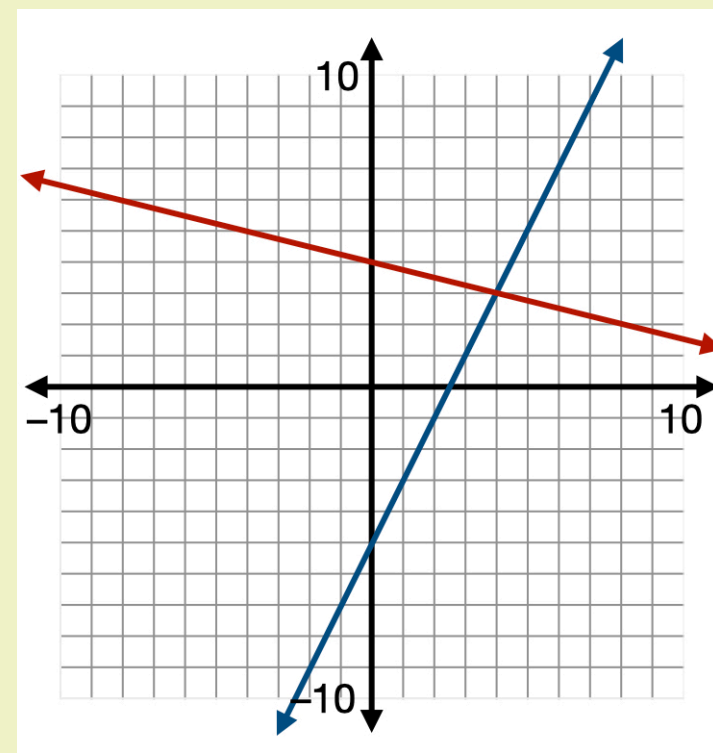
- the solution is  $(-3, -1)$
- one line has a negative slope
- one line enters the first quadrant

Place the numbers from 1 to 9 in the boxes below so that the system has infinitely many solutions:



# solve systems of linear equations graphically

What is the solution to the system represented by the graph?



form

Solve graphically:

$$y = 2x - 5$$

$$y = -\frac{1}{4}x + 4$$

Solve graphically:

$$2x + 5y + 25 = 0$$

$$4x - 2y + 14 = 0$$

determine the  
number of  
solutions

Analyze the system to determine whether it has one solution, no solution, or infinitely many solutions:

$$y = \frac{1}{2}x - 4$$

$$3x - 6y - 12 = 0$$

Create a system so that:

- the solution is  $(-3, -1)$
- one line has a negative slope
- one line enters the first quadrant

Place the numbers from 1 to 9 in the boxes below so that the system has infinitely many solutions:

$$\square x + \square y = \square$$

$$\square x + \square y = \square$$

(Each number can be used only once.)

**solve  
systems of  
linear  
equations  
algebraically**

**Emerging**

verify the  
solution by  
substitution

Is (2, 5) a solution  
to the system:

$$y = 3x - 1$$
$$x - 2y = 8?$$

solve by  
elimination  
where  
multiplication is  
*not* necessary

Solve:

**Developing**

solve by  
substitution  
where *one*  
variable is  
isolated in an  
equation

Solve:

$$x = 6 - 4y$$
$$2x - 3y = 1$$

solve by  
elimination  
where  
multiplication of  
*one* equation is  
necessary

**Proficient**

solve by  
substitution  
where *neither*  
variable is  
isolated in an  
equation

Solve:

$$2x + 5y + 7 = 0$$
$$3x - y = -2$$

solve by  
elimination  
where  
multiplication of  
*both* equations  
is necessary

**Extending**

select, apply,  
and defend an  
algebraic  
approach

Would you rather  
solve the following  
system by  
elimination or  
substitution?

$$4x - y - 3 = 0$$
$$6x - 2y - 5 = 0$$

Why?

**solve  
systems of  
linear  
equations  
algebraically**

Is (2, 5) a solution  
to the system:

$$y = 3x - 1$$
$$x - 2y = 8?$$

solve by  
elimination  
where  
multiplication is  
*not* necessary

Solve:

$$3x - 4y = 23$$
$$7x + 4y = 27$$

variable is  
isolated in an  
equation

Solve:

$$x = 6 - 4y$$
$$2x - 3y = 1$$

solve by  
elimination  
where  
multiplication of  
*one* equation is  
necessary

Solve:

$$7x + 2y = -1$$
$$3x - 4y = 19$$

variable is  
isolated in an  
equation

Solve:

$$2x + 5y + 7 = 0$$
$$3x - y = -2$$

solve by  
elimination  
where  
multiplication of  
*both* equations  
is necessary

Solve:

$$5x + 4y = 13$$
$$8x + 3y + 3 = 0$$

approach

Would you rather  
solve the following  
system by  
elimination or  
substitution?

$$4x - y - 3 = 0$$
$$6x - 2y - 5 = 0$$

Why?



**model and  
solve  
contextual  
problems  
involving  
systems of  
linear**

**Emerging**

interpret the  
solution in  
context given  
a model

The heights of two  
candles over time  
can be modelled  
by:

$$h = 20 - 2t$$

$$h = 16 - 1.5t$$

What is the  
meaning, in  
context, of the  
solution (8, 4)?

**Developing**

model and  
solve  
combination  
problems

Two t-shirts and  
four hoodies sell for  
\$254. Four t-shirts  
and five hoodies  
sell for \$361. What  
is the price of each  
item?

**Proficient**

model and  
solve parts-  
whole and  
catch-up  
problems

Tickets to a charity  
hockey game cost  
\$12 for adults and  
\$8 for children. A  
total of 150 tickets  
were sold for  
\$1640. How many  
of each type of  
ticket were sold?

A gas vehicle has  
an initial cost of

**Extending**

model and  
solve mixture  
problems

A scientist needs to  
make 200 ml of a  
42% alcohol  
solution. They mix  
30% alcohol and  
50% alcohol  
solutions. How  
much of each  
solution do they  
need?

**solve  
contextual  
problems  
involving  
systems of  
linear  
equations**

$$h = 20 - 2t$$
$$h = 16 - 1.5t$$

What is the meaning, in context, of the solution (8, 4)?

sell for \$361. What is the price of each item?

\$12 for adults and \$8 for children. A total of 150 tickets were sold for \$1640. How many of each type of ticket were sold?

A gas vehicle has an initial cost of \$31 000 and an operating cost of \$1500 per year. An electric vehicle has an initial cost of \$43 000 and an operating cost of \$500 per year. How many years will it take for the total cost of both vehicles to be same?

50% alcohol solutions. How much of each solution do they need?



AnonymizePacingPause  
0 students ⌚ Time Entered ▾

1 Consider...  
How are these two

2 Counting...  
Which pack do

3 Make an...  
Check your

4 Let's get...  
Use the information

5 Describe...  
How did you refine your prediction on the

6 Reveal  
Here are your predictions

7 Extensio...  
On this screen

Single Crème

Nutrition Facts
Calories 320

Double Crème

Nutrition Facts
Calories 280

Triple Crème

Nutrition Facts
Calories

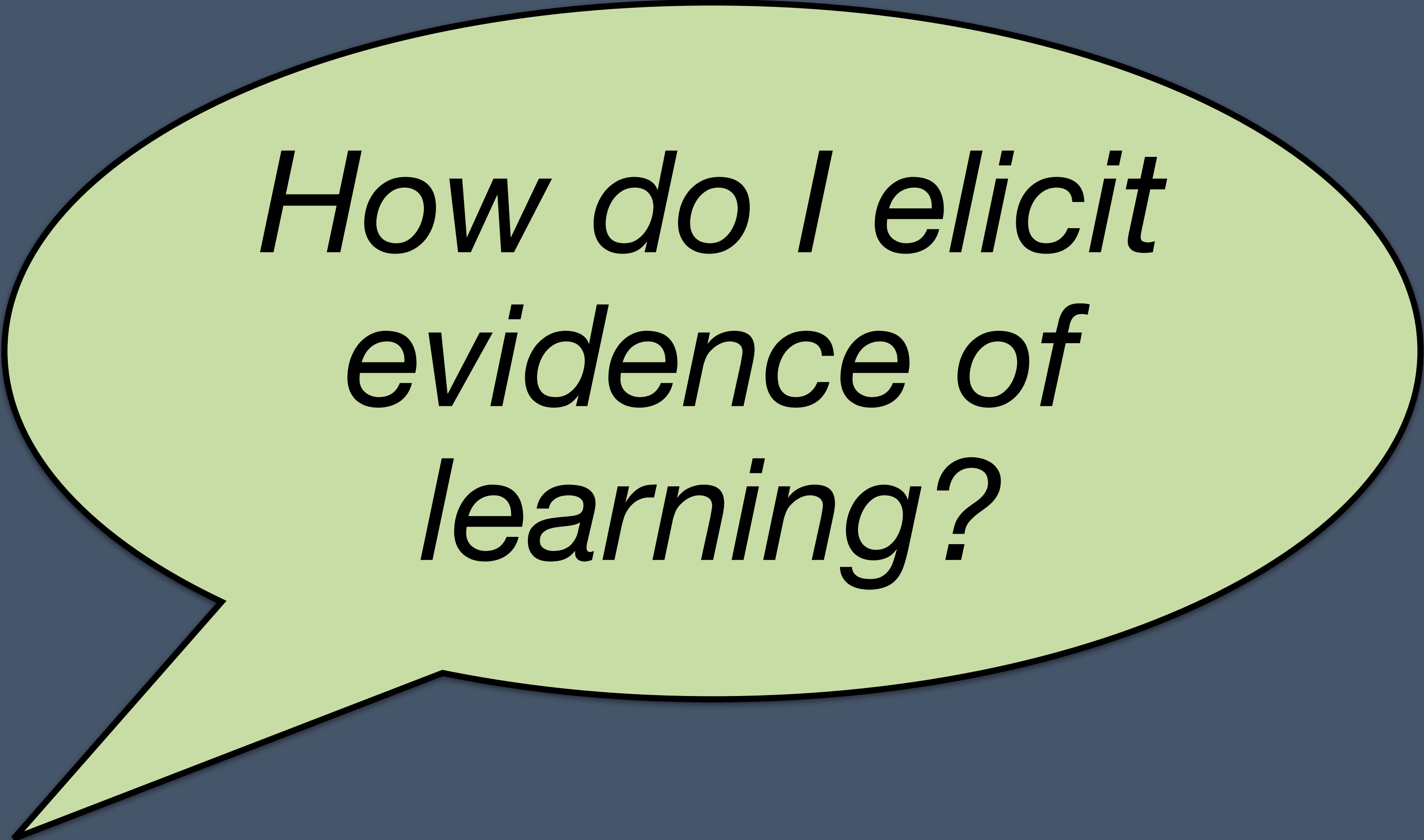
Use the information here—with whatever tools you want—to calculate the exact number of calories in the Triple Crème pack.

Enter your answer here.

ResponsesSummary

No responses yet...





*How do I elicit  
evidence of  
learning?*

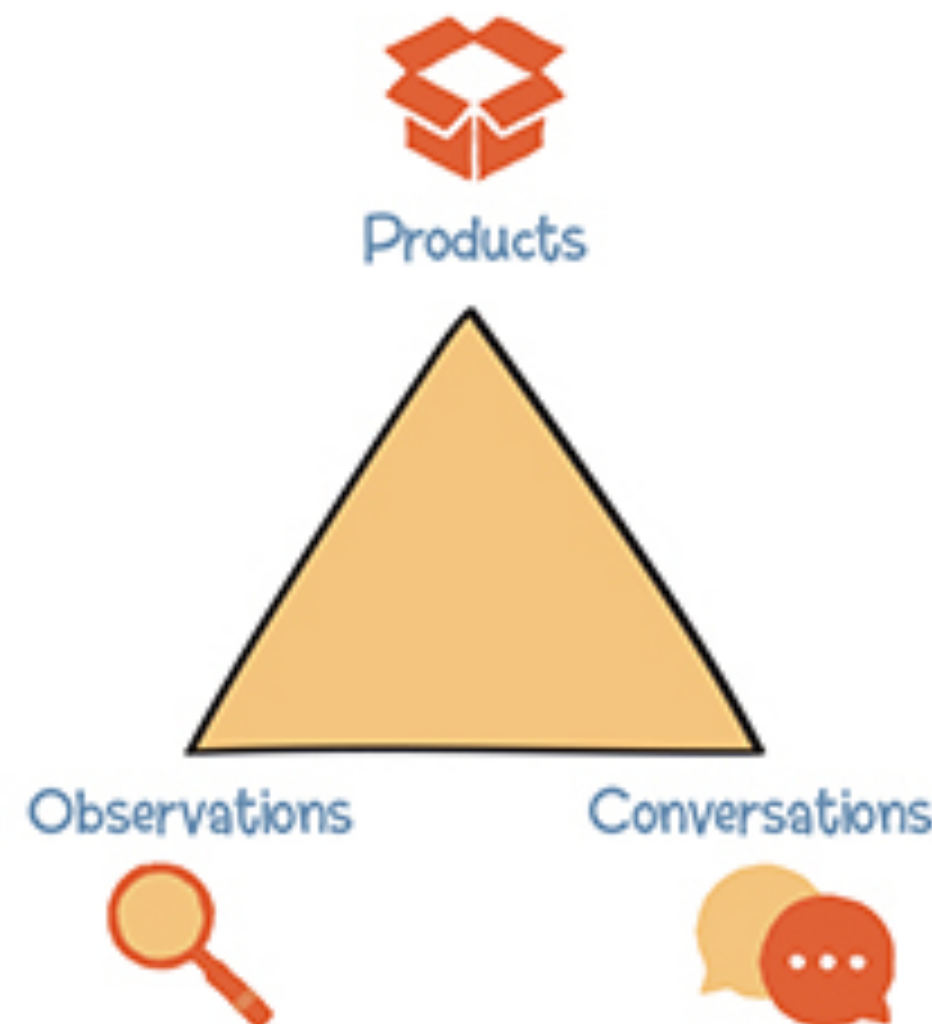


# SEEKING TRUTH VIA TRIANGULATION

Ideas by Peter Liljedahl & Sketchnote by @DaniellaGamba

## DATA SOURCES

Student learning can be documented through multiple sources of data



## MISCONCEPTION

Triangulation is NOT about averaging the data from multiple sources

$$\bar{X} = \frac{\text{Products} + \text{Observations} + \text{Conversations}}{n}$$

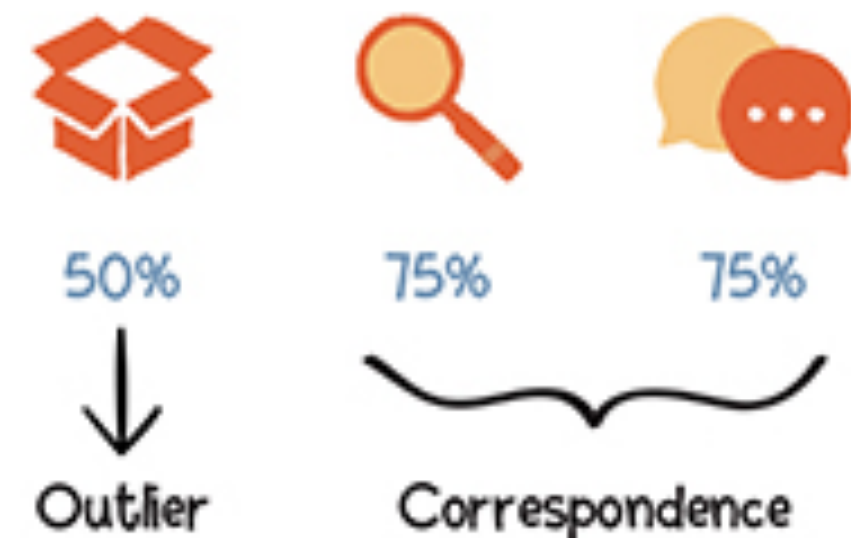
### TYRANNY OF OBJECTIVITY

Averaging in this manner is a form of grade deflation.



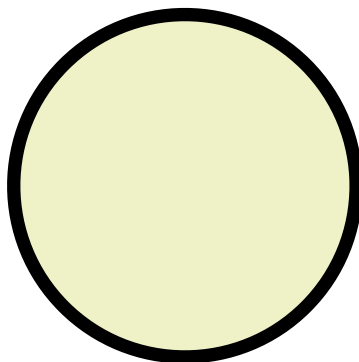
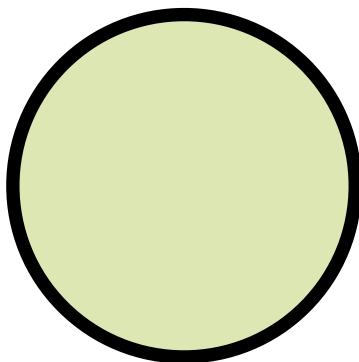
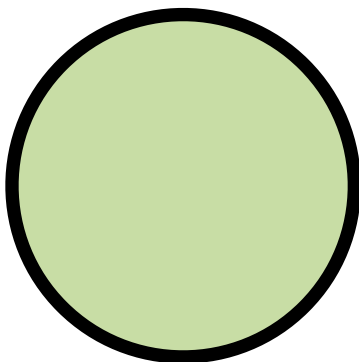
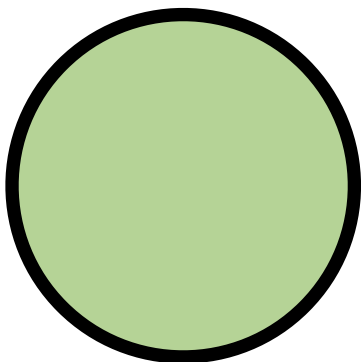
## CORRESPONDENCE

Triangulation seeks correspondence between multiple sources of data



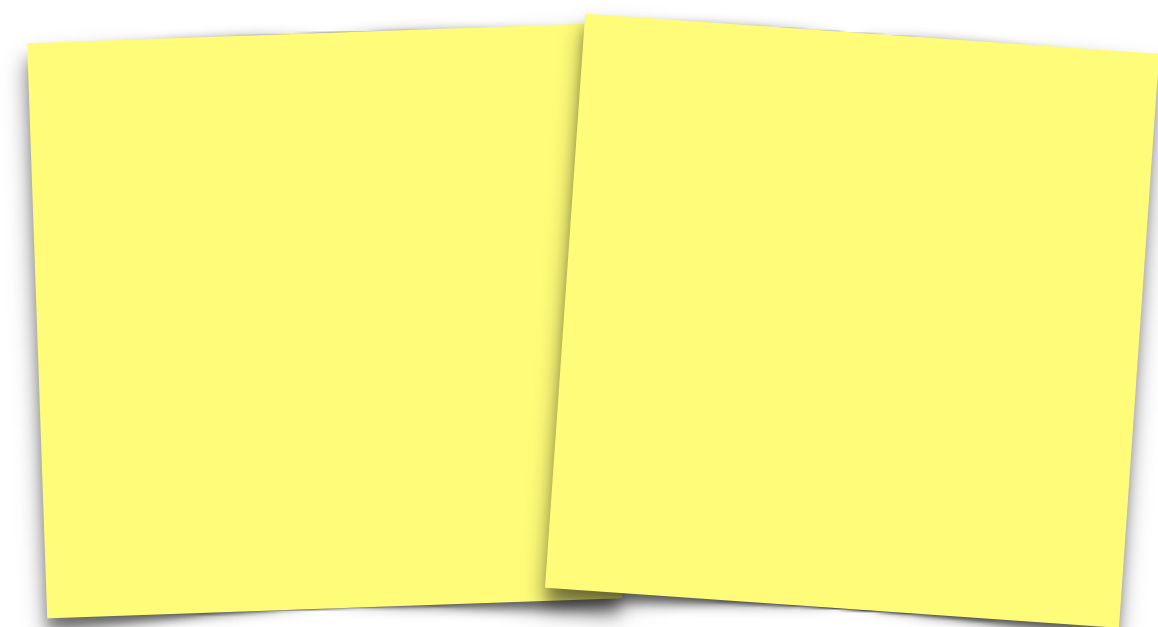
### RULE OF TWO

If there is correspondence between two data forms, then it is unnecessary or redundant to reference a third data form.

learning standard	Emerging	Developing	Proficient	Extending
				

learning standard	Emerging	Developing	Proficient	Extending
				




$$= 0 \quad \textcircled{1}$$
$$= 0 \quad \textcircled{2}$$

$$10p + 6q + 38 = 0$$

$$-10p + 25q + 55 = 0$$

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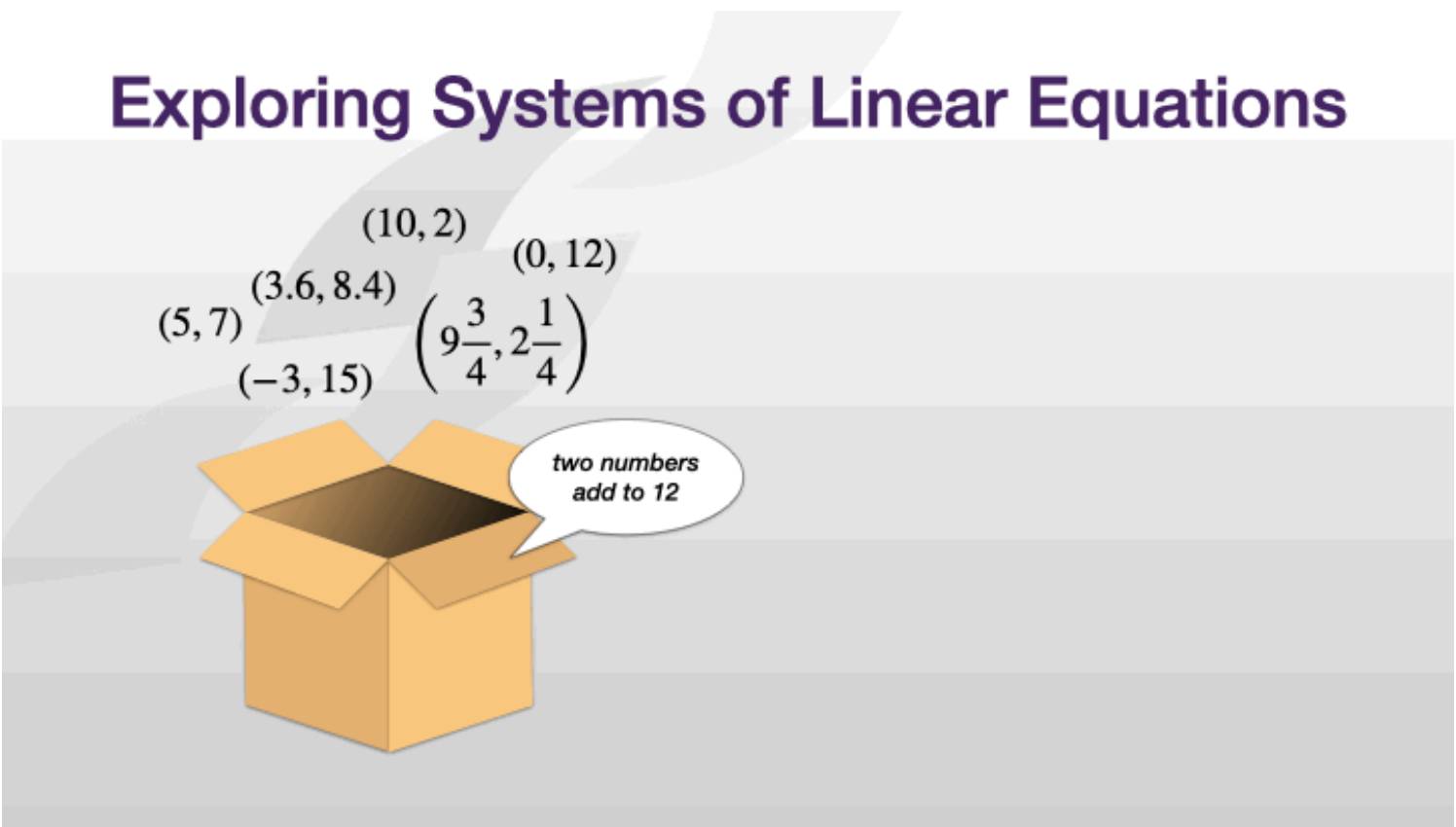
$$31q + 93 = 0$$

$$31q = -93$$

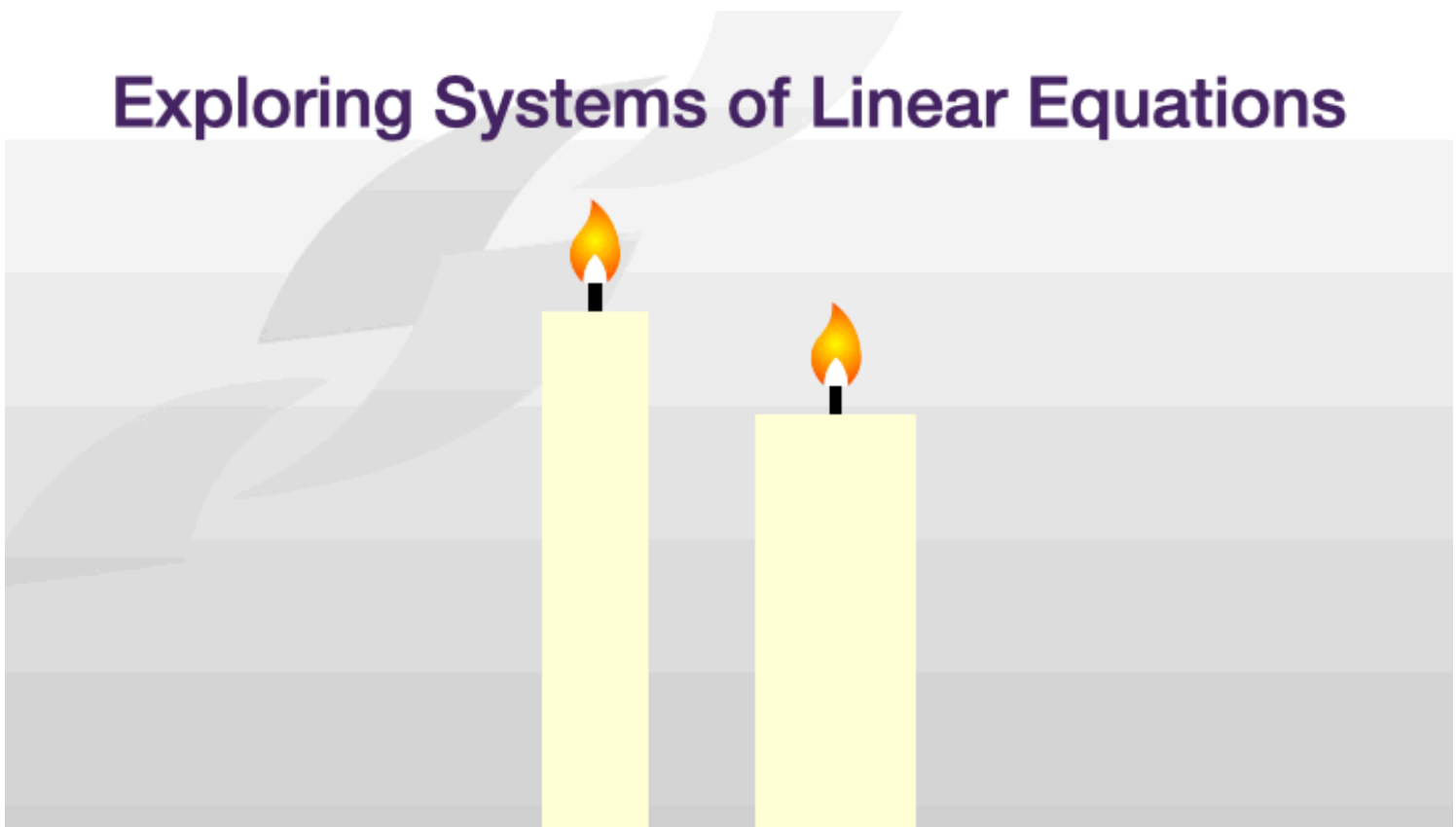
$$q = -3$$

# chrishunter.ca/2020/11/23/principles-of-math-videos/

## Exploring Systems of Linear Equations



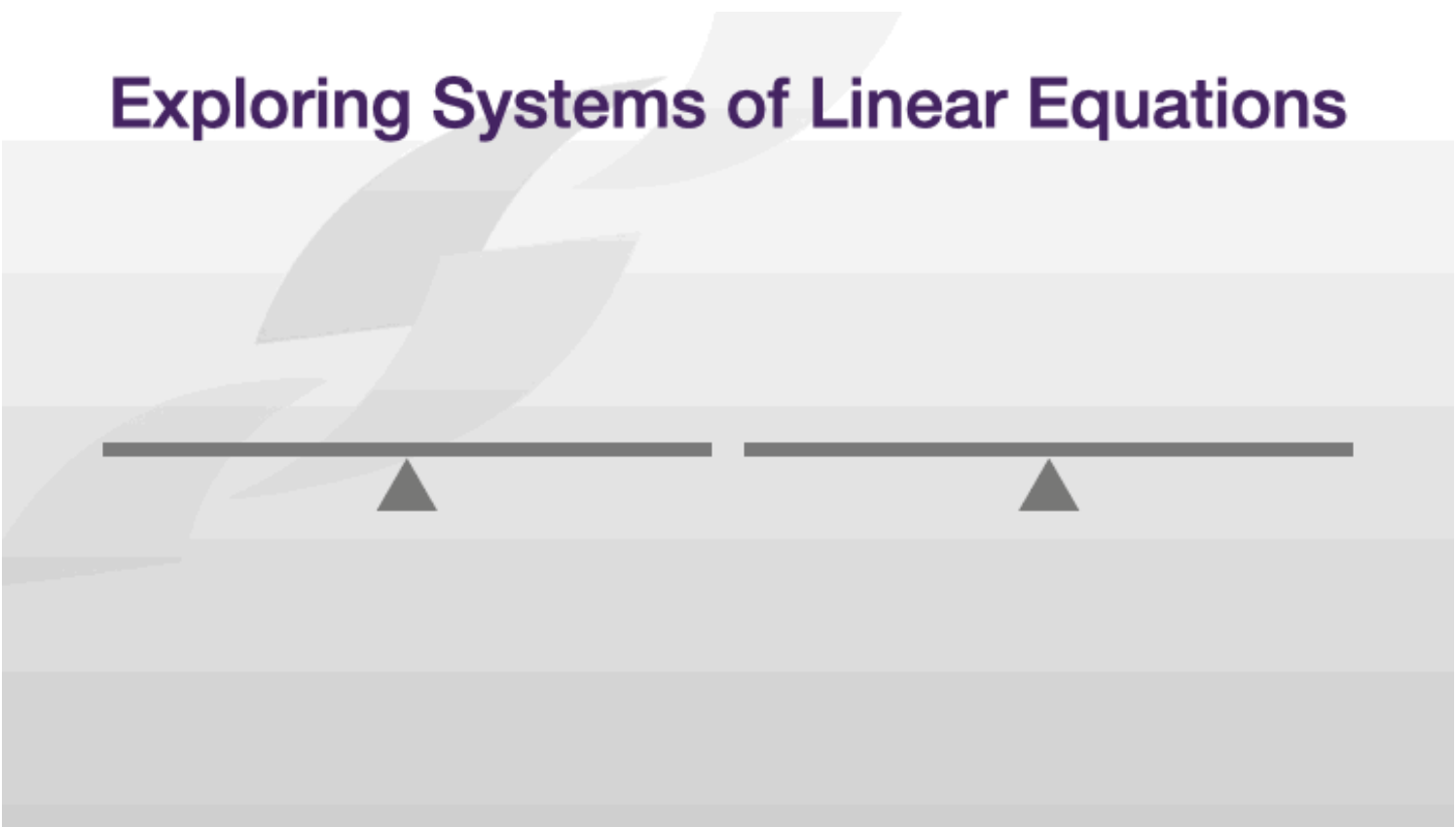
## Exploring Systems of Linear Equations



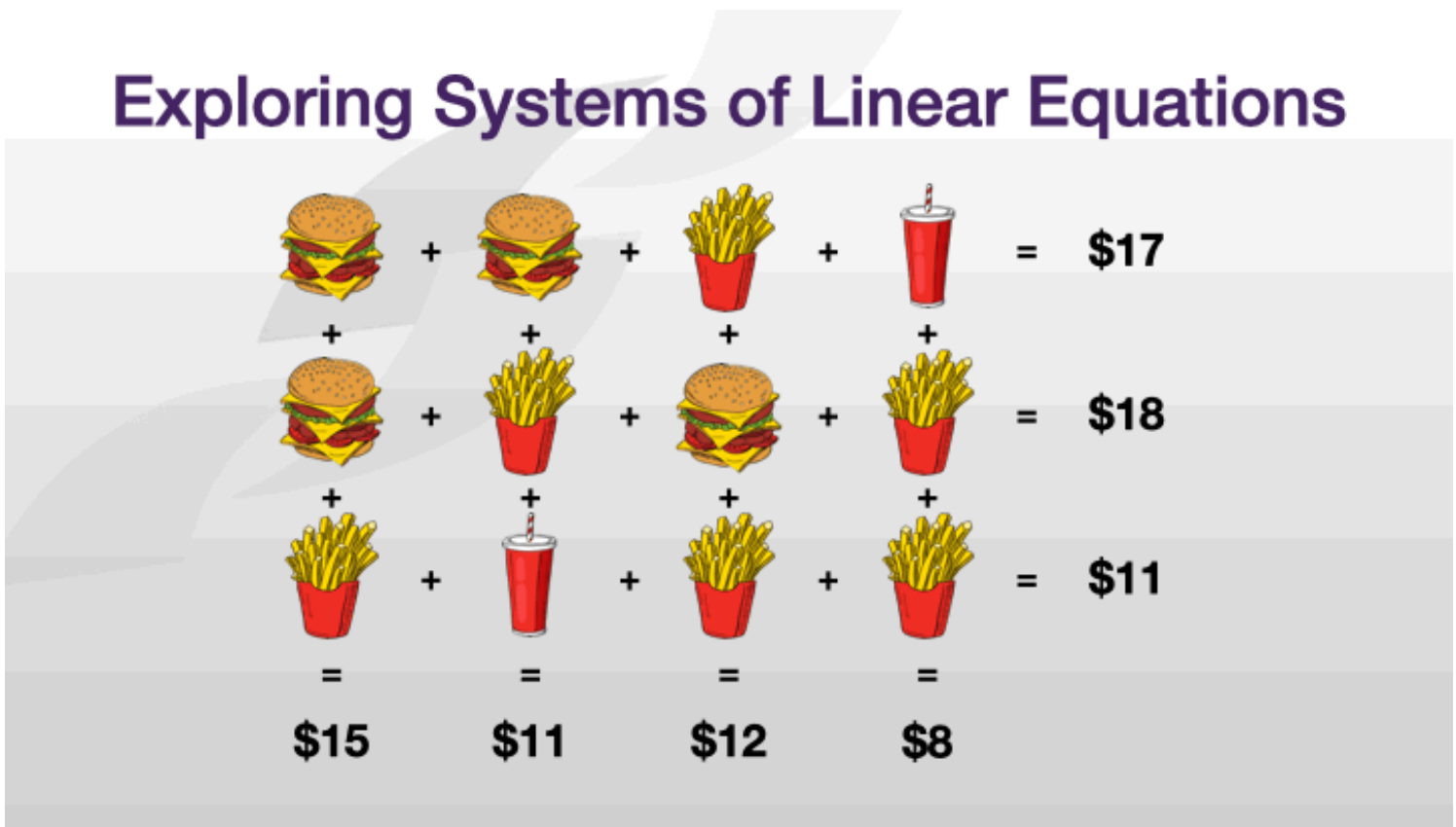
## Applying Systems of Linear Equations



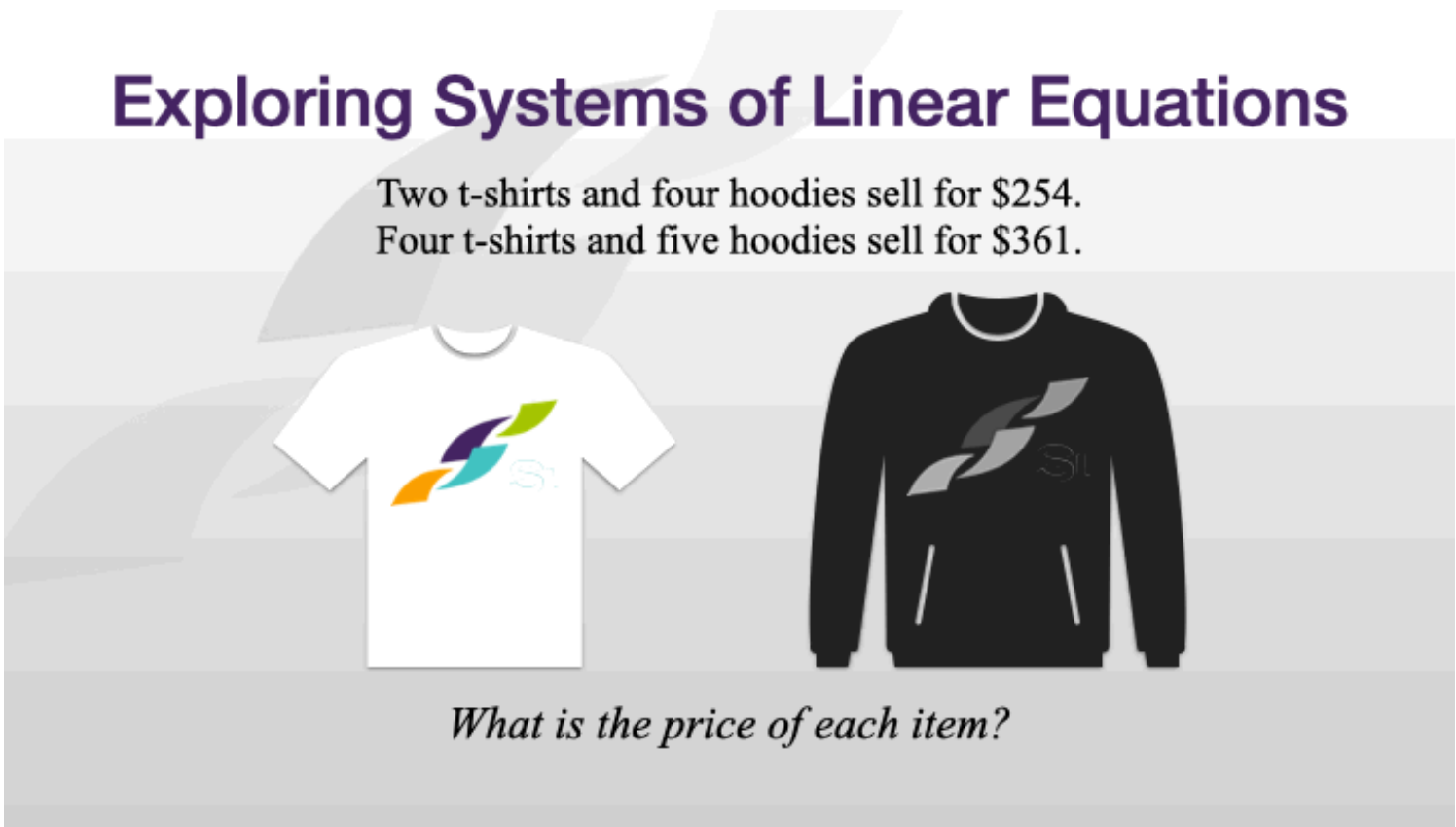
## Exploring Systems of Linear Equations



## Exploring Systems of Linear Equations



## Exploring Systems of Linear Equations



**Emerging**

**Solve Graphically**

**Solve Algebraically**

**Model Contextual Problems**

**VS.**

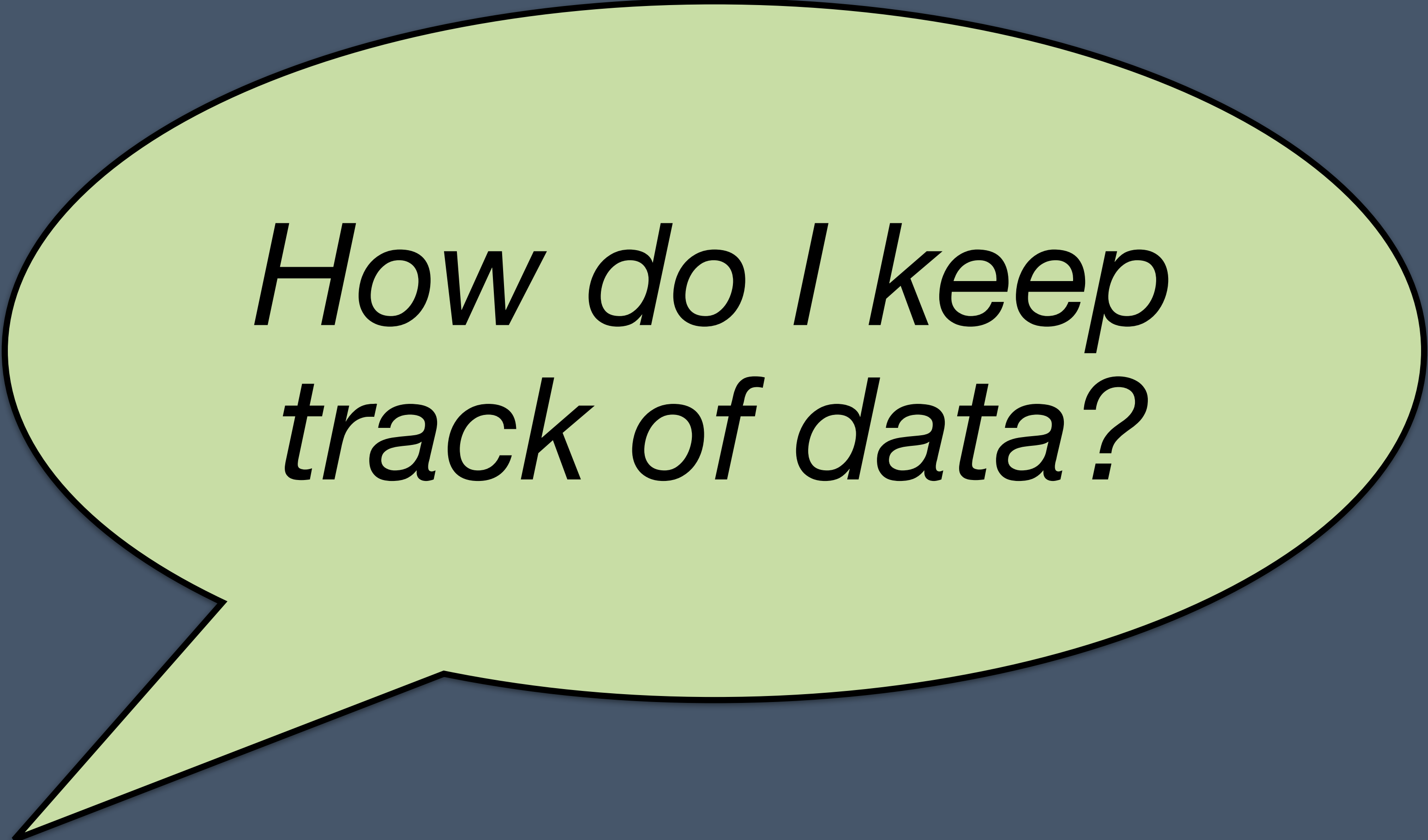
**Solve Graphically**

**Emerging**

**Developing**

**Proficient**

**Extending**



*How do I keep  
track of data?*





Name	Learning Outcome									
	1	2	3	4	5	6	7	8	9	10
Aaron	Ex	P	Ex	P	P	P	P	Ex	P	P
Blake	D	Em	Ex	P	P	Em	D	Ex	P	D
Denise	D	Em	P	D	P	D	Em	D	D	Em
...										

D P P Ex Ex → Ex

BUILDING  
**THINKING  
CLASSROOMS**  
in MATHEMATICS

GRADES K-12

**14** TEACHING  
PRACTICES  
FOR ENHANCING  
LEARNING



**PETER LILJEDAH**

FOREWORD BY TRACY JOHNSTON ZAGER

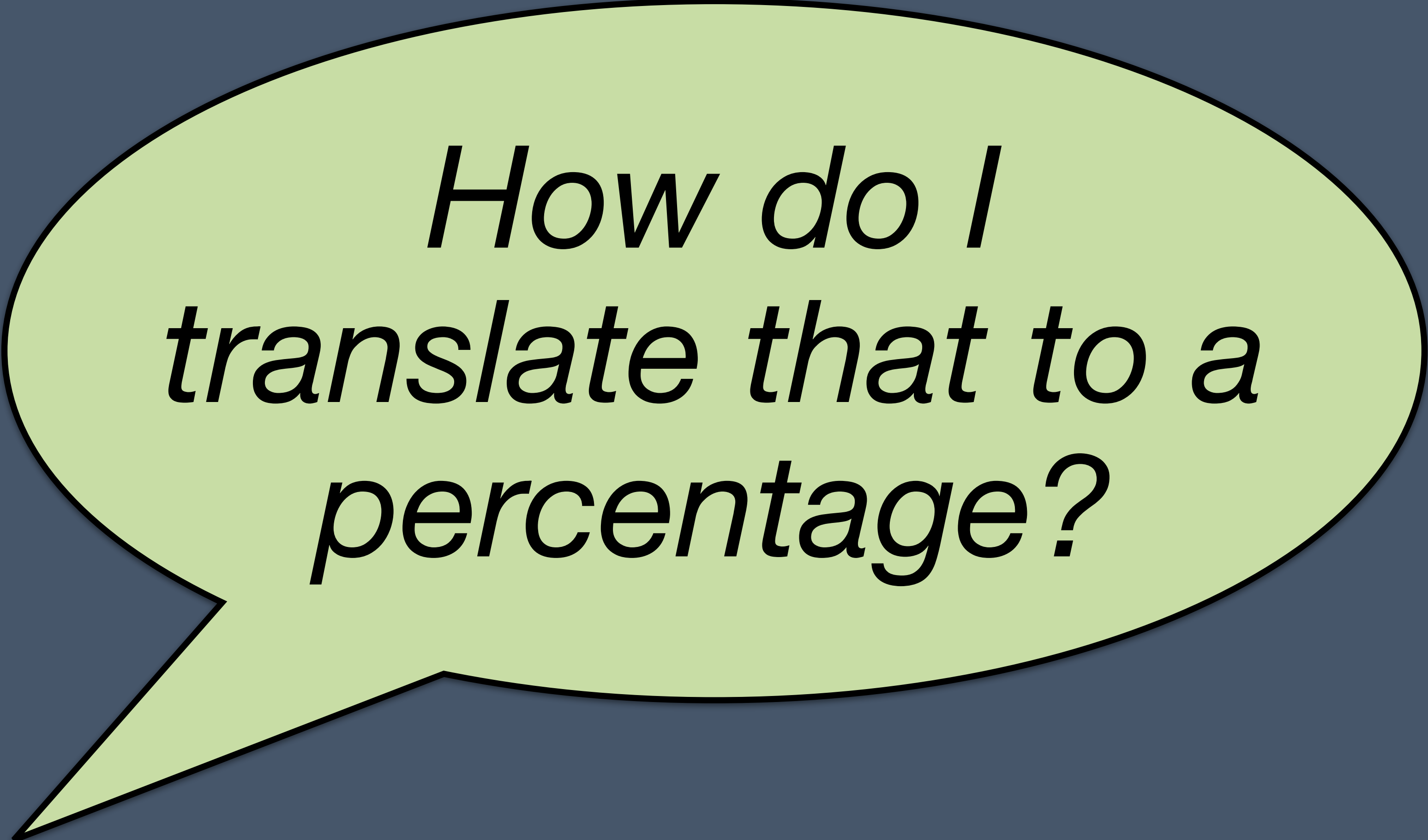
ILLUSTRATIONS BY LAURA WHEELER

CORWIN Mathematics

“The fact that she didn’t know how to do something in the beginning is expected—she is *learning*, not *learned*, and she shouldn’t be punished for her early-not-knowing.”

Peter Liljedahl





*How do I  
translate that to a  
percentage?*

<b>80</b>
<b>descriptor</b>

<b>79</b>	<b>80</b>	<b>81</b>
<b>descriptor</b>	<b>descriptor</b>	<b>descriptor</b>

	<b>B</b>	
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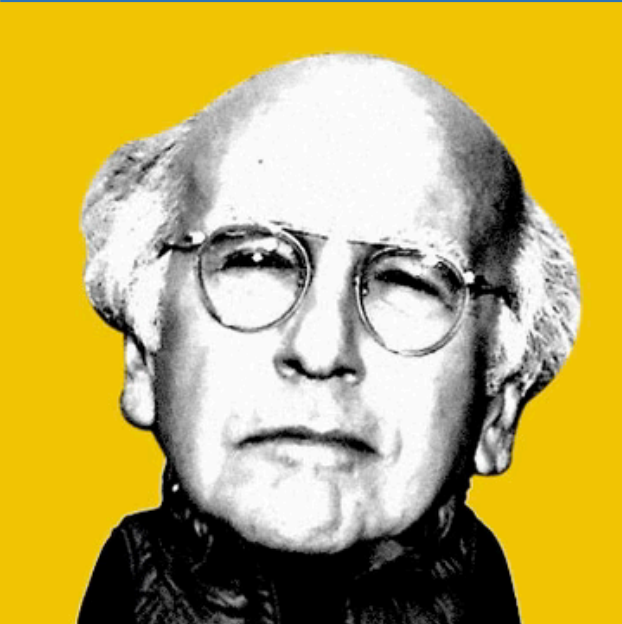
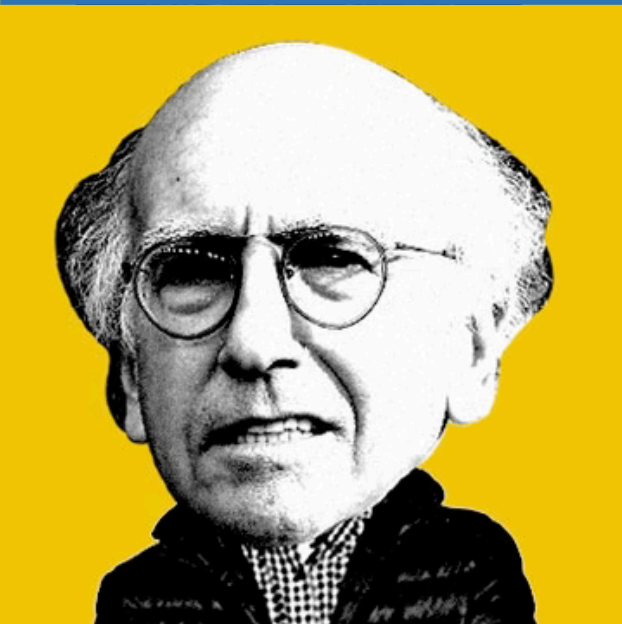
	<b>73</b>	<b>74</b>	<b>75</b>	<b>76</b>	<b>77</b>	<b>78</b>	<b>79</b>	<b>80</b>	<b>81</b>	<b>82</b>	<b>83</b>	<b>84</b>	<b>85</b>	
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[illegible]





Letter Grade	Percentage Range	Definition
A	86 - 100	The student demonstrates excellent or outstanding performance in relation to the learning outcomes for the course or subject and grade.
B	73 – 85	The student demonstrates very good performance in relation to the learning outcomes for the course or subject and grade
C+	67 – 72	The student demonstrates good performance in relation to the learning outcomes for the course or subject and grade.
C	60 – 66	The student demonstrates satisfactory performance in relation to the expected learning outcomes for the course or subject and grade.
C-	50 – 59	The student demonstrates minimally acceptable performance in relation to the learning outcomes for the course or subject and grade.
F	0 – 49	The student has not demonstrated, or is not demonstrating, minimally acceptable performance in relation to the learning outcomes for the course or subject and grade.

Letter Grade	Percentage Range	Definition	
Hi-B	82 – 85	The student demonstrates <b>pretty, pretty, pretty, pretty good</b> performance in relation to the learning outcomes for the course or subject and grade.	
Mid-B	77 – 81	The student demonstrates <b>pretty, pretty, pretty good</b> performance in relation to the learning outcomes for the course or subject and grade.	
Lo-B	73 – 76	The student demonstrates <b>pretty, pretty good</b> performance in relation to the learning outcomes for the course or subject and grade.	

F										C-										C						C+				B										A																							
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
descriptor										descriptor										descriptor						descriptor				descriptor										descriptor																							



1-2-3-4

Aaron				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

$$\frac{(7 \times 3) + (3 \times 4)}{10 \times 4} = \frac{33}{40} = 83 \%$$

Blake				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

$$\frac{(2 \times 1) + (3 \times 2) + (3 \times 3) + (2 \times 4)}{10 \times 4} = \frac{25}{40} = 63 \%$$

Denise				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

$$\frac{(3 \times 1) + (5 \times 2) + (2 \times 3)}{10 \times 4} = \frac{19}{40} = 48 \%$$

2-3-4-5

Aaron				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

$$\frac{(7 \times 4) + (3 \times 5)}{10 \times 5} = \frac{43}{50} = 86 \%$$

Blake				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

$$\frac{(2 \times 2) + (3 \times 3) + (3 \times 4) + (2 \times 5)}{10 \times 5} = \frac{35}{50} = 70 \%$$

Denise				
L0	Em	D	P	Ex
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

$$\frac{(3 \times 2) + (5 \times 3) + (2 \times 4)}{10 \times 5} = \frac{29}{50} = 58 \%$$



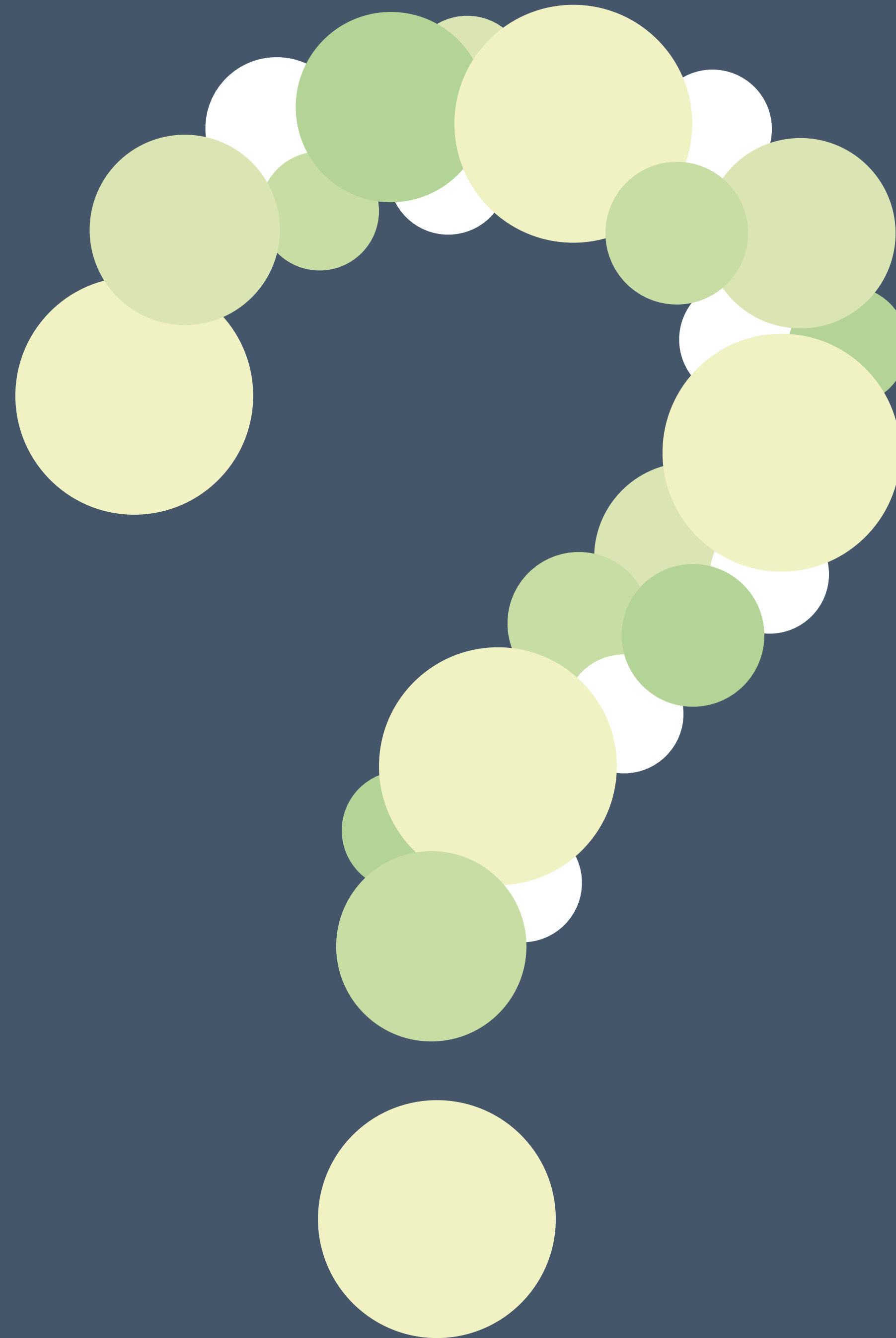
*What letter grade or percentage would **you** assign to Aaron, Blake, and Denise?*

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