

Functions Across Secondary Mathematics

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Chris Hunter

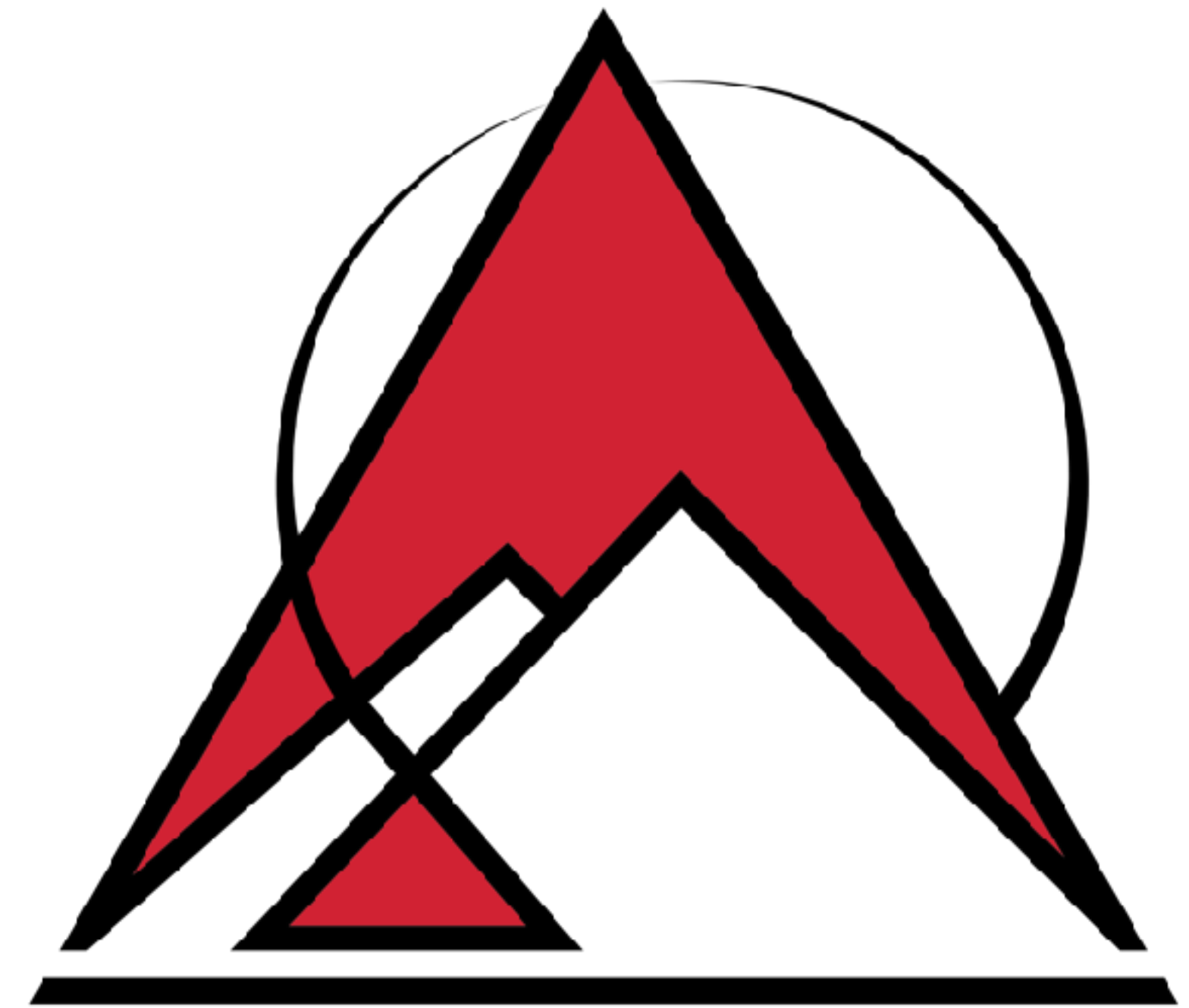
Past President

BCAMT

email: bcamt@bctf.ca

Twitter: @BCAMT

website: bcamt.ca



BCAMT

British Columbia Association
of Mathematics Teachers

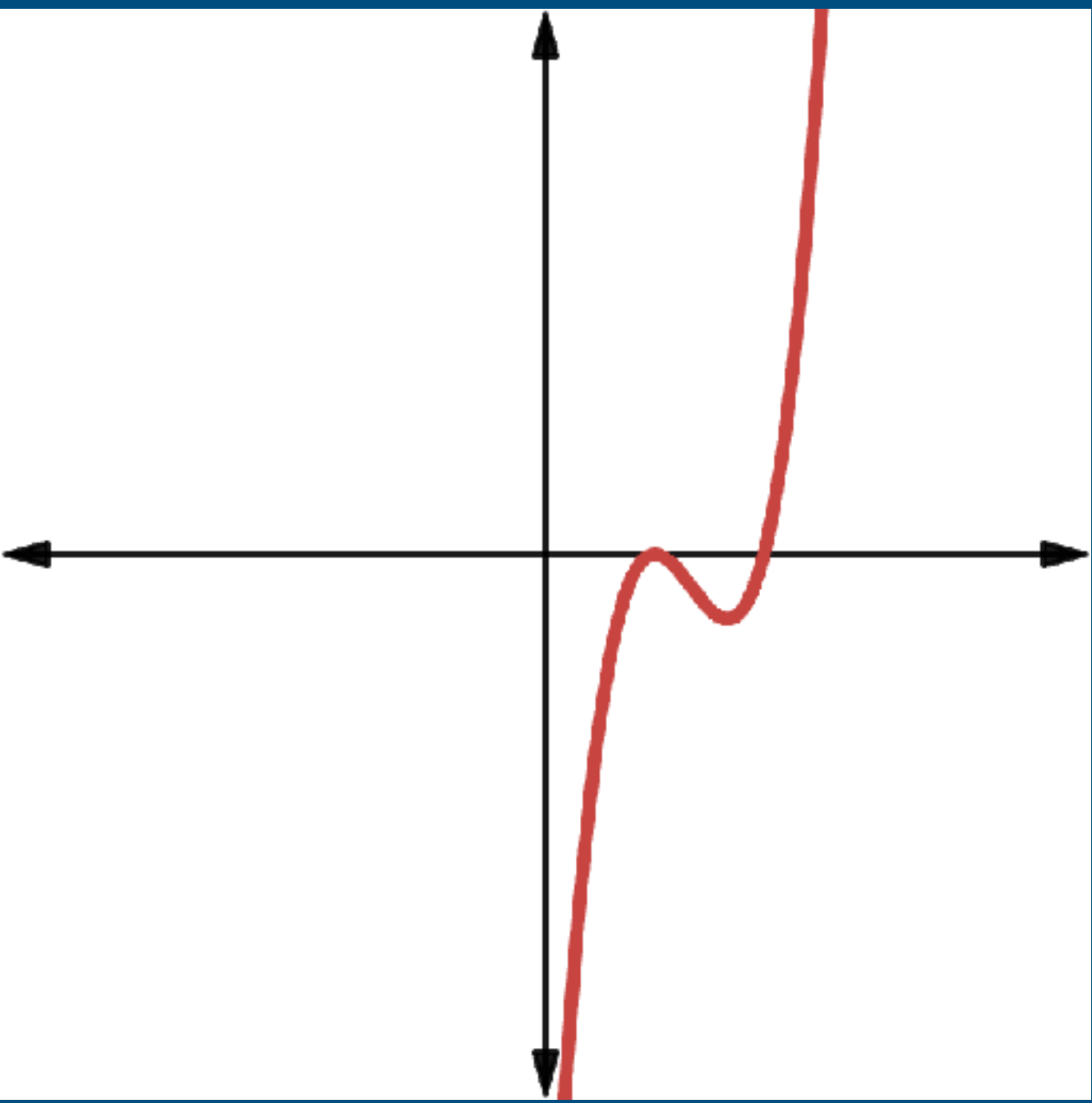
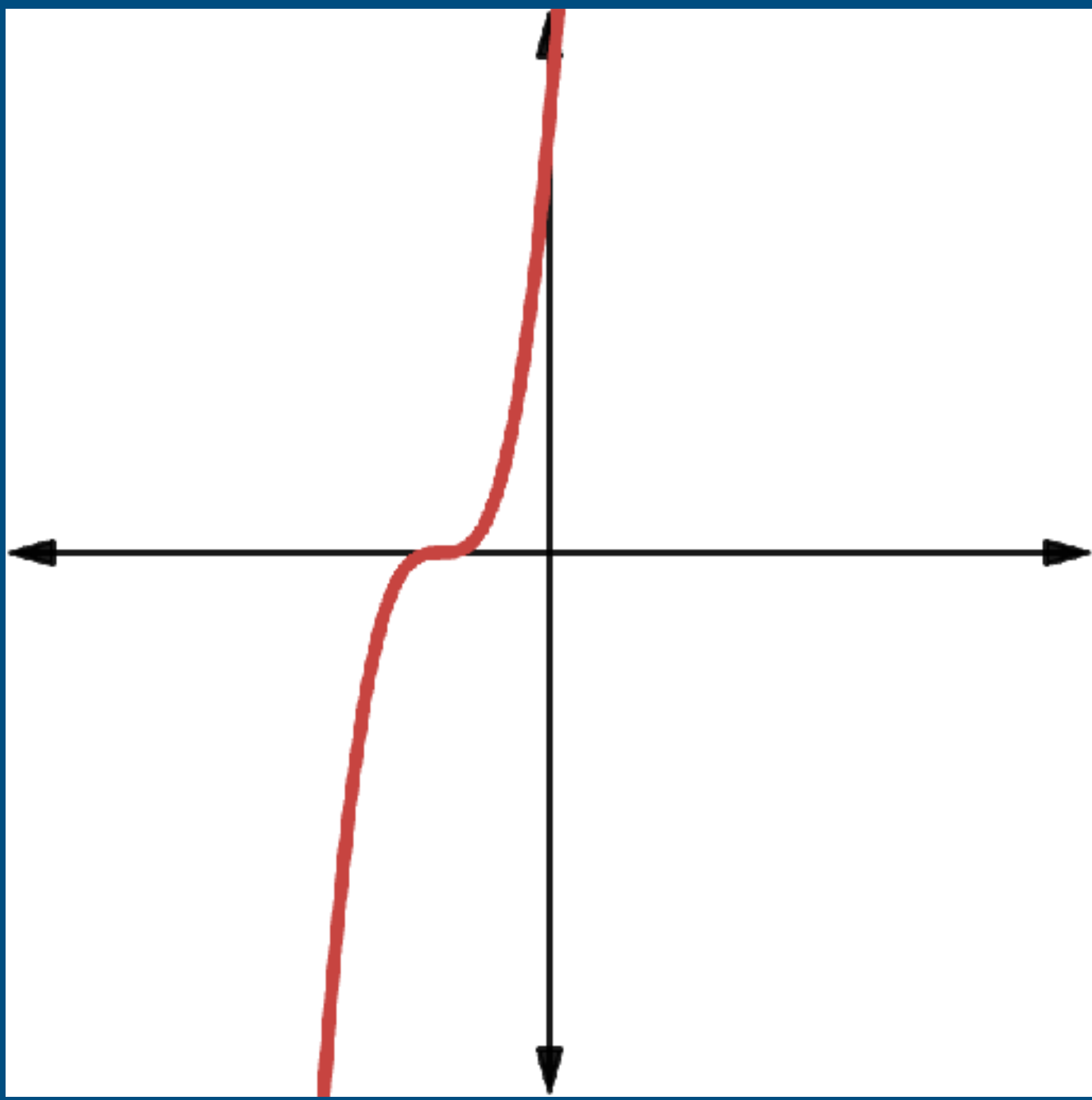
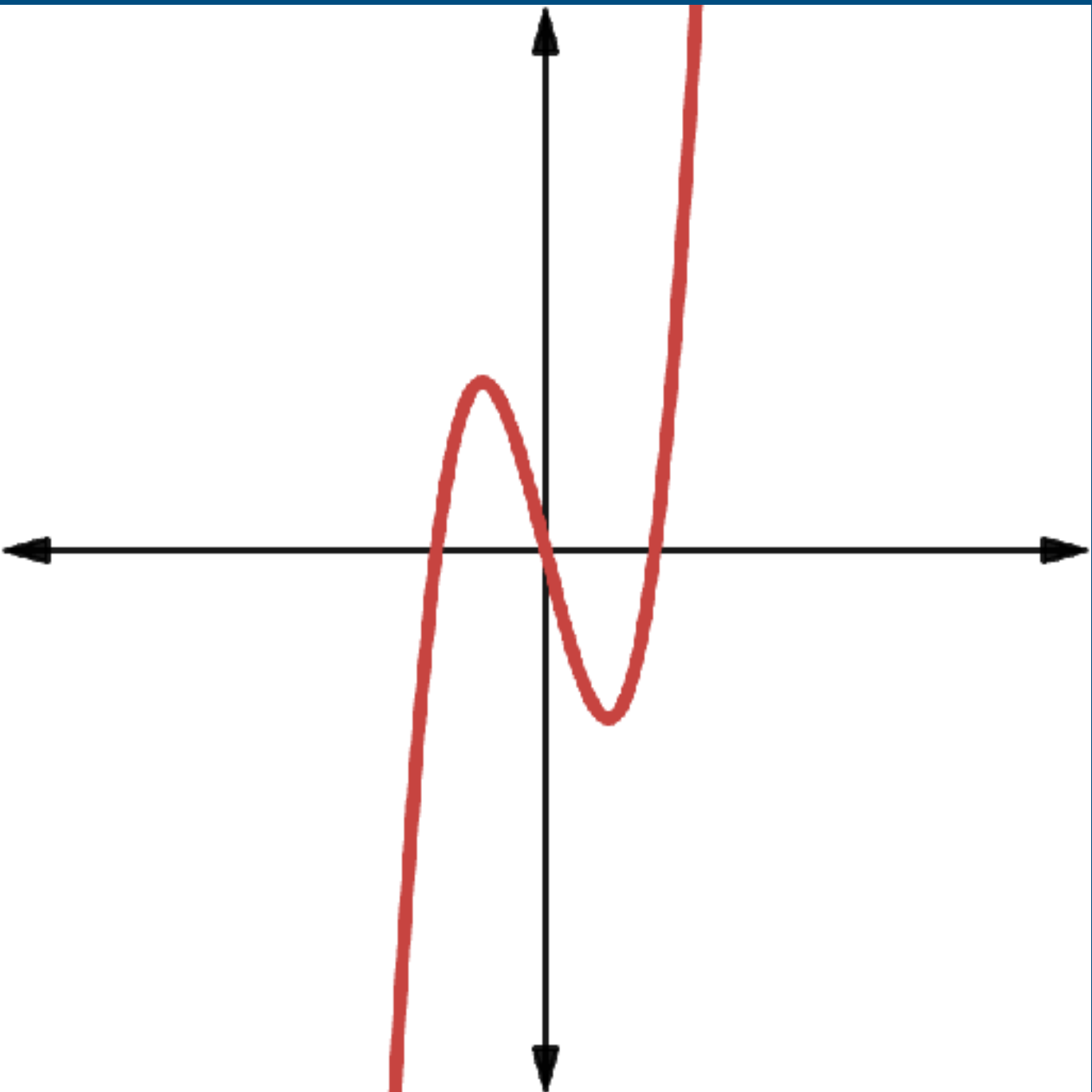
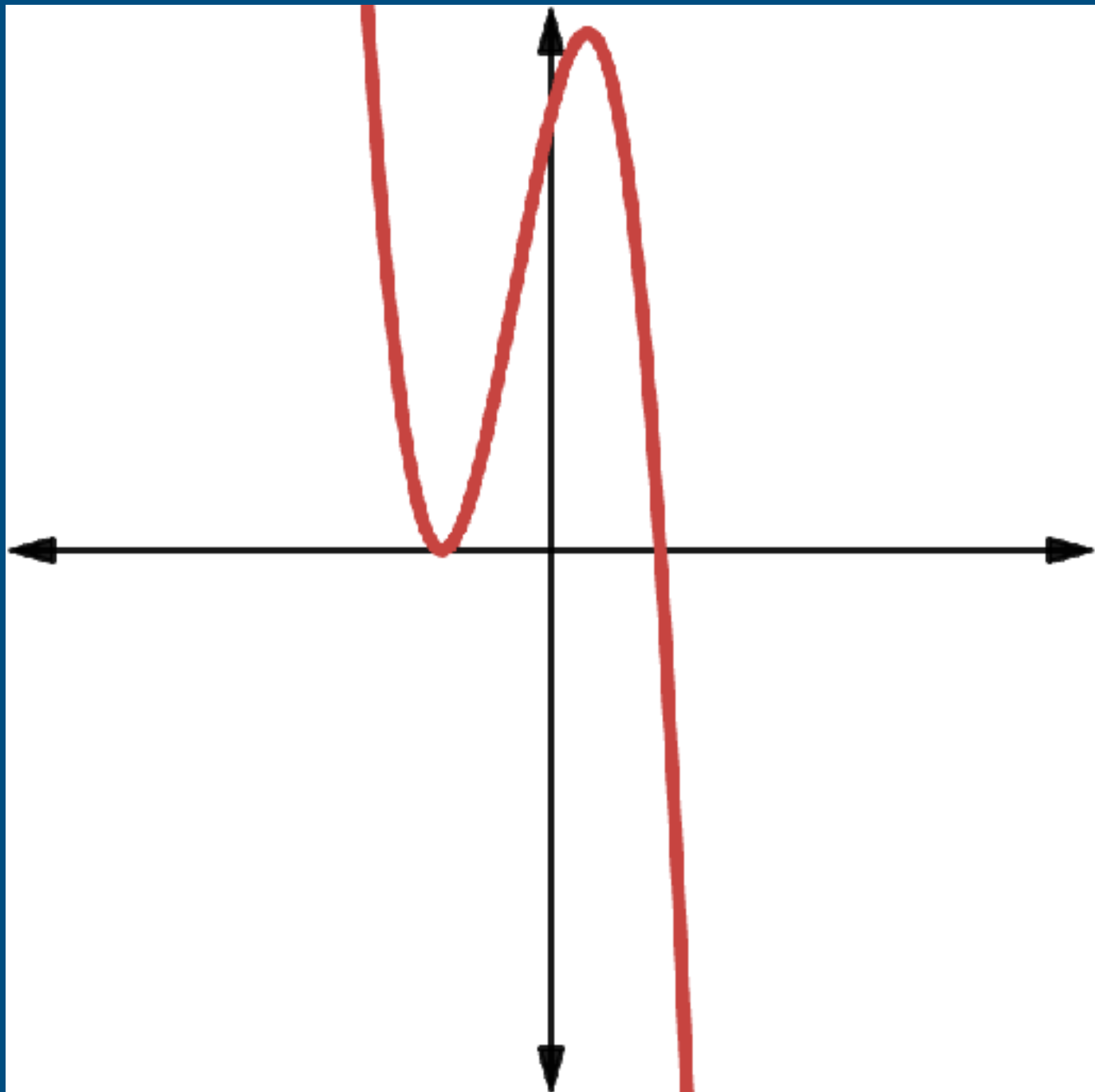
Which One Doesn't Belong?

_____ *does not belong because...*

What makes _____ *different from the others is...*

Only _____ *has* _____

All _____ *have* _____ *except* _____



10

functions and
relations

linear functions

10

functions and
relations
linear functions

11

quadratic
functions

10

functions and
relations
linear functions

11

quadratic
functions

12

transformations
exponential, logarithmic,
polynomial, rational, and
trigonometric functions

6

increasing and
decreasing
patterns

functional relationships
expressions, graphs, tables

7

linear relations

integral coordinates

8

linear relations

(larger) integral coordinates
equations, graphs, tables

8

linear relations

(larger) integral coordinates
equations, graphs, tables

9

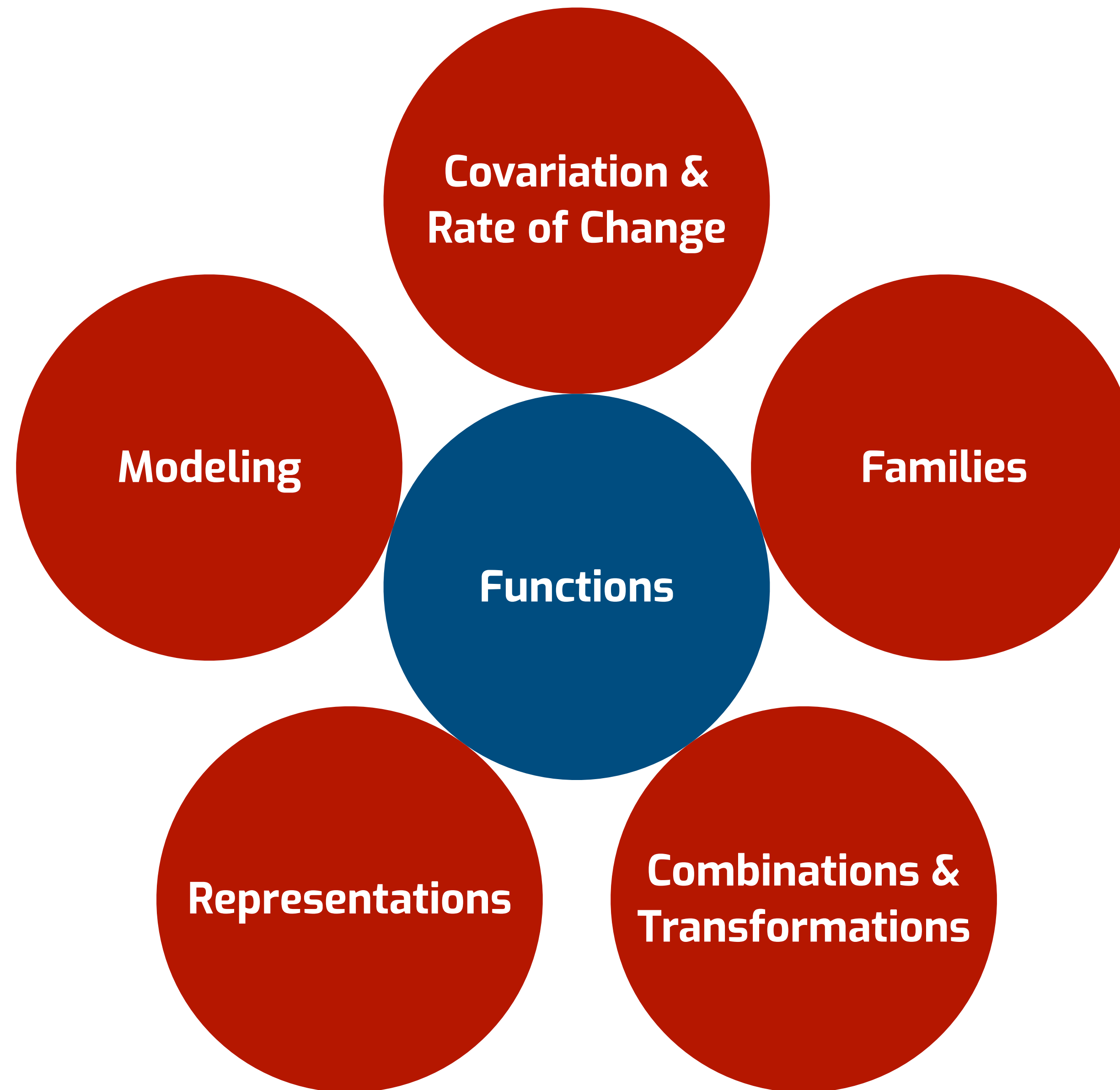
linear relations

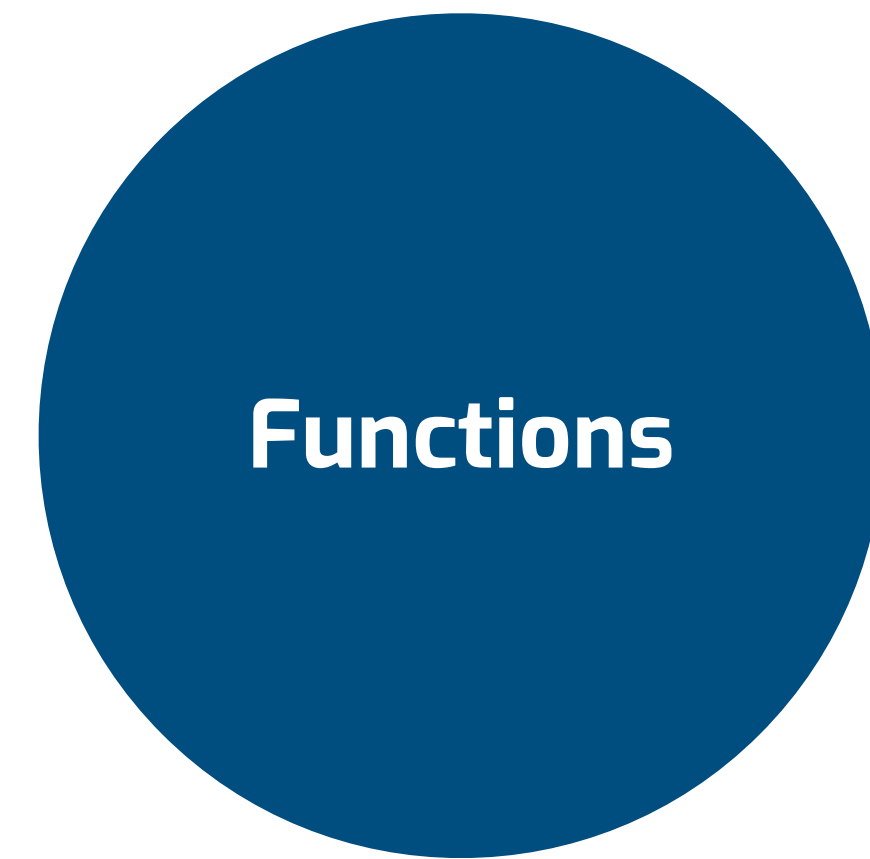
continuous
rational coordinates

10

functions and
relations
linear functions

slope
equations of lines





How do quantities relate to each other?

A

Polypad

What's the Function?

Save

Tiles

Geometry

Numbers

Fractions



Algebra

Algebra Tiles

Balance Scale

Function Machines

123456781010




Coordinate Axes and Tables

Variable Sliders

Probability and Data

Games and Applications

CH



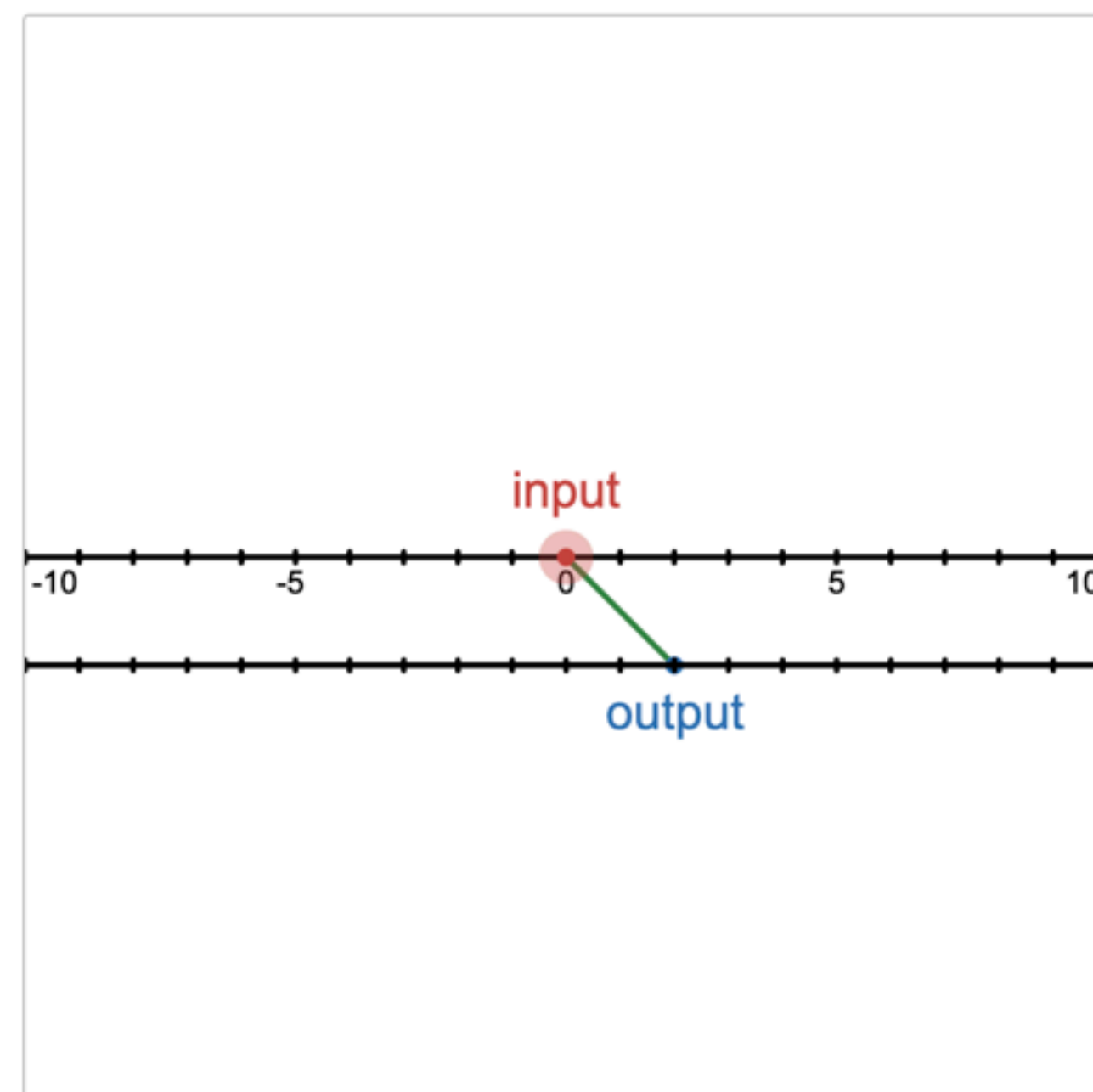


**Covariation &
Rate of Change**

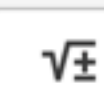
How do quantities change together?



Function #1



Drag the input point to explore the input and output values visually and numerically. What is the function f ? How do you know?

[Share With Class](#)

Anonymize Pace Sync to Me Pause

SORT BY Time Entered ▾

1 Dynagr...
A Dynagraph maps
input values / on
one number line to
output values $f(f)$

2 Functi...
Drag the
input

3 Functi...
Drag the
input

4 Functi...
Drag the
input

5 Functi...
Drag the
input

6 Functi...
Drag the
input

7 Functi...
Drag the
input

8 Functi...
Drag the
input

9 Functi...
Drag the
input

10 Funct...
Drag the
input

11 >

Hey, students!

Go to student.amplify.com/join and type in:

9W A2 G9

You can also share this invitation link with your students:

<https://student.amplify.com/join/9WA2G9> COPY

Have all students joined this class?

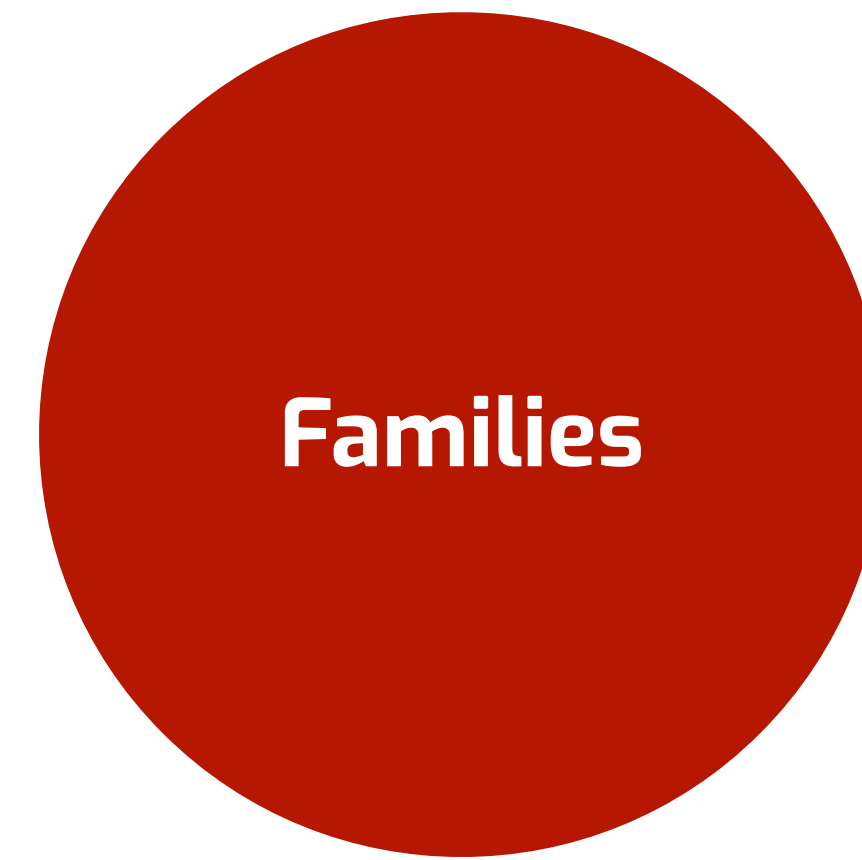
This prevents additional students from joining. You can always reactivate the code.

Deactivate this invite code

Do additional students need to join the class?

New students can use the code to join until **Nov 7, 2025**

Change Date



What are the important characteristics of ... ?

WANTED

QUADRATIC FUNCTION (A.K.A. “PARABOLA”)...

... OPENS UP

... POSITIVE Y-INTERCEPT

... NO X-INTERCEPTS

... NEVER ENTERS QIII

... VERTEX IN QII

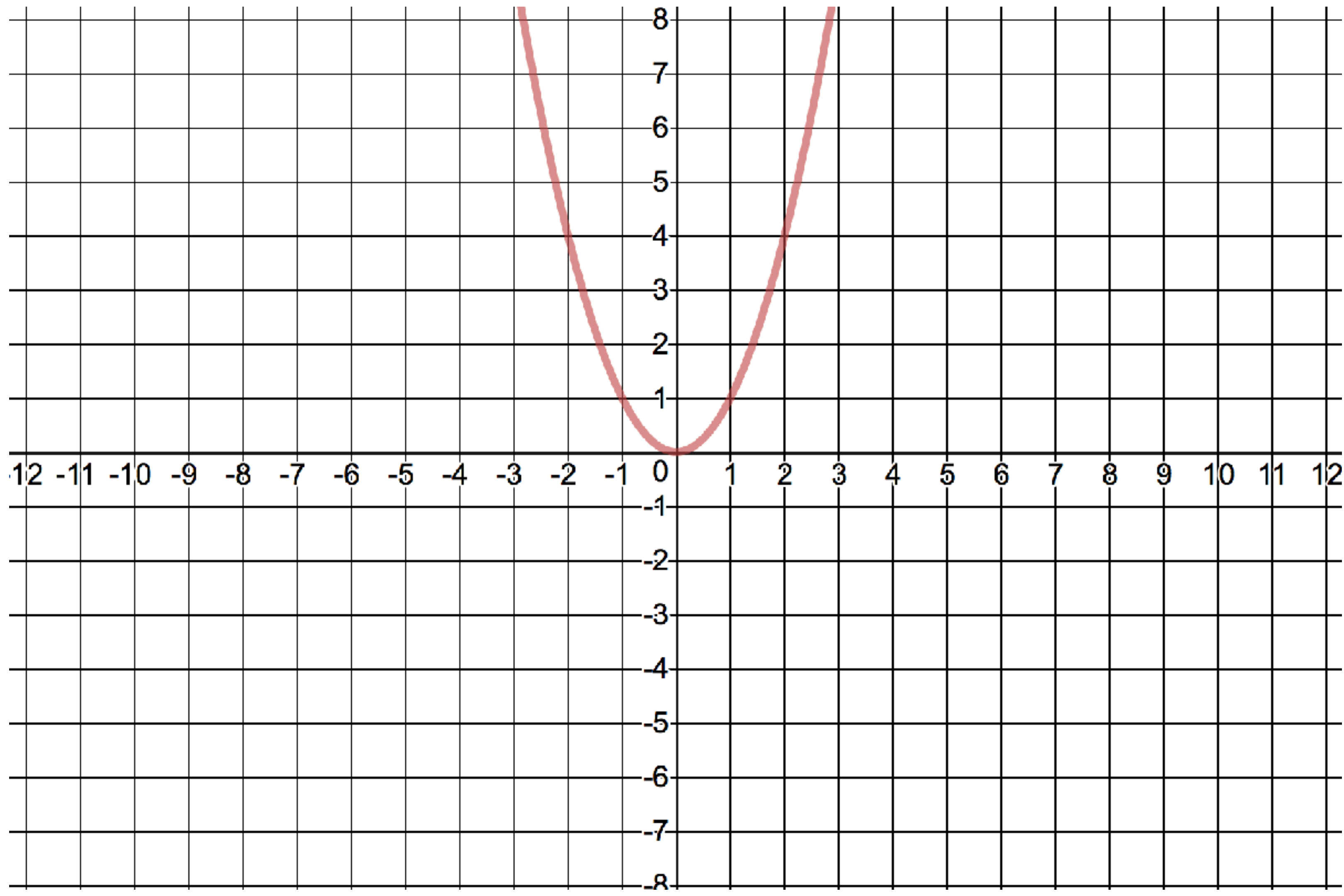
... MINIMUM VALUE OF 3

... AXIS OF SYMMETRY $x = -5$

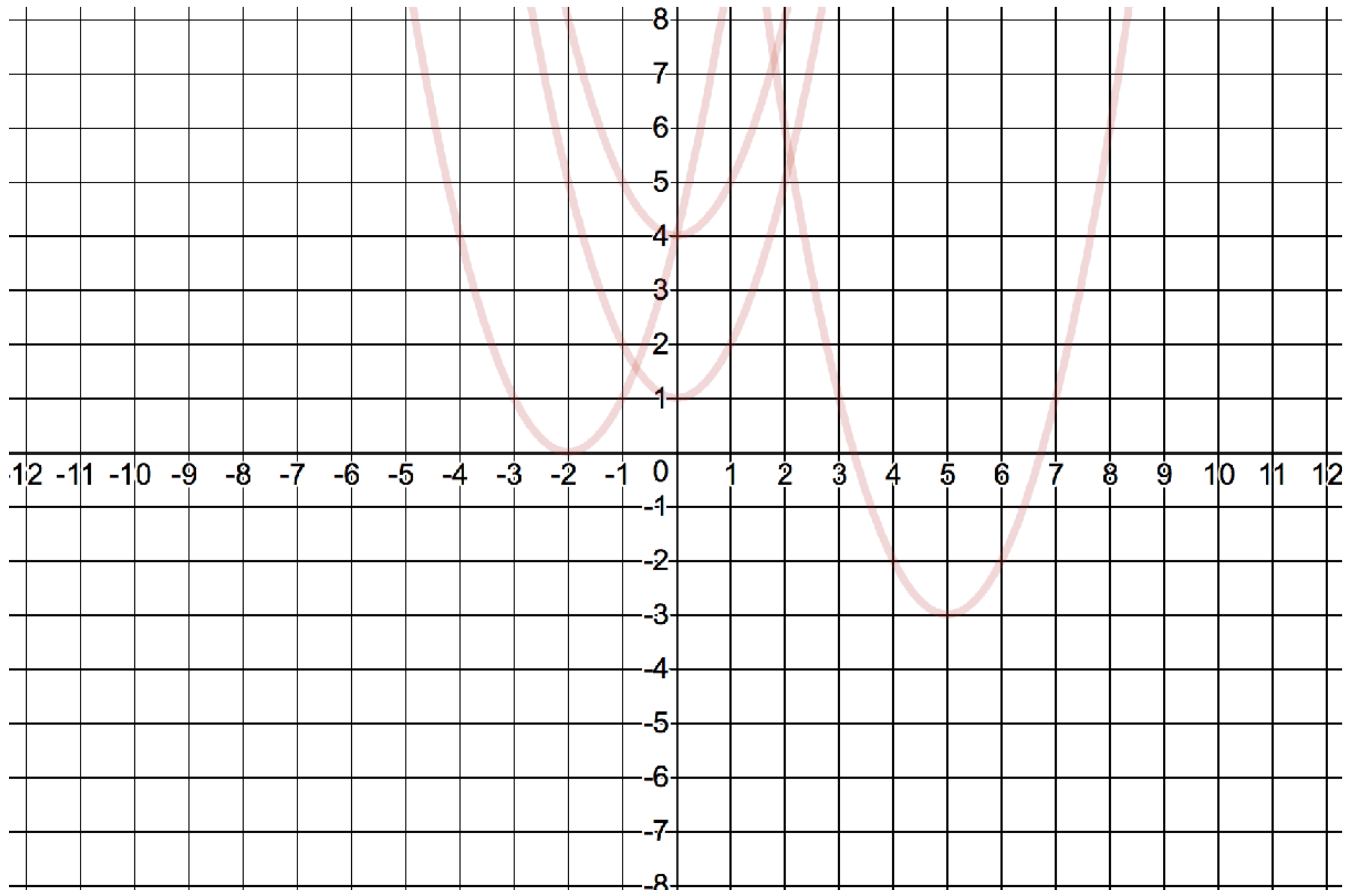
... VERTICALLY STRETCHED

... PASSES THROUGH $(-7, 15)$

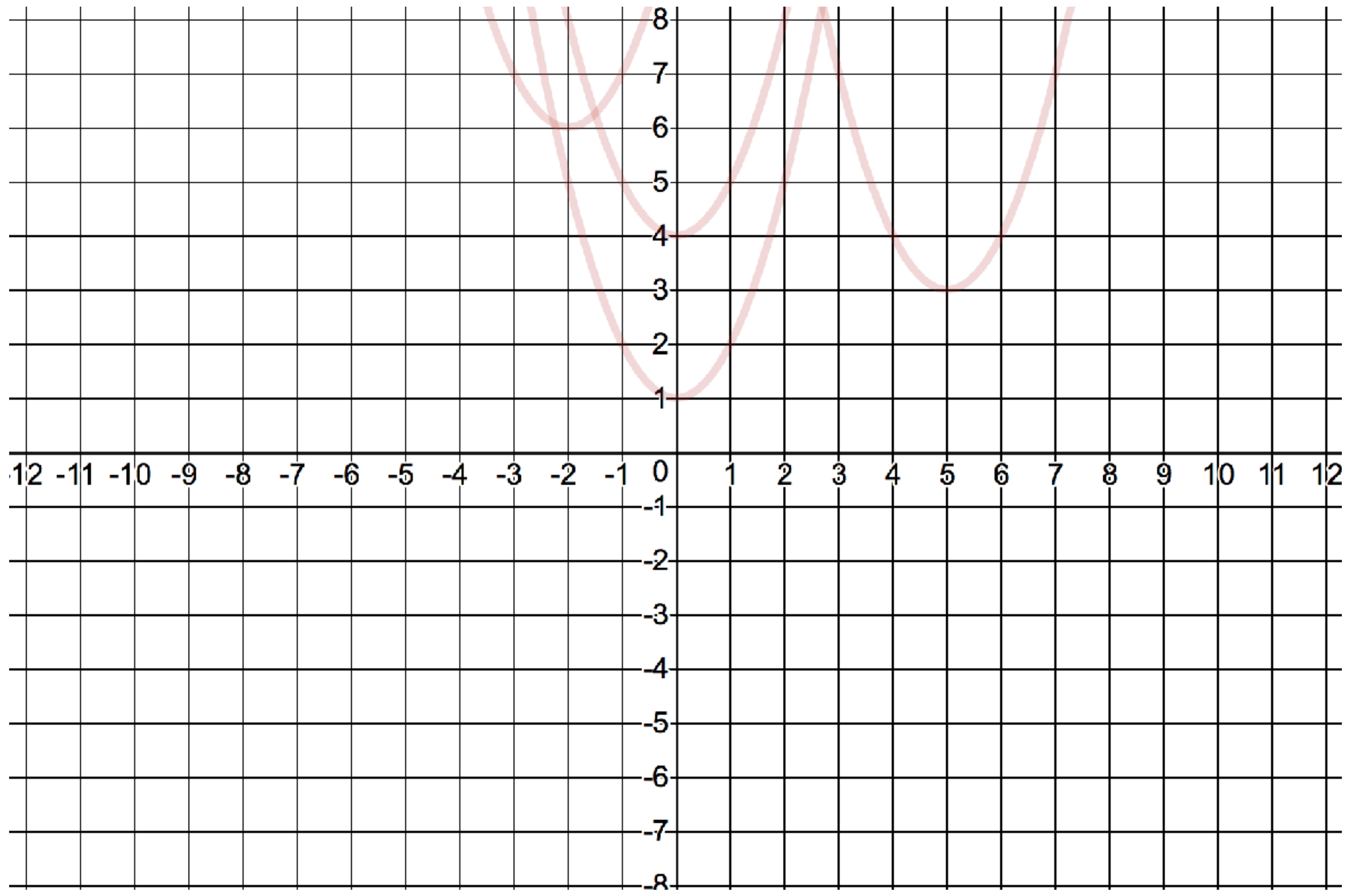
... VERTEX $(-5, 3)$



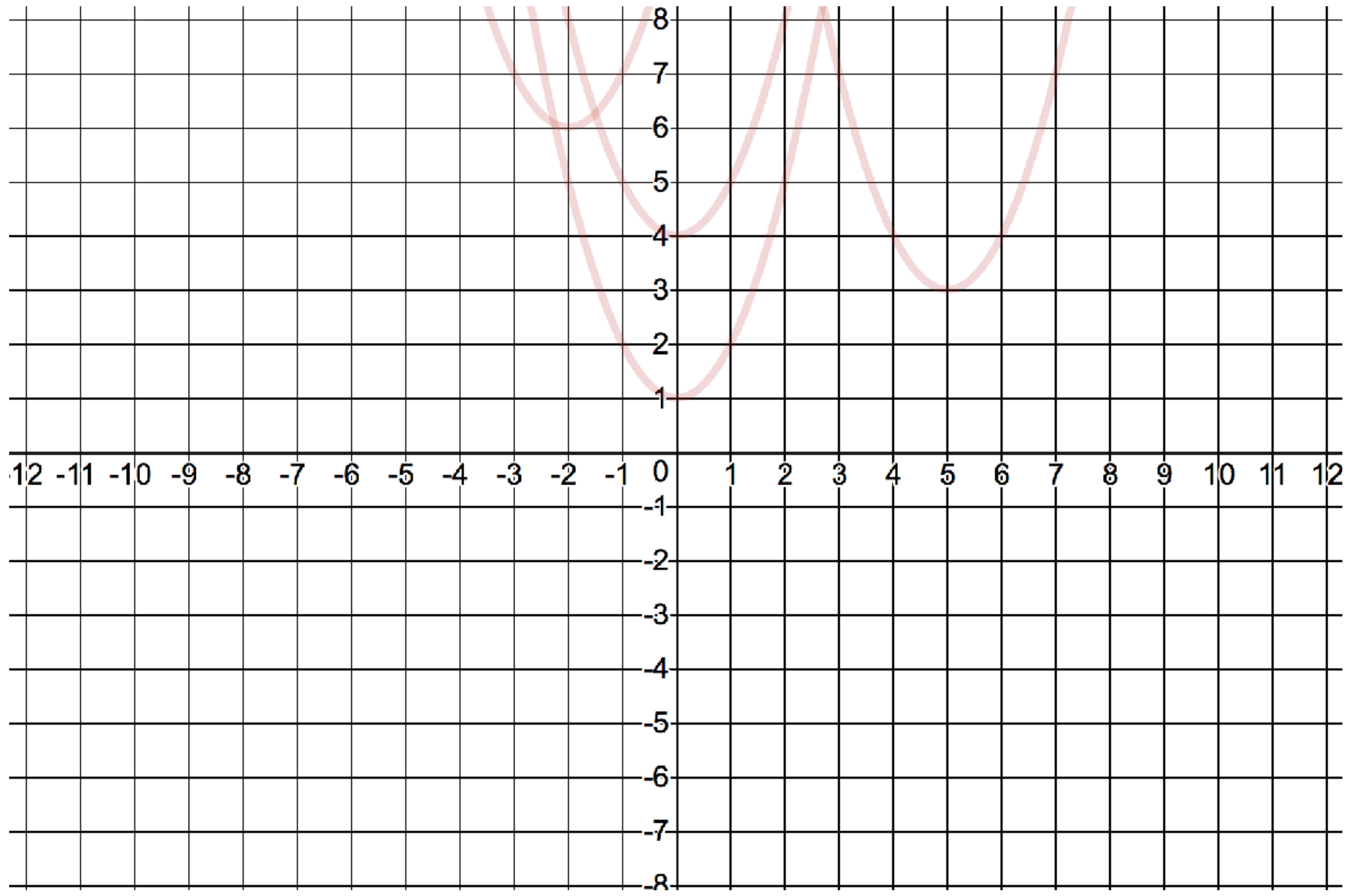
... OPENS UP



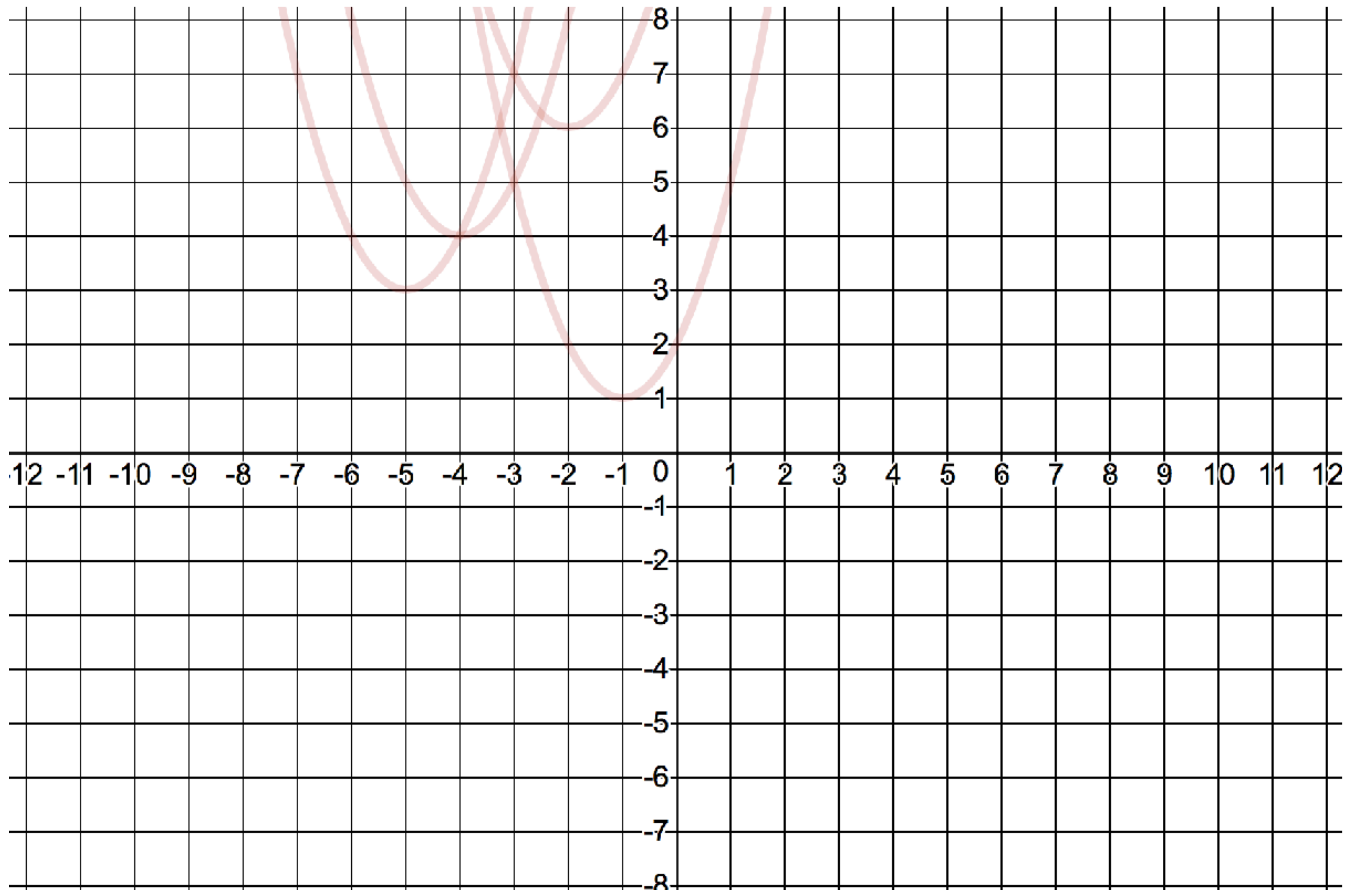
... POSITIVE Y-INTERCEPT



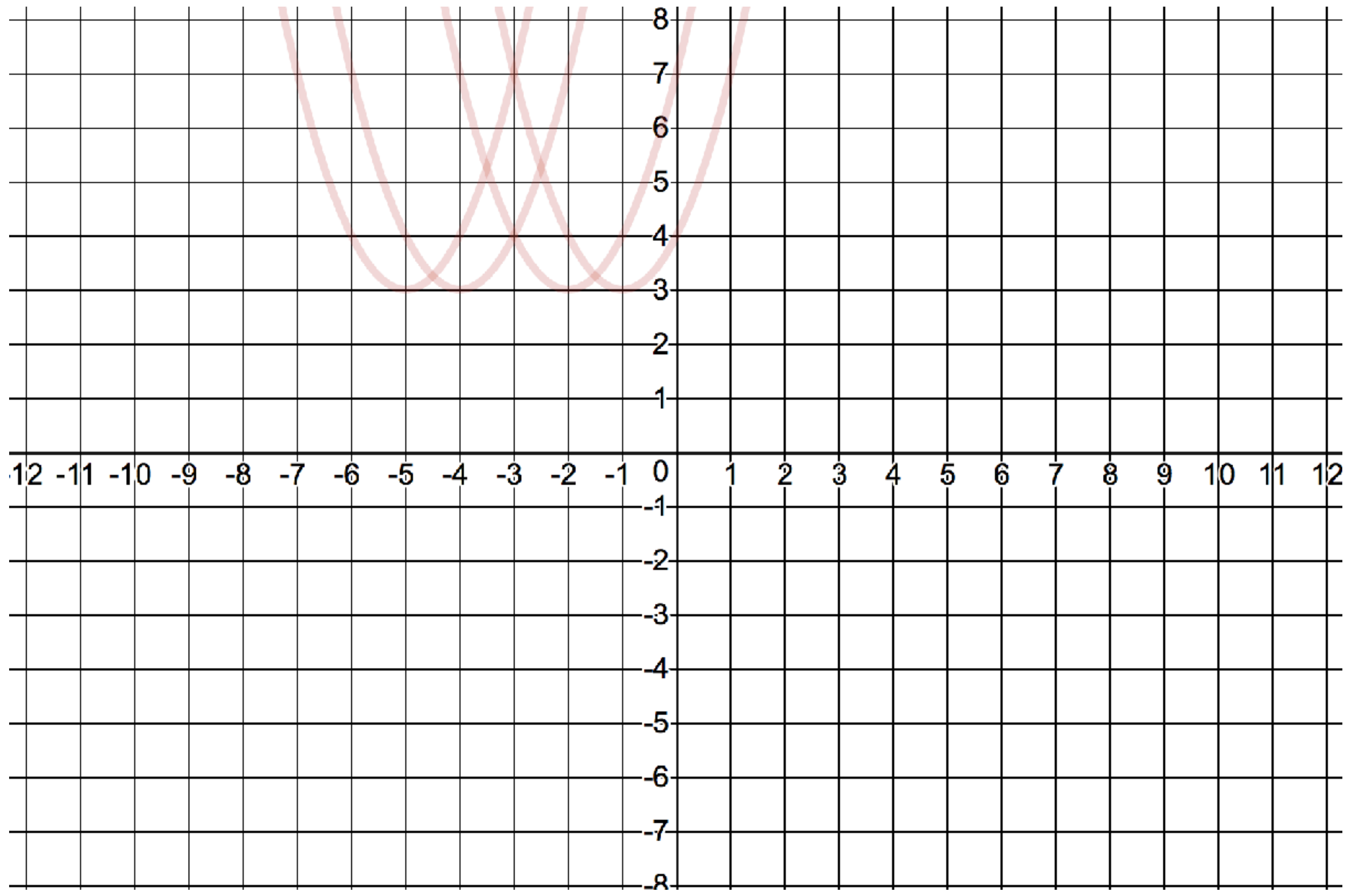
... NO X-INTERCEPTS



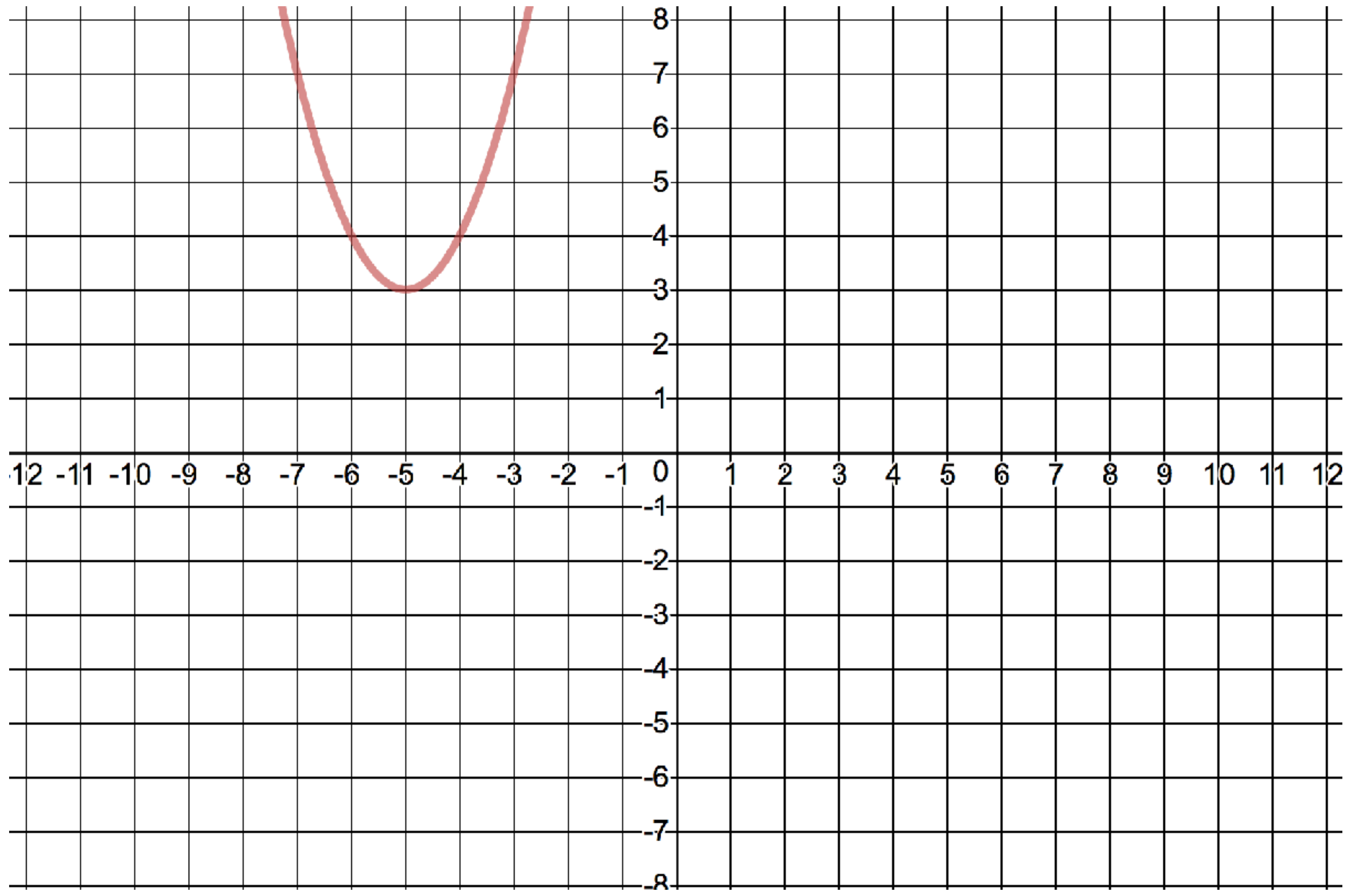
... NEVER ENTERS QIII



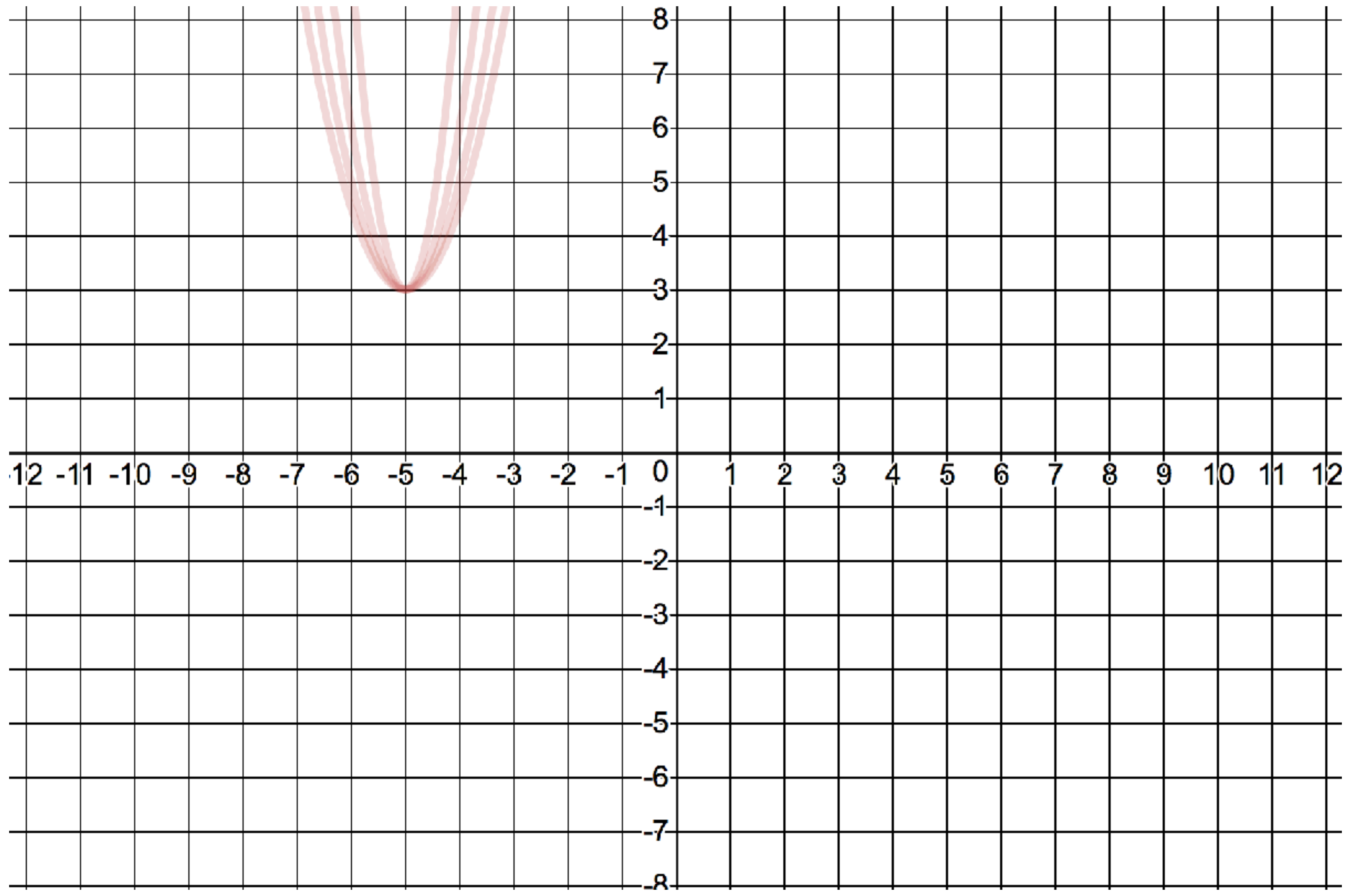
... VERTEX IN QII



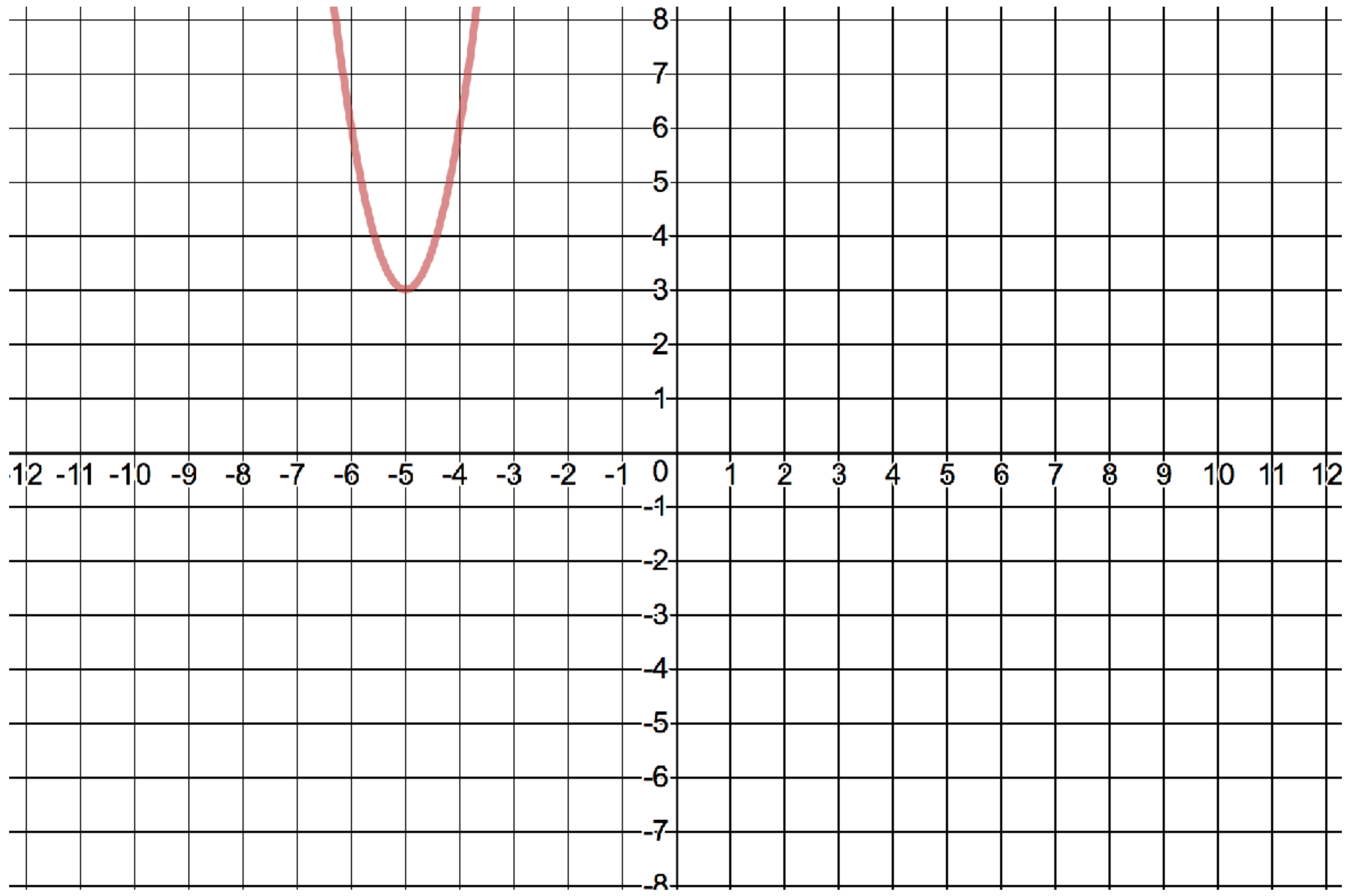
... MINIMUM VALUE OF 3



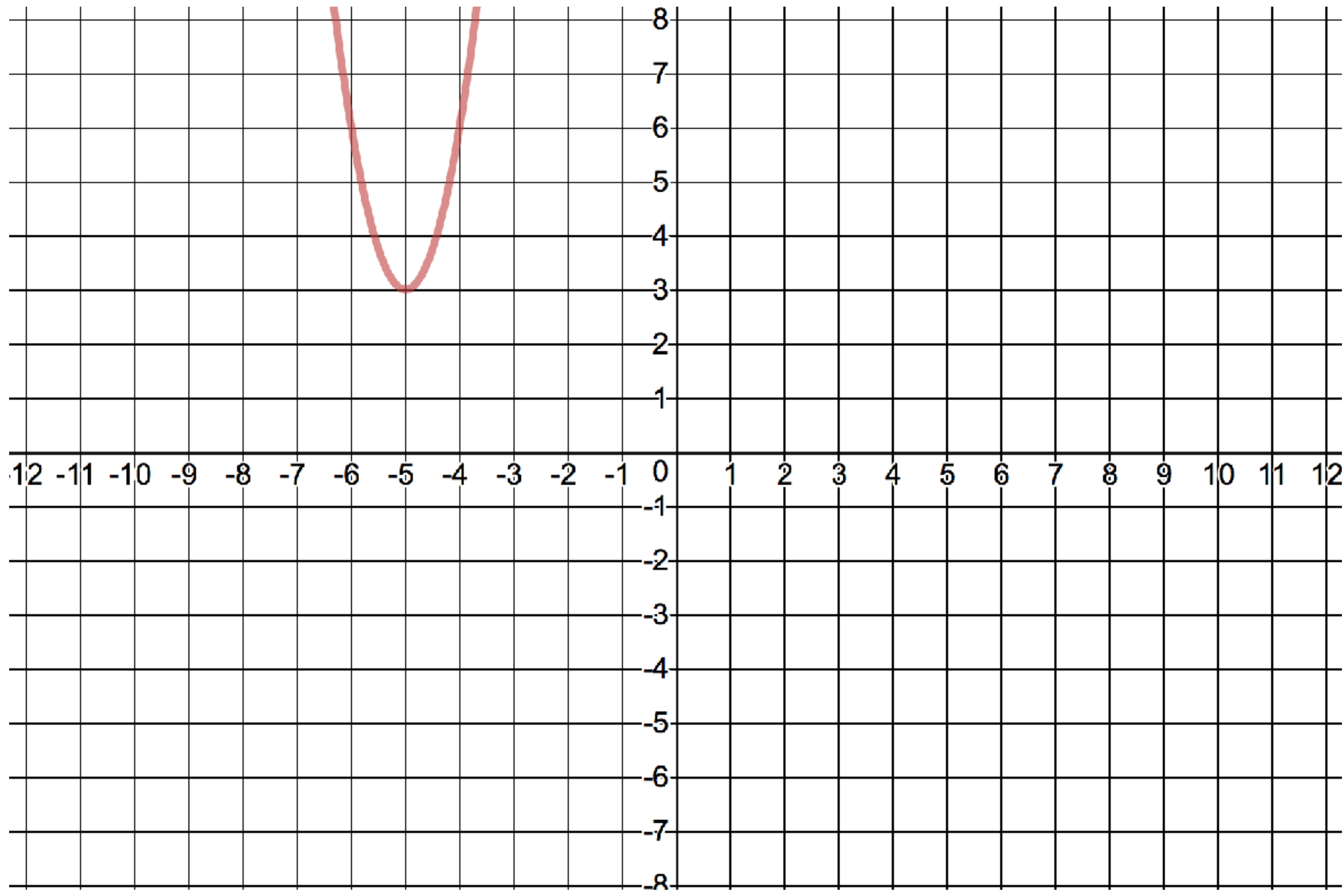
... AXIS OF SYMMETRY $x = -5$



... VERTICALLY STRETCHED



... PASSES THROUGH $(-7, 15)$



... VERTEX $(-5, 3)$

*Which clues were **helpful**?*

*Which clues were **necessary**?*

*What is the **fewest** number of clues you need?*

WANTED

QUADRATIC FUNCTION (A.K.A. “PARABOLA”)...

... TWO X-INTERCEPTS

... POSITIVE Y-INTERCEPT

... AXIS OF SYMMETRY $x = 2$

... VERTEX IN QI

... OPENS DOWN

... RANGE $y \leq 4$

... CONTAINS POINTS IN ALL FOUR QUADRANTS

... VERTEX $(2, 4)$

... PASSES THROUGH $(5, 1)$

... VERTICALLY SHRUNK

WANTED

QUADRATIC FUNCTION (A.K.A. “PARABOLA”)...

... PASSES THROUGH $(-2, 14)$

... POSITIVE Y-INTERCEPT

... DOES NOT CONTAIN POINTS IN QIII, QIV

... OPENS UP

... VERTEX IN QII

... AXIS OF SYMMETRY $x = -4$

... PASSES THROUGH $(-6, 14)$

... VERTICALLY STRETCHED

... VERTEX $(-4, 6)$

... PASSES THROUGH $(-3, 8)$

WANTED

LINEAR RELATION (A.K.A. “LINE”)...

... POSITIVE Y-INTERCEPT

... NEVER PASSES THROUGH QIII

... POSITIVE X-INTERCEPT

... PERPENDICULAR TO $Y = \frac{1}{2}X + 3$

... DECREASES FROM LEFT TO RIGHT

... SLOPE = -2

... X-INTERCEPT = 4

... HAS THE SAME Y-INTERCEPT AS $8X - 3Y + 24 = 0$

... PASSES THROUGH (1, 6)

A.	Has a positive slope	B.	Has a positive y -intercept
C.	Has a negative x -intercept	D.	Never enters Quadrant I
E.	Passes through (2, -3)	F.	Has a negative y -intercept
G.	Has a negative slope	H.	Passes through (4, 0)
I.	Never enters Quadrant III	J.	Has a slope less than 1

A.	Two negative x -intercepts	B.	Vertex in Quadrant II
C.	Never enters Quadrant III	D.	Vertex on the y -axis
E.	Positive y -intercept	F.	No x -intercepts
G.	Never enters Quadrant I	H.	Has a minimum value
I.	Horizontally stretched	J.	Line of symmetry enters Quadrant IV

*Which constraints **pair nicely**?*

*Which constraints **cannot be paired?***



**Combinations &
Transformations**

*In which ways can new functions
be derived from existing ones?*

Functions

On the grid are eight points from two different functions.

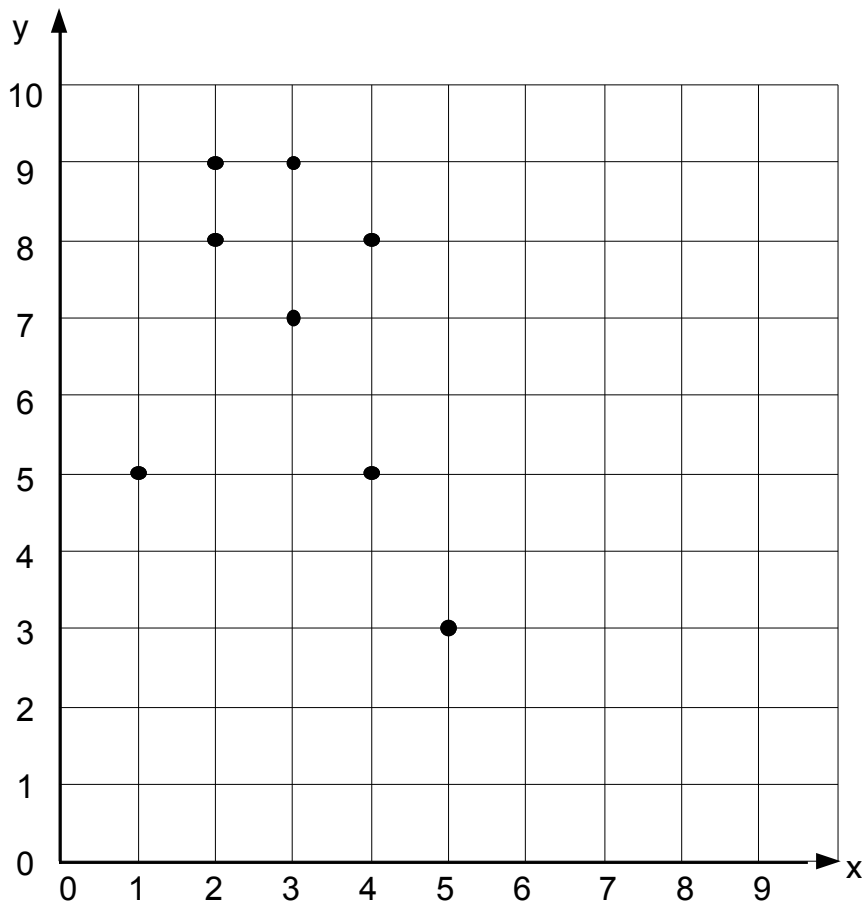
A certain linear function passes through exactly four of the points shown.

A certain quadratic function passes through the remaining four points.

For the **linear** function:

1. Write the coordinate pairs of its four points.

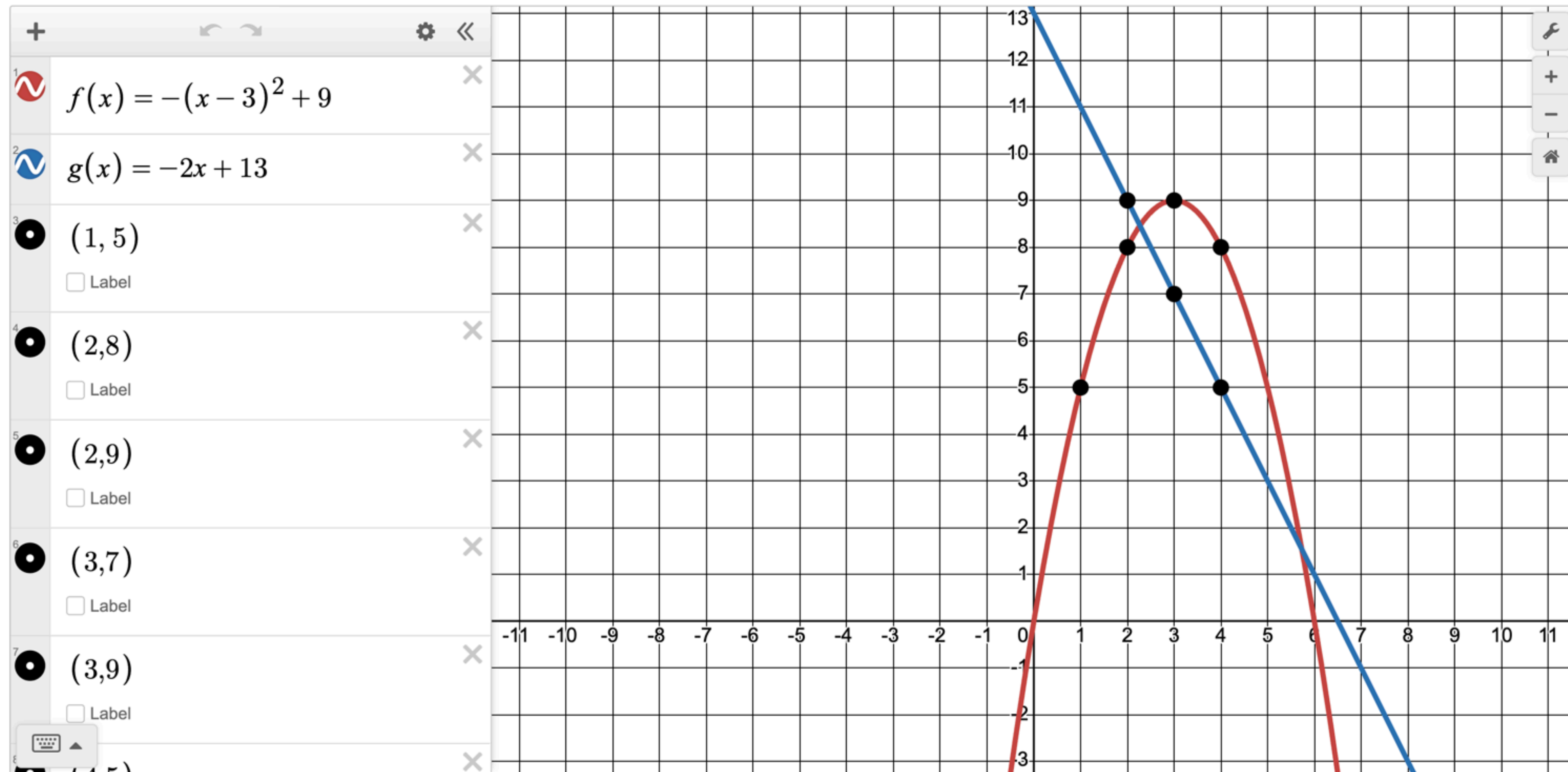
Draw the line on the grid.



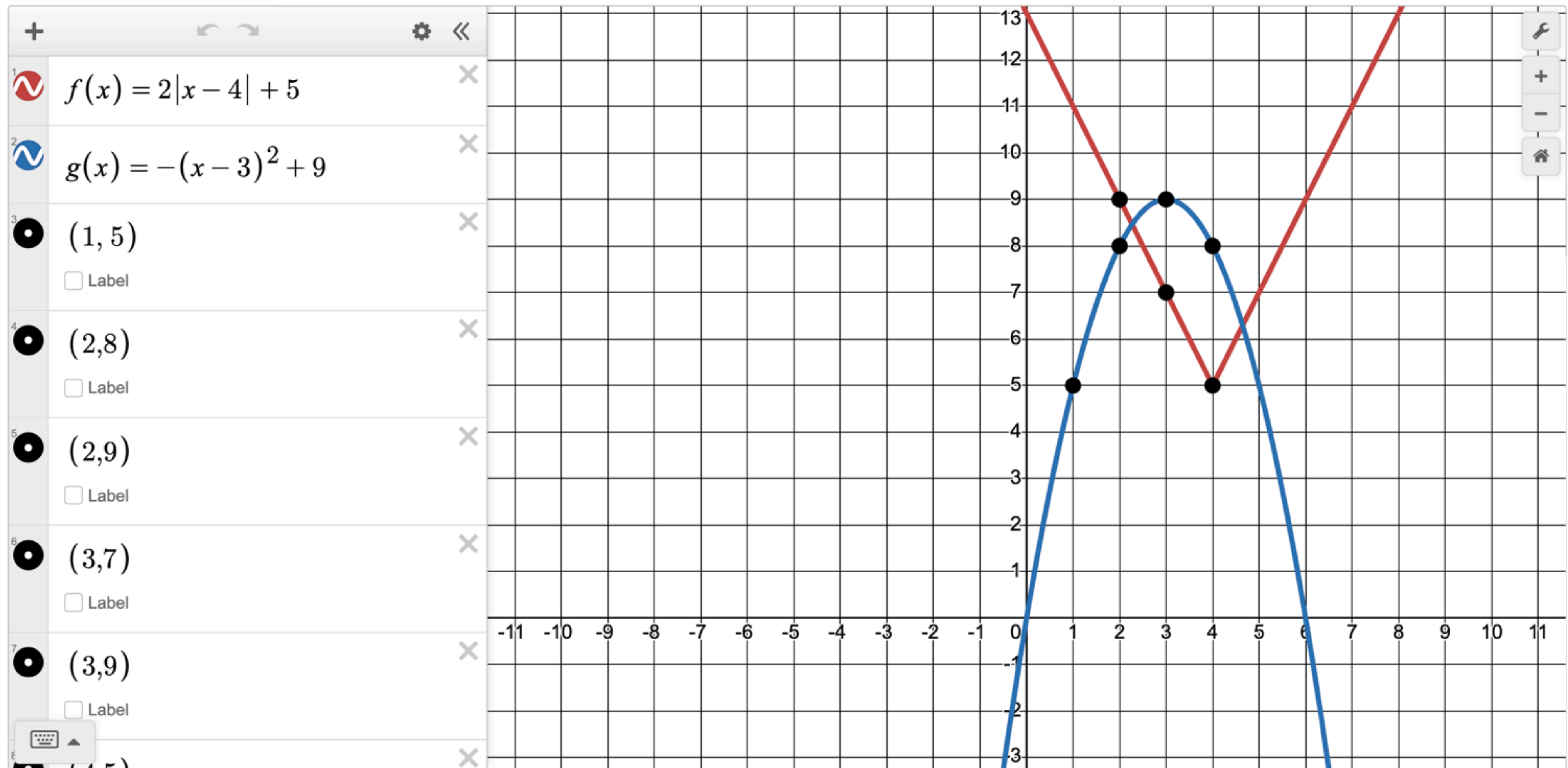
2. Write an equation for the function.

Show your work.

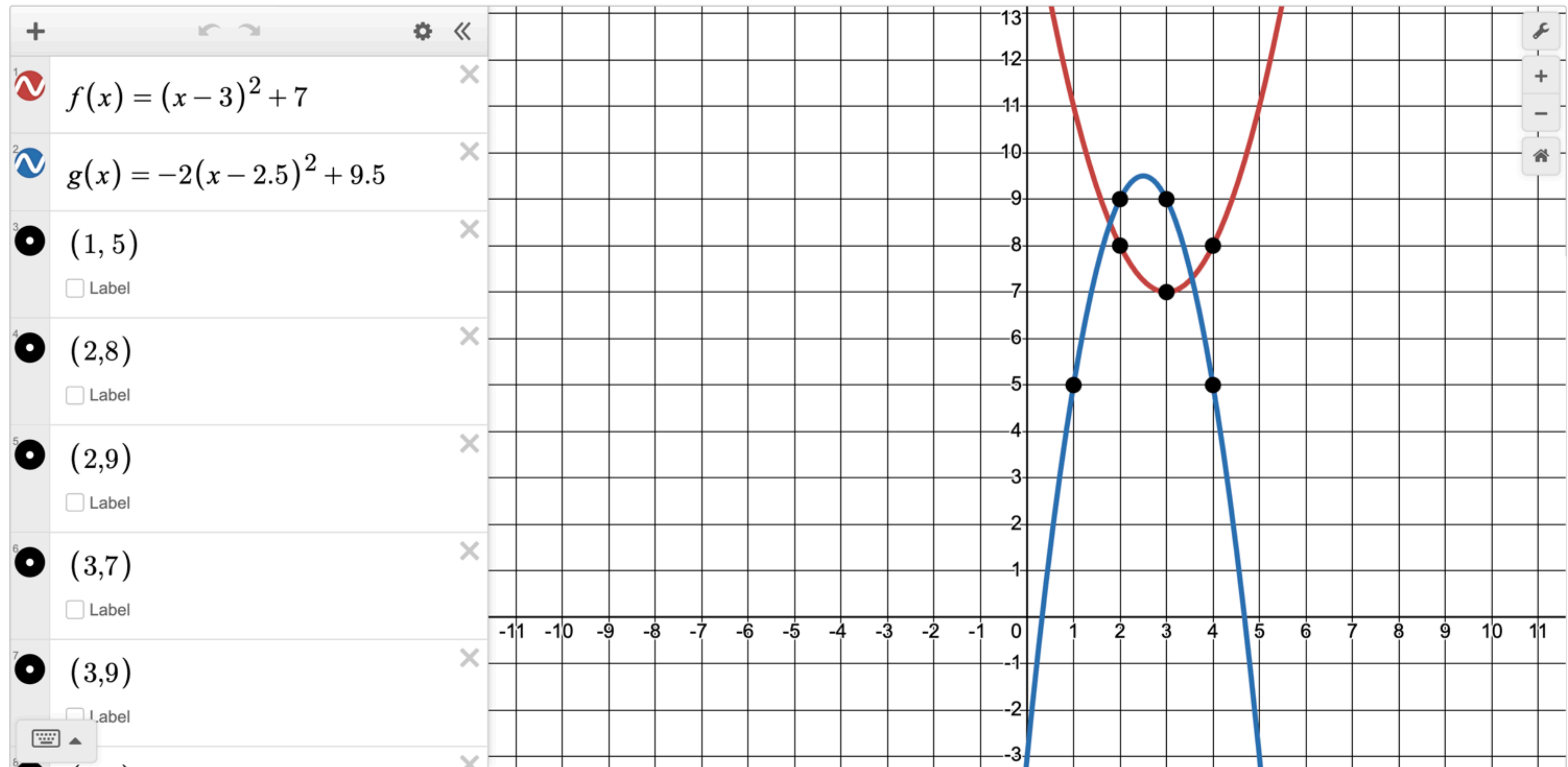
A set of functions pass through the points shown. What could the equations for the functions be?



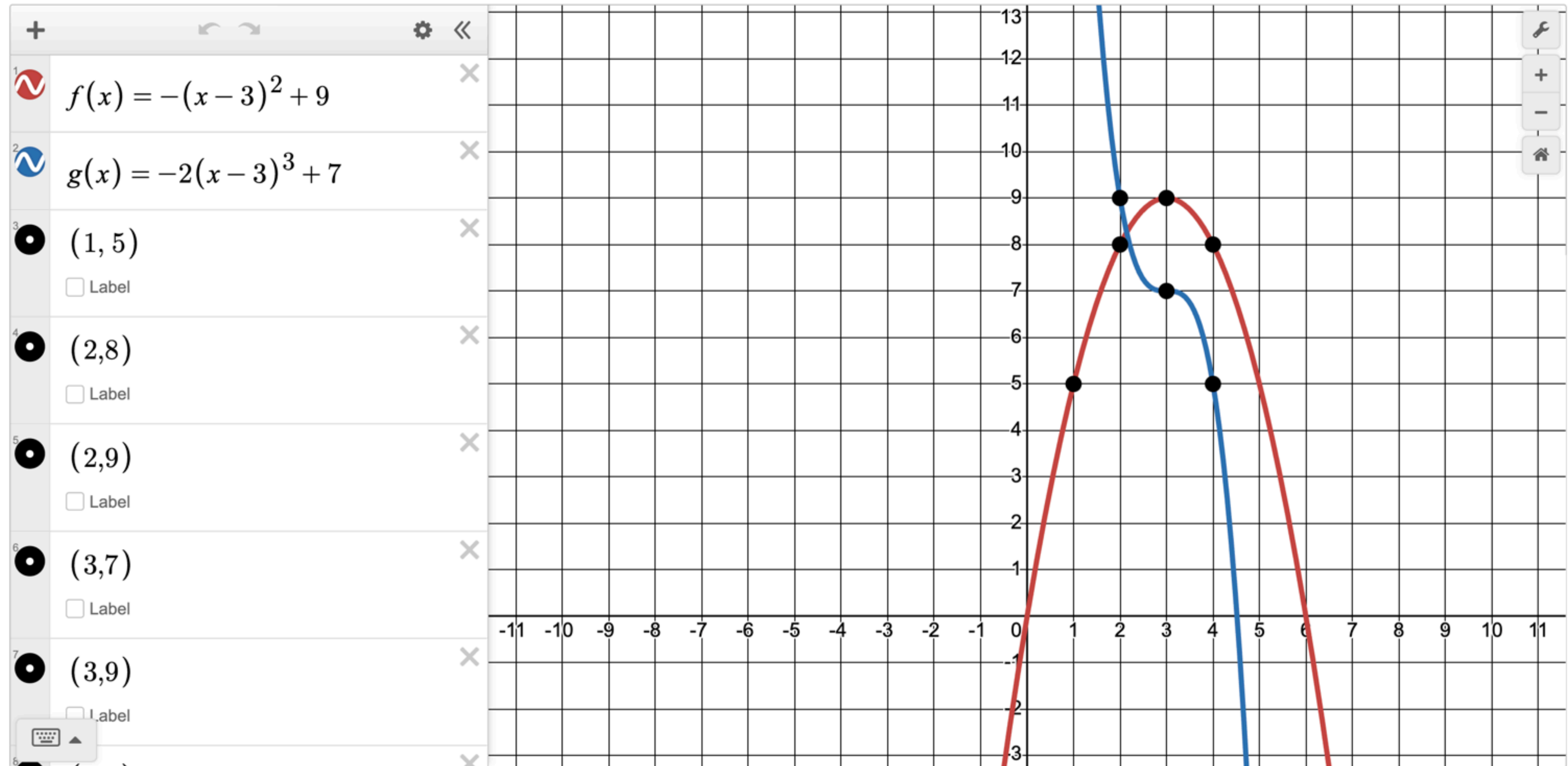
A set of functions pass through the points shown. What could the equations for the functions be?



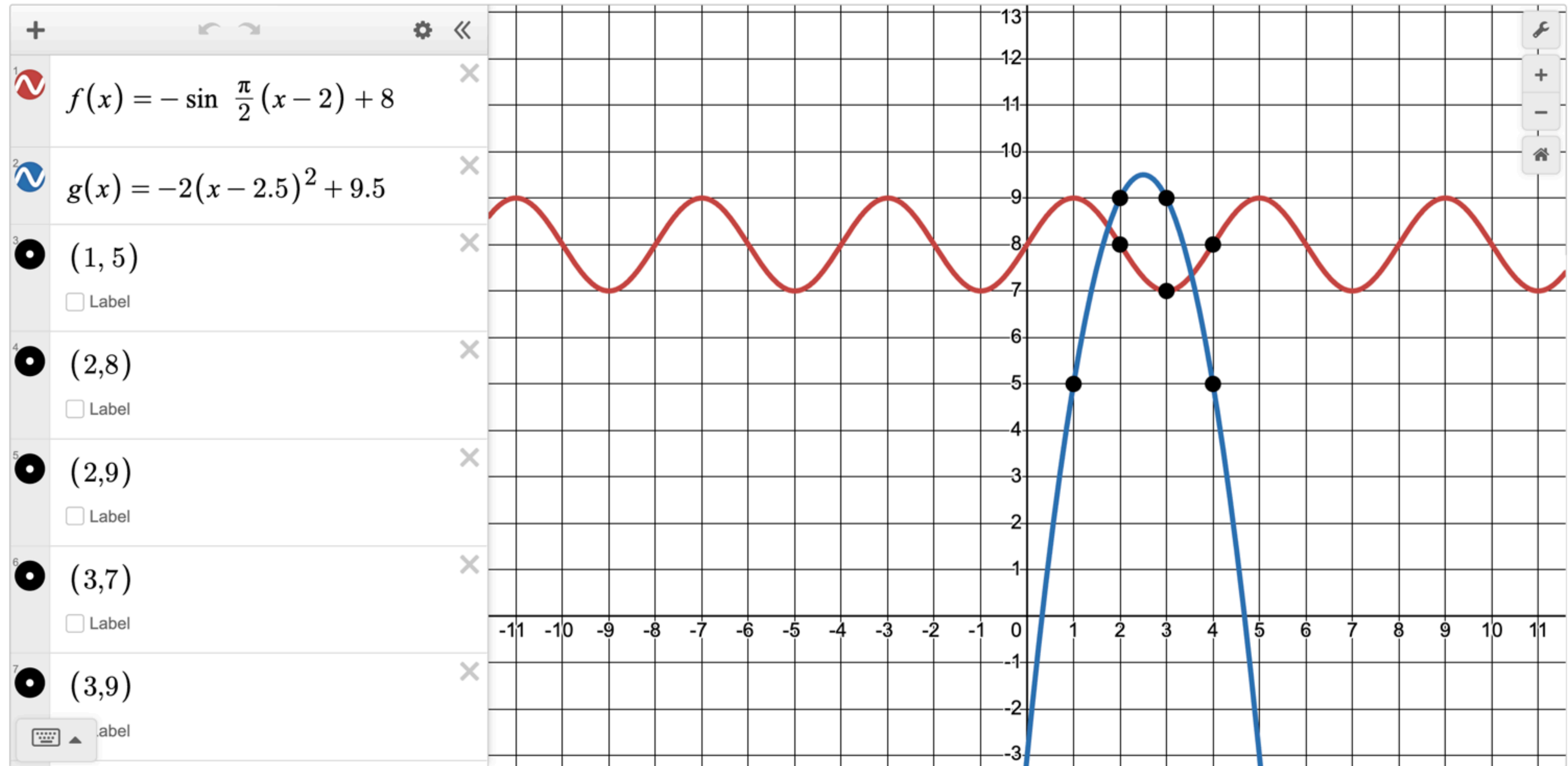
A set of functions pass through the points shown. What could the equations for the functions be?



A set of functions pass through the points shown. What could the equations for the functions be?



A set of functions pass through the points shown. What could the equations for the functions be?



$$y = 4x + 7$$

Translate
three units
down

Reflect in the
 y -axis

Translate two
units to the
left

Reflect in the
 x -axis

$$y = 4x - 2$$

$$y = 4x + 7$$

Reflect in the
 y -axis

Reflect in the
 x -axis

Translate
three units
down

Translate two
units to the
left

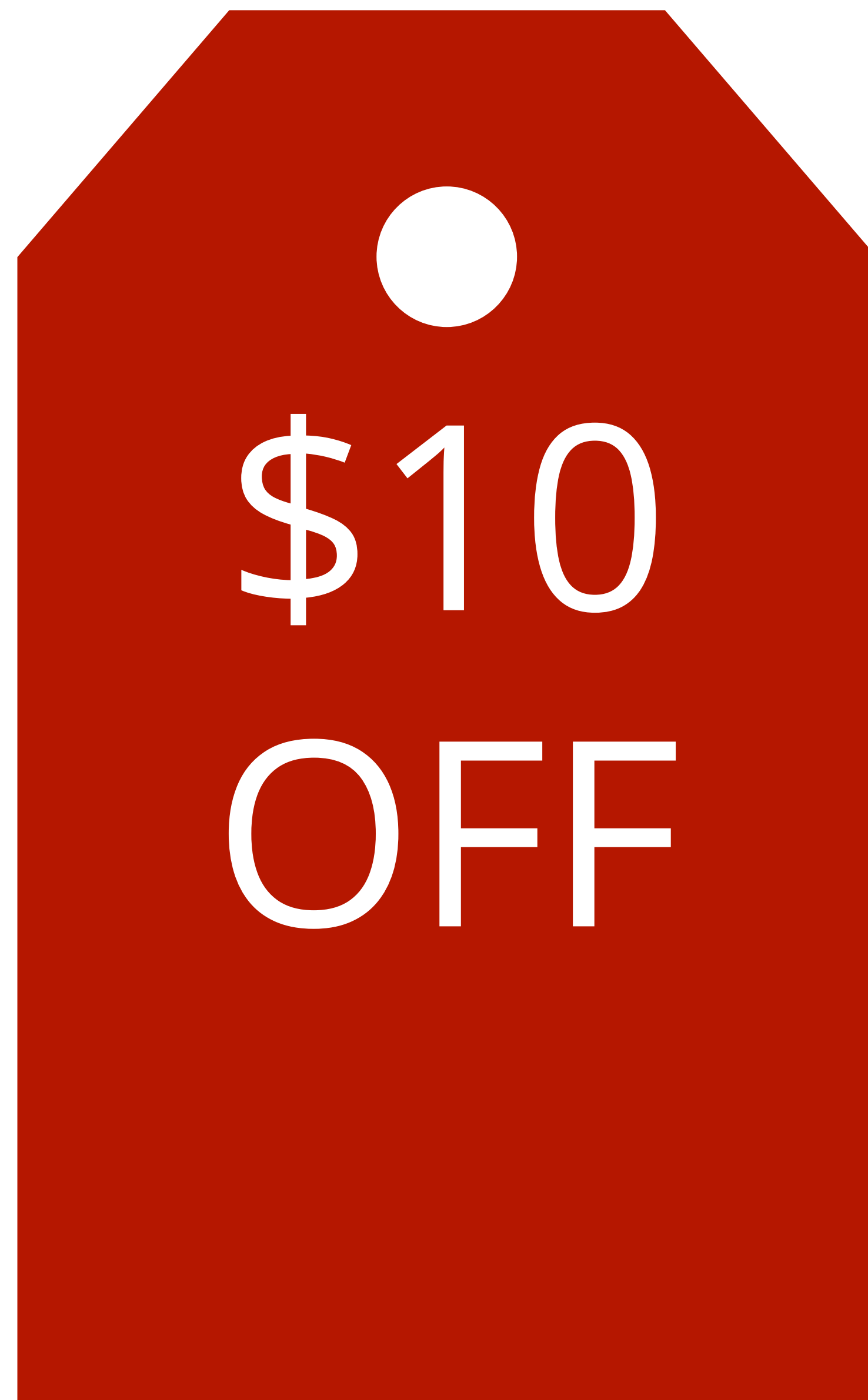
$$y = 4x - 2$$

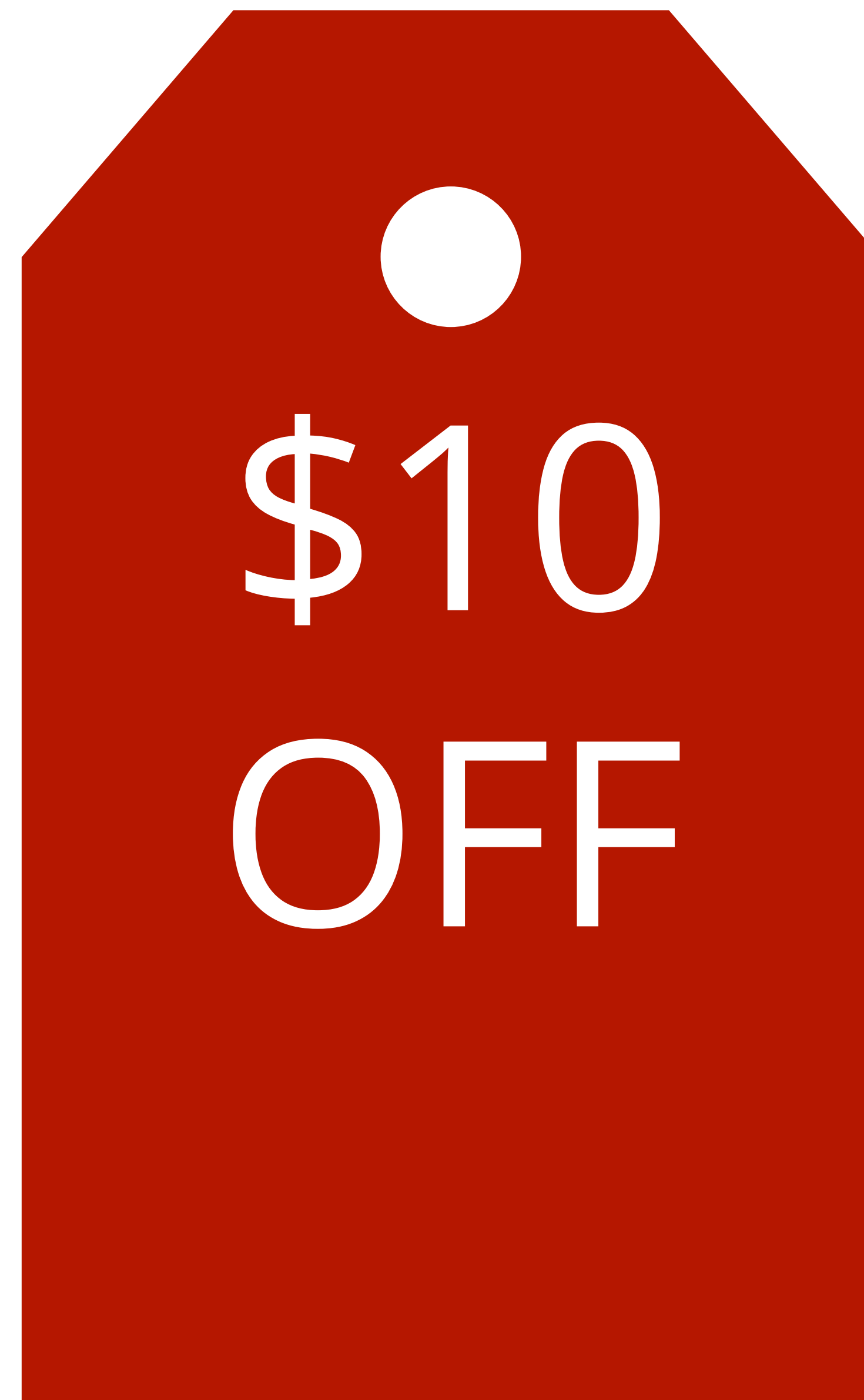
There is more than one way of doing this - can you find them all?

Can you explain why different orders can lead to the same outcome?

What other lines could I have ended up with if I had performed the four transformations in a different order?

Would you rather...





Polypad
Composition Coupons
Save
⋮
🔗
?

Tiles
⚙️
📁
?

🔗 Geometry

123 Numbers

1/2 Fractions

x² Algebra

Algebra Tiles

Balance Scale

Function Machines

1

2

3

4

5

6

7

8

10

10

Coordinate Axes and Tables

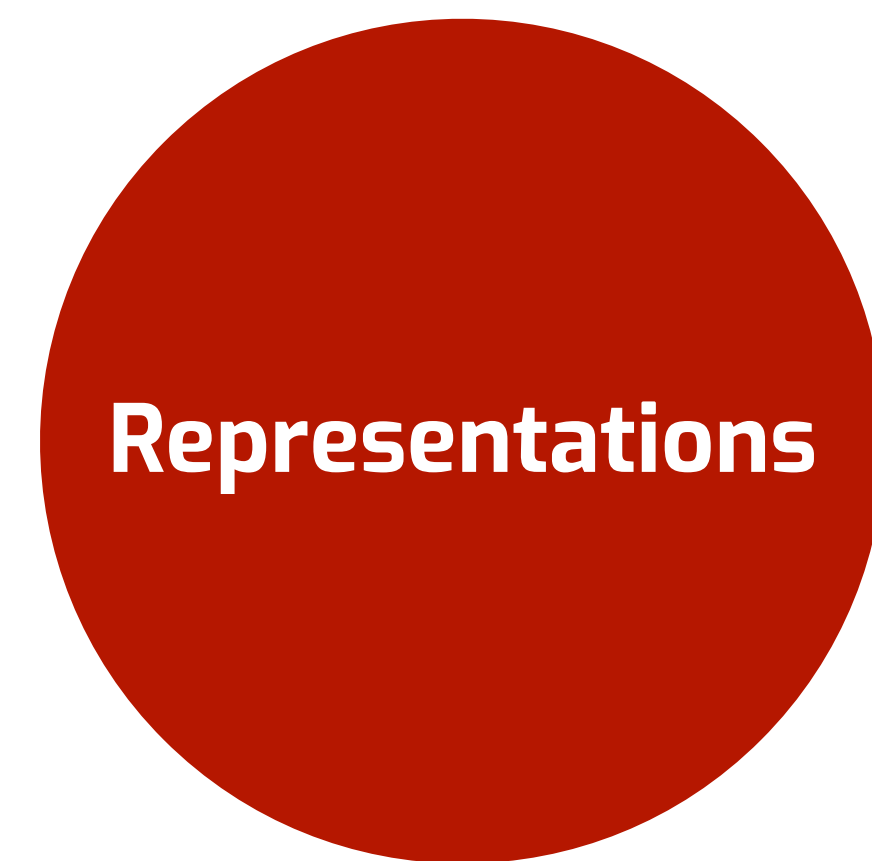
Variable Sliders

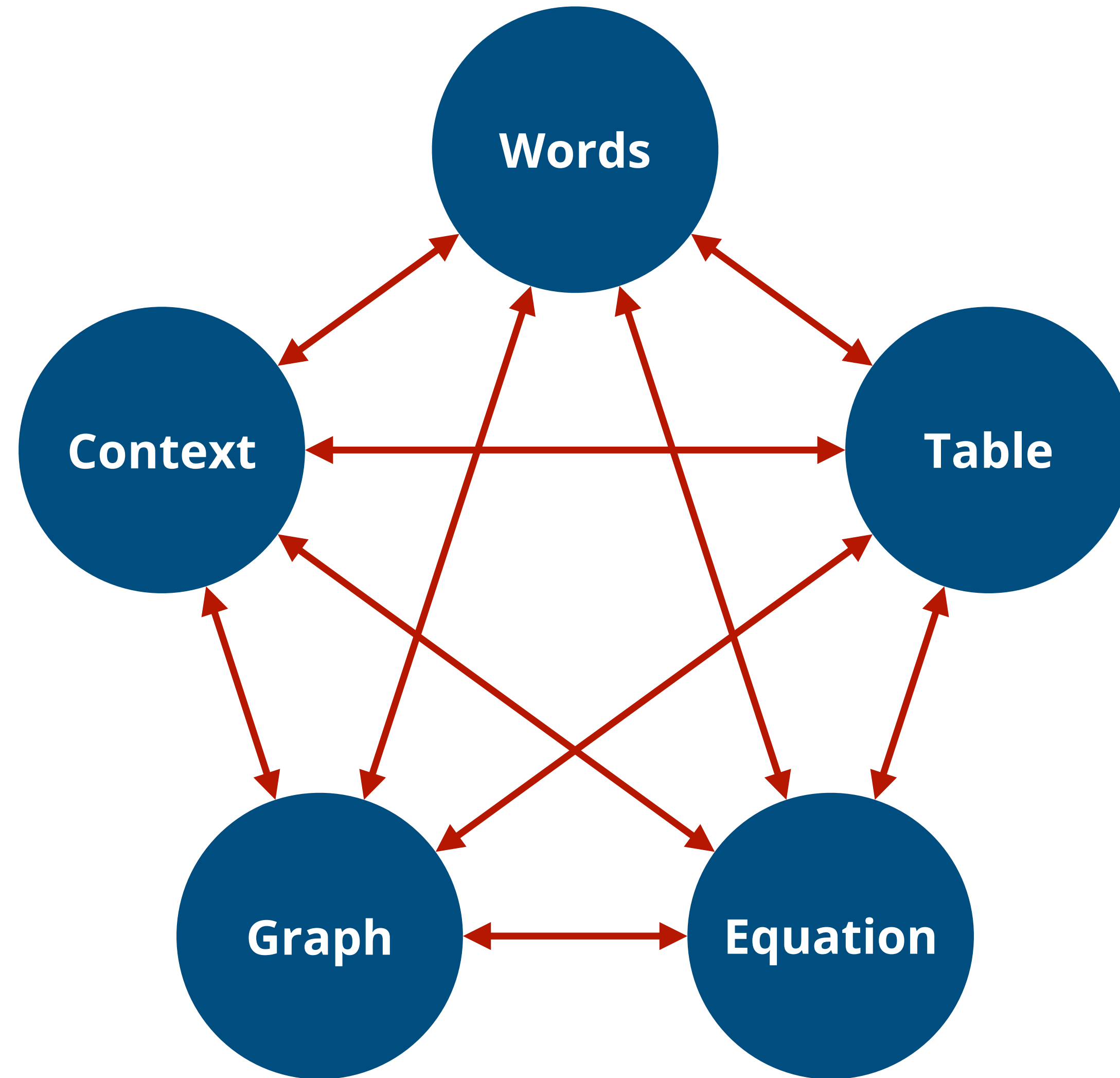
📊 Probability and Data

💡 Games and Applications

🔍
 🔍
 🔄

🖱️
🖋️
🔗
📝
x²
📷
🌈





*How do these characteristics appear
in tables, graphs, and equations?*

A

$$y = 2 \sin x$$

B

$$y = 3 \cos \frac{1}{2}(x + 90^\circ) - 1$$

C

$$y = \cos x + 2$$

D

$$y = -2 \cos 3(x - 60^\circ)$$

E

$$y = \frac{1}{2} \sin(x + 60^\circ)$$

F

$$y = \cos 2x - 3$$

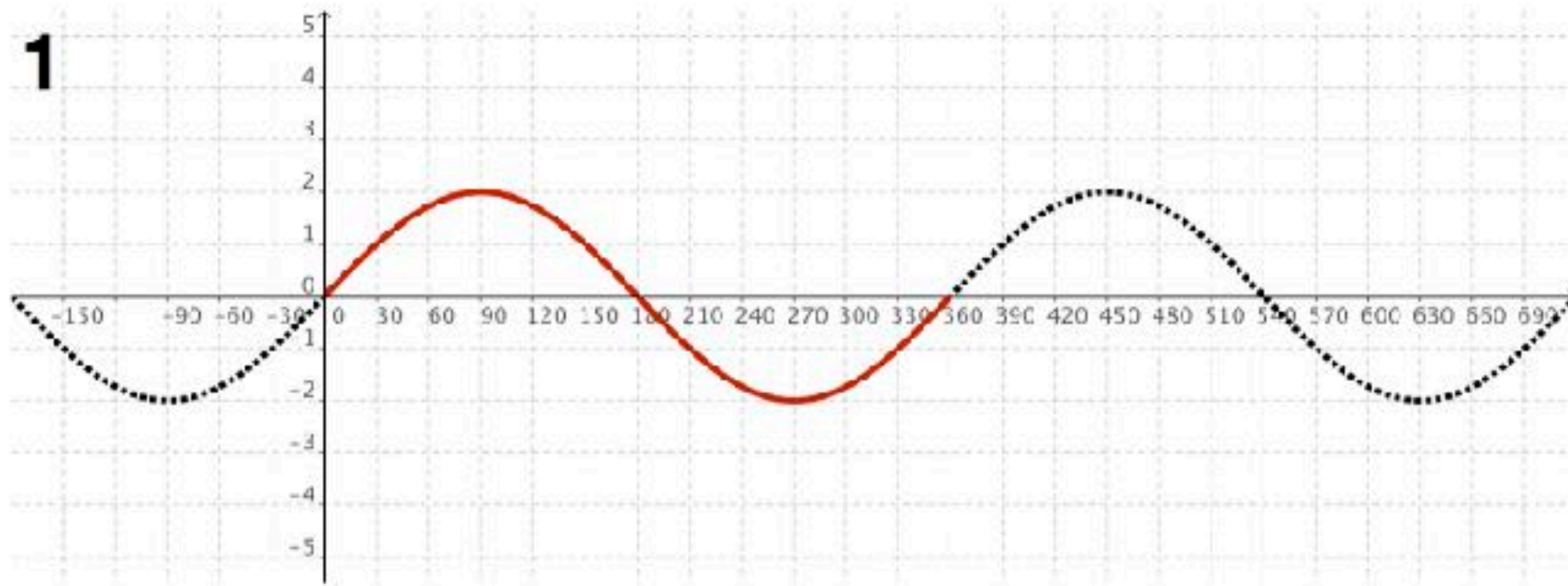
G

$$y = -3 \sin 2x$$

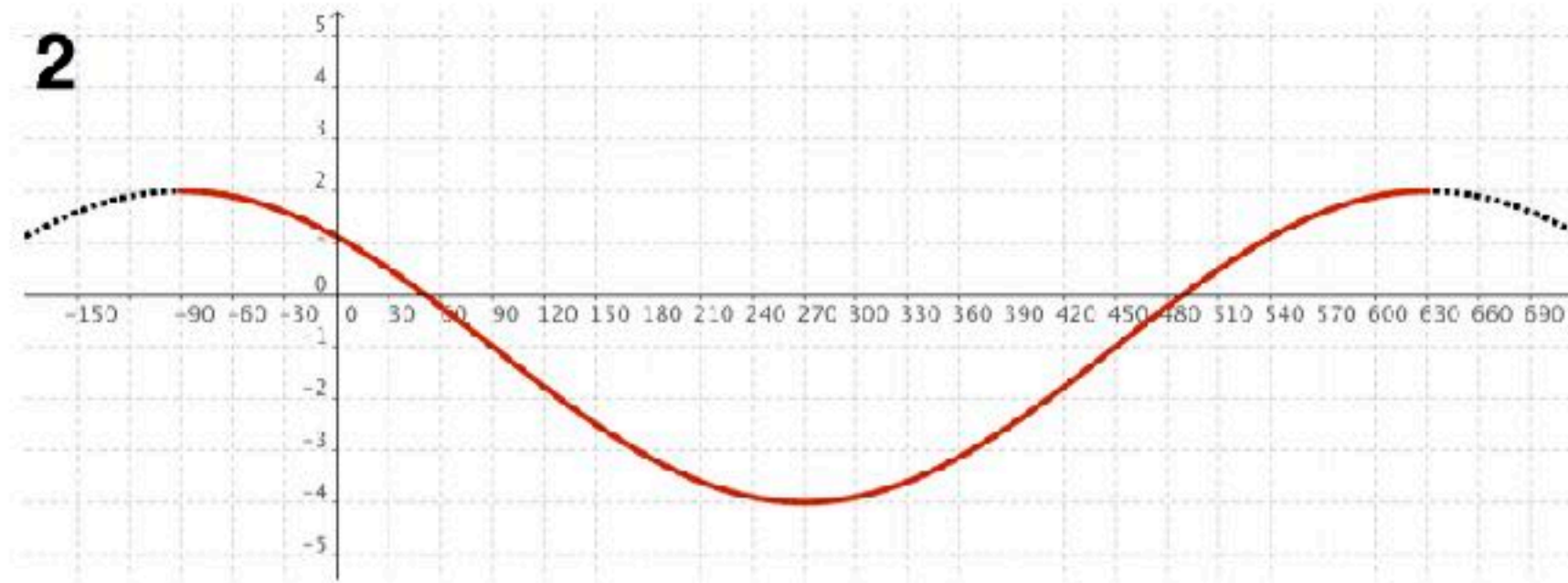
H

$$y = \sin 3(x - 90^\circ) + 1$$

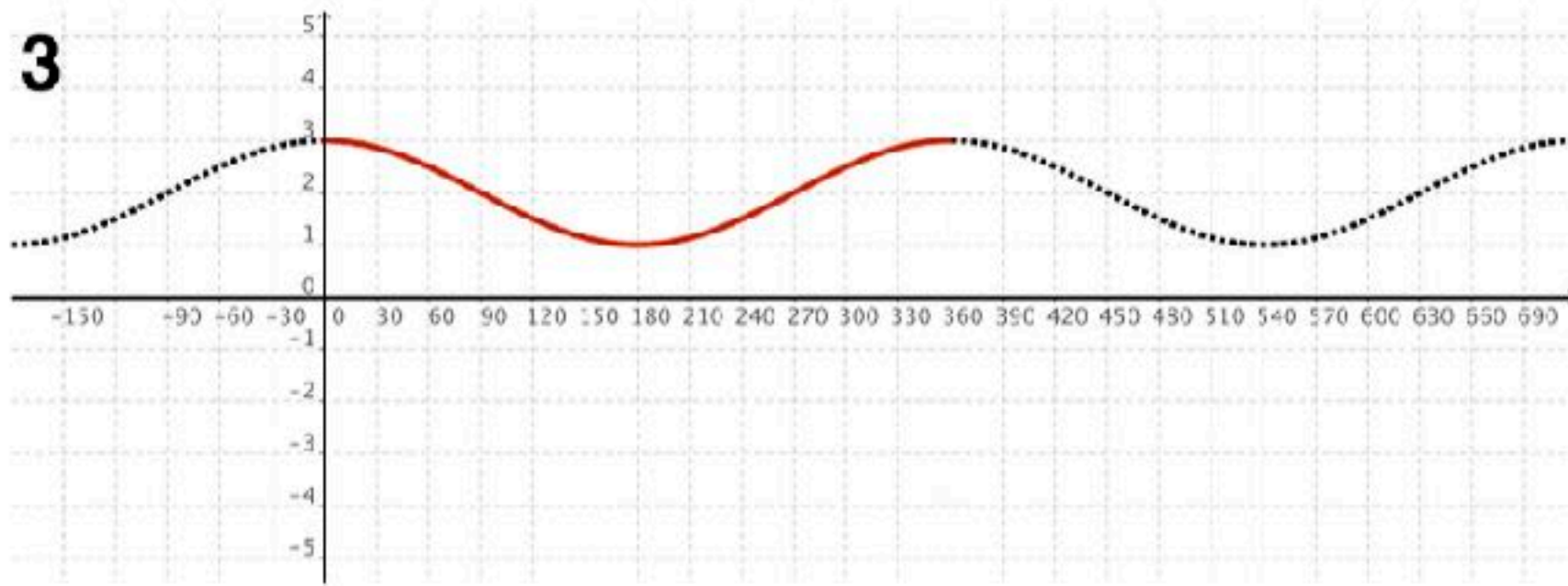
1



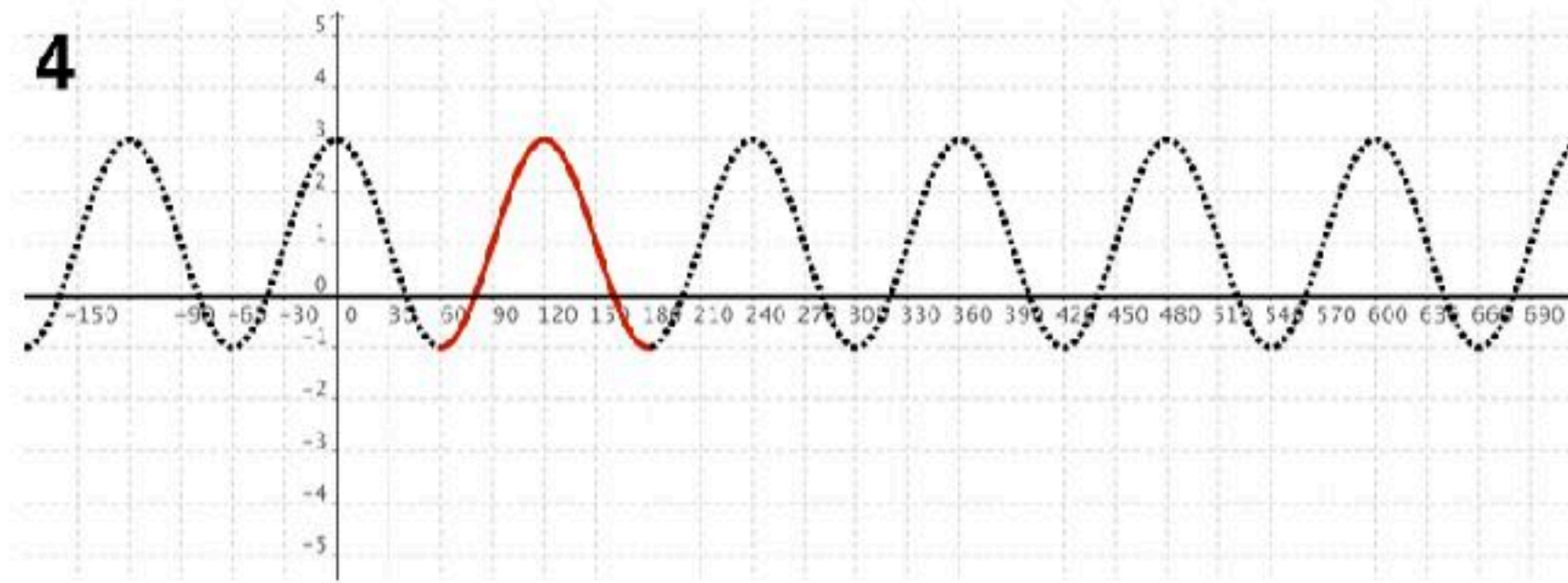
2



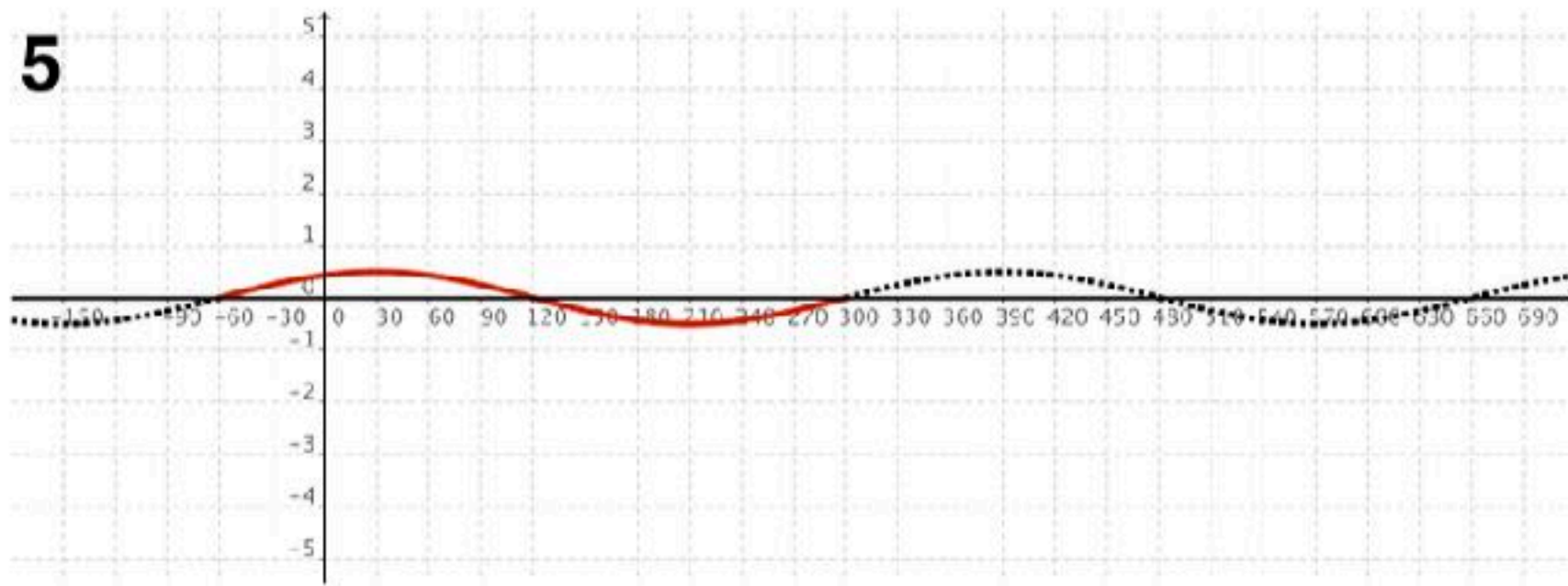
3



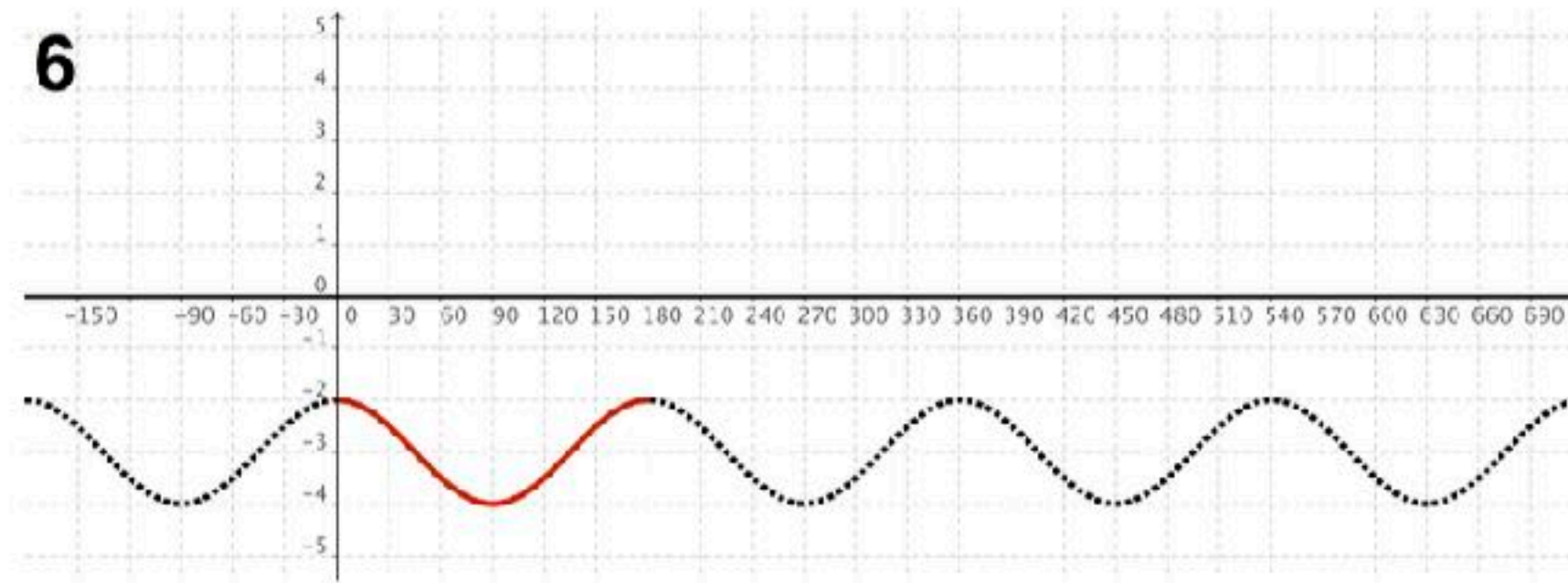
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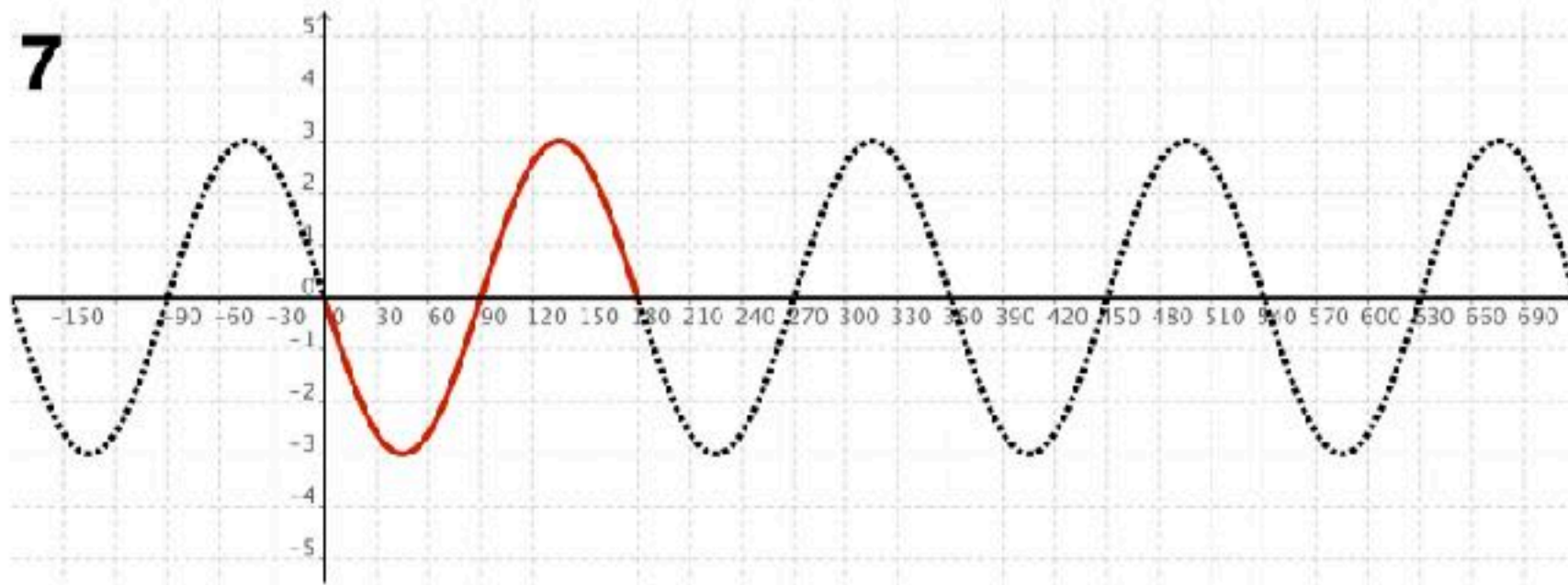
5



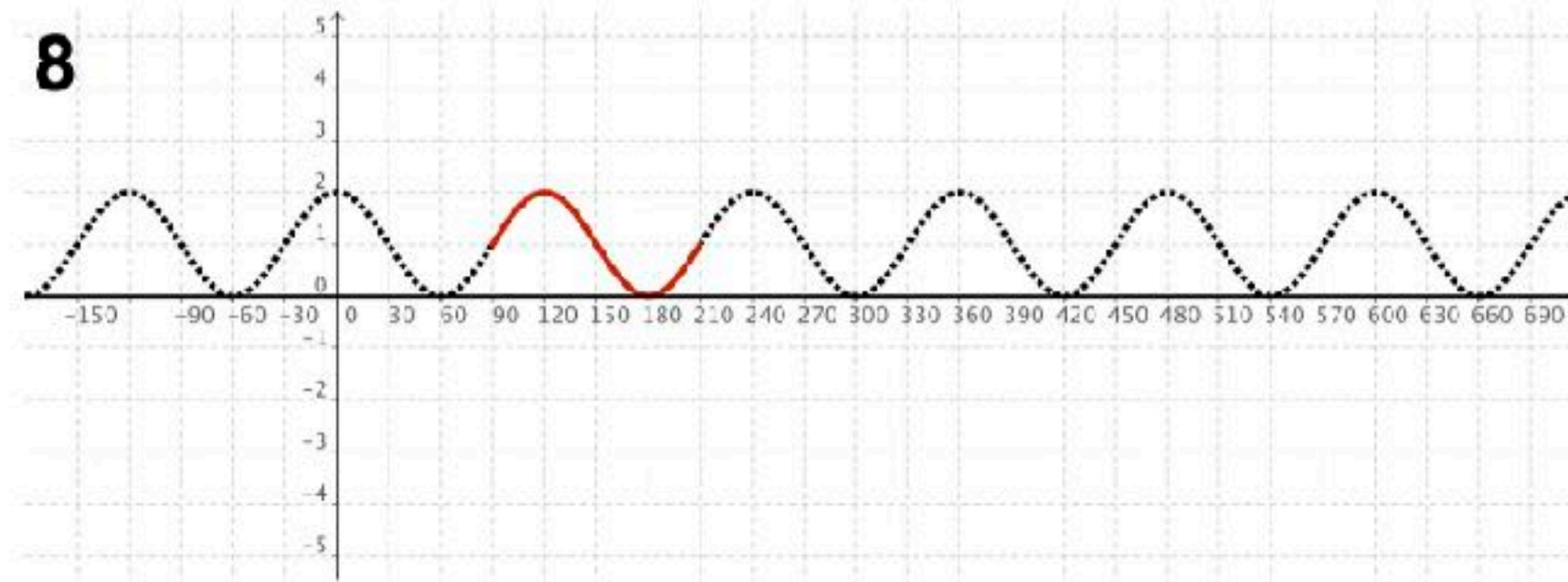
6



7



8



i	amplitude: 1 period: 360° maximum: 3 minimum: 1 range: $1 \leq y \leq 3$ vertical translation: up 2	ii	amplitude: 1 period: 180° maximum: -2 minimum: -4 range: $-4 \leq y \leq -2$ vertical translation: down 3
iii	amplitude: $\frac{1}{2}$ period: 360° maximum: $\frac{1}{2}$ minimum: $-\frac{1}{2}$ range: $-\frac{1}{2} \leq y \leq \frac{1}{2}$ horizontal translation: left 60°	iv	amplitude: 3 period: 180° maximum: 3 minimum: -3 range: $-3 \leq y \leq 3$ reflection: x-axis
v	amplitude: 3 period: 720° maximum: 2 minimum: -4 range: $-4 \leq y \leq 2$ horizontal translation: left 90° vertical translation: down 1	vi	amplitude: 2 period: 120° maximum: 2 minimum: -2 range: $-2 \leq y \leq 2$ horizontal translation: right 60° reflection: x-axis
vii	amplitude: 1 period: 120° maximum: 2 minimum: 0 range: $0 \leq y \leq 2$ horizontal translation: right 90° vertical translation: up 1	viii	amplitude: 2 period: 360° maximum: 2 minimum: -2 range: $-2 \leq y \leq 2$

“Admittedly, there’s little cognitive difference between a tactile matching activity and a matching exercise on a worksheet. However, **in a card sort, the emphasis rests on the conversation among students** rather than the conversation between the student and the worksheet. **Because students can arrange and rearrange shapes or cards on the table, they naturally refine and test ideas, and talk about them.** In this way, card sorts can reinforce our message that mistakes are learning opportunities.”

Krall, G. (2018). *Necessary conditions: Teaching secondary math with academic safety, quality tasks, and effective facilitation*. Stenhouse.

Open Middle

$$f(x) = (x - \square) (x - \square)$$

$$f(x) = (x - \square)^2 - \square$$

1

2

3

4

5

6

7

8

9

$$f(x) = (x - \square) (x - \square)$$

$$f(x) = (x - \square)^2 - \square$$

$$f(x) = x^2 - \square x + \square$$

1

2

3

4

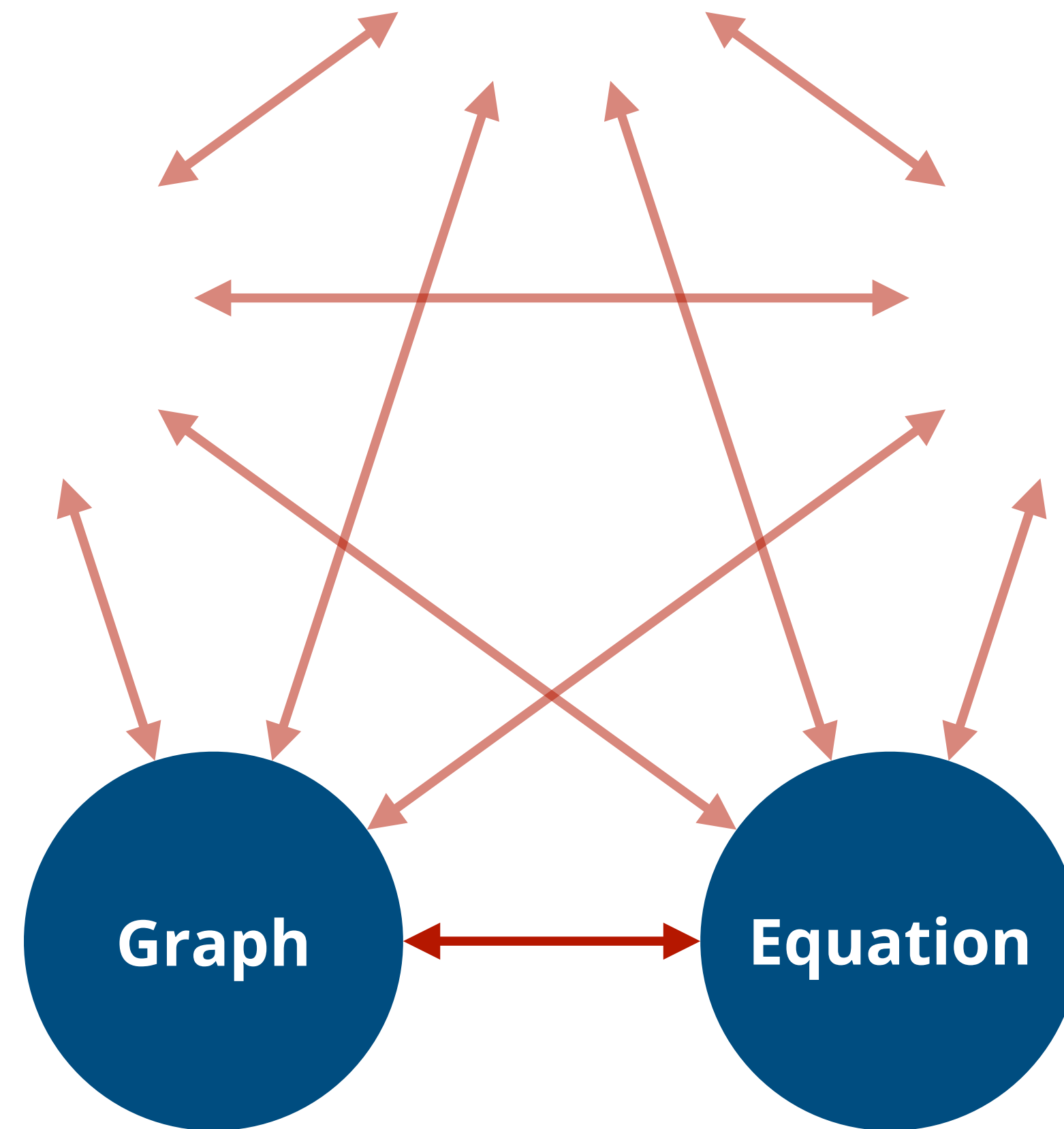
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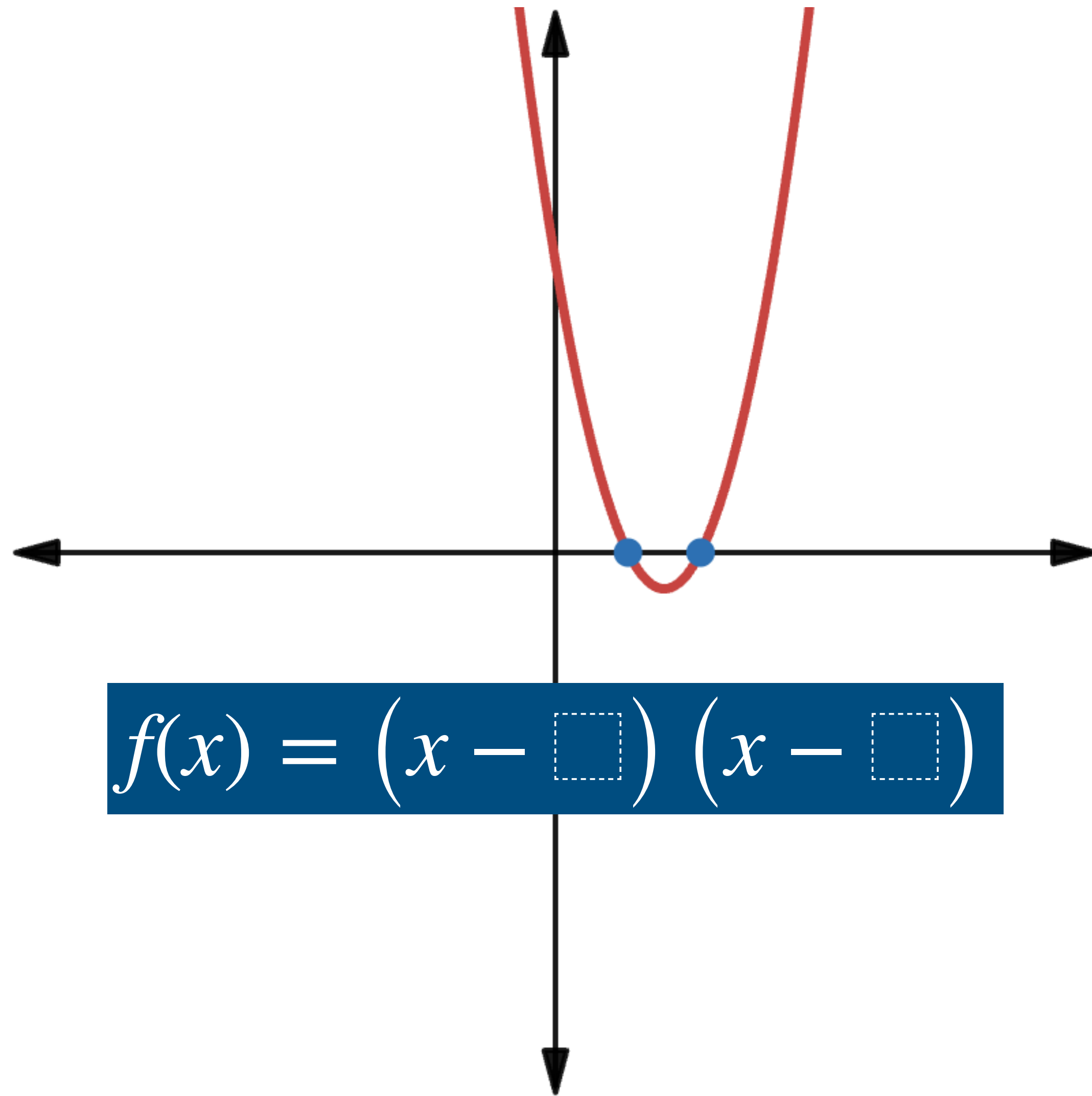
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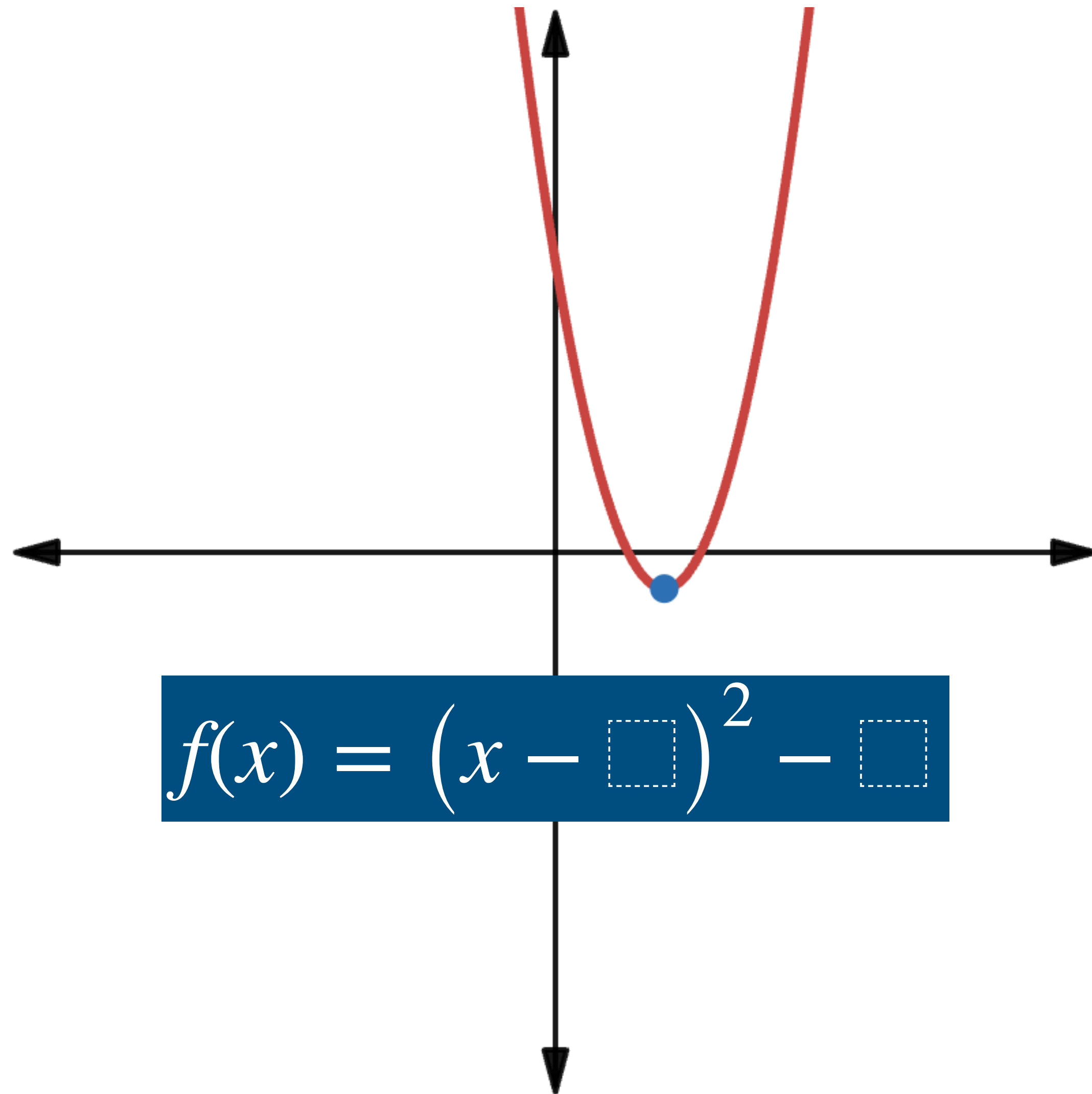
7

8

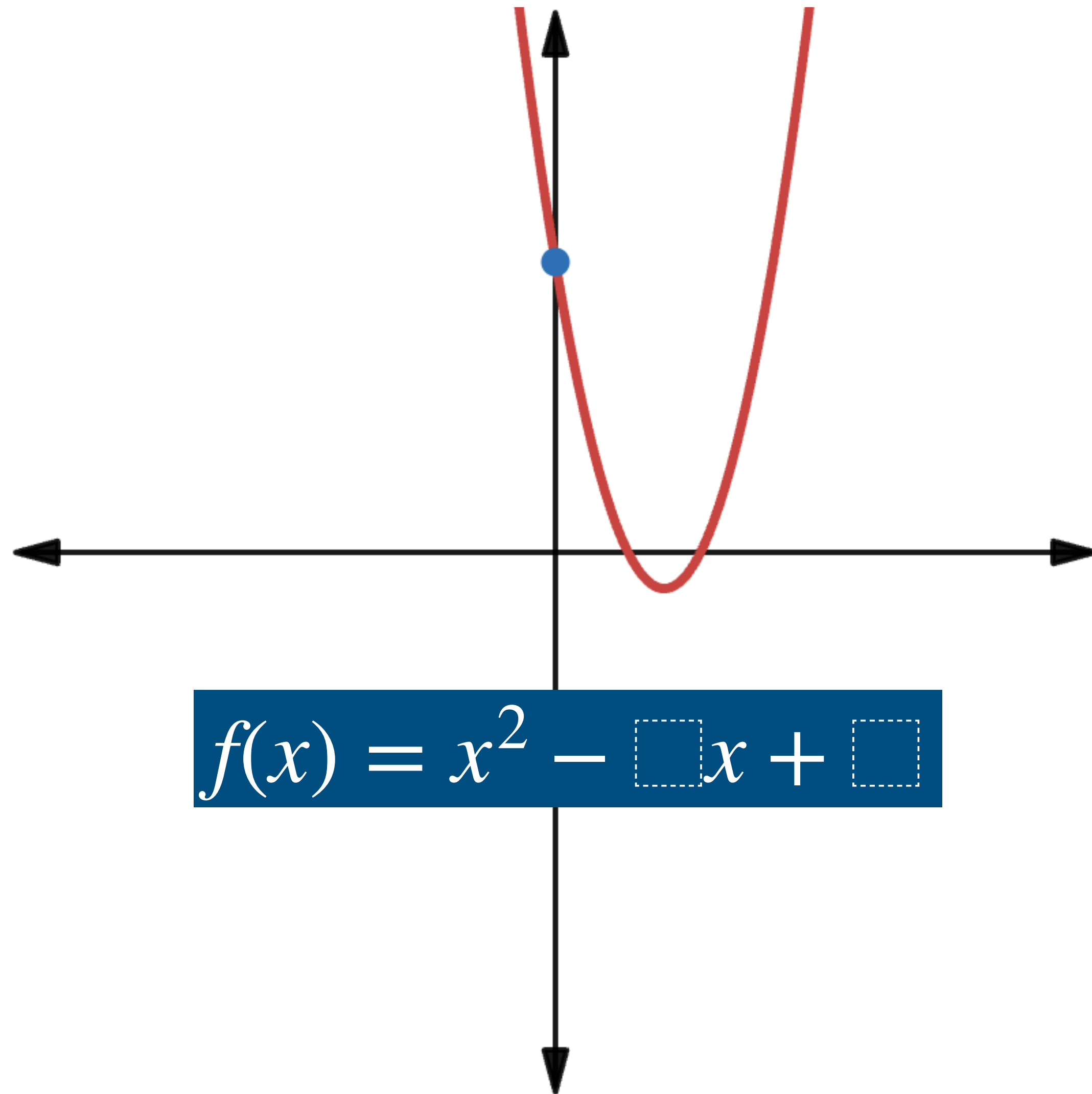
9



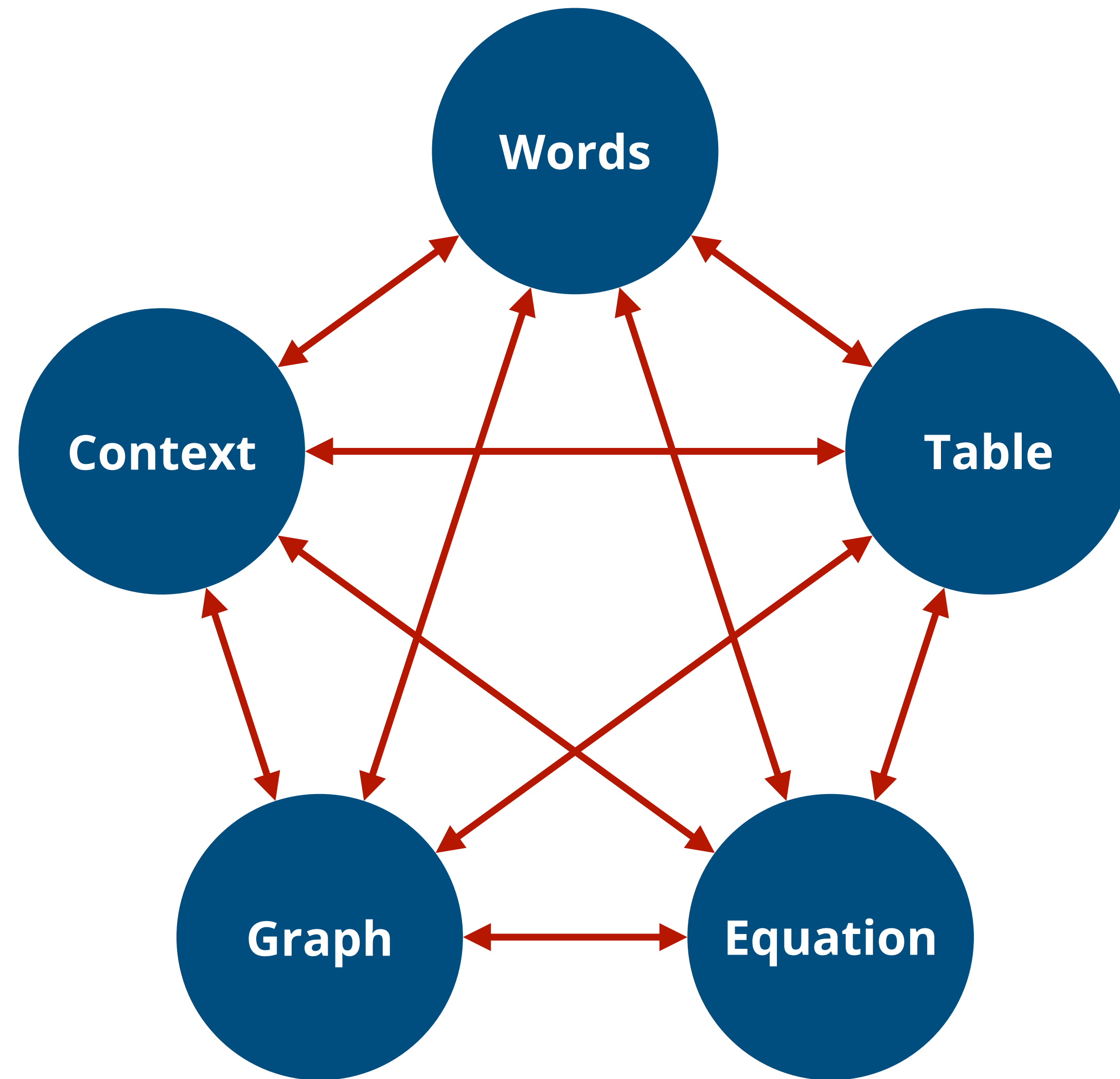




$$f(x) = (x - \square)^2 - \square$$



$$f(x) = x^2 - \square x + \square$$



Once upon a time, there was a thirsty crow.

She came upon a pitcher that had some water in it, but when she put her beak into the pitcher she found she could not reach the water.

Then, she had an idea.

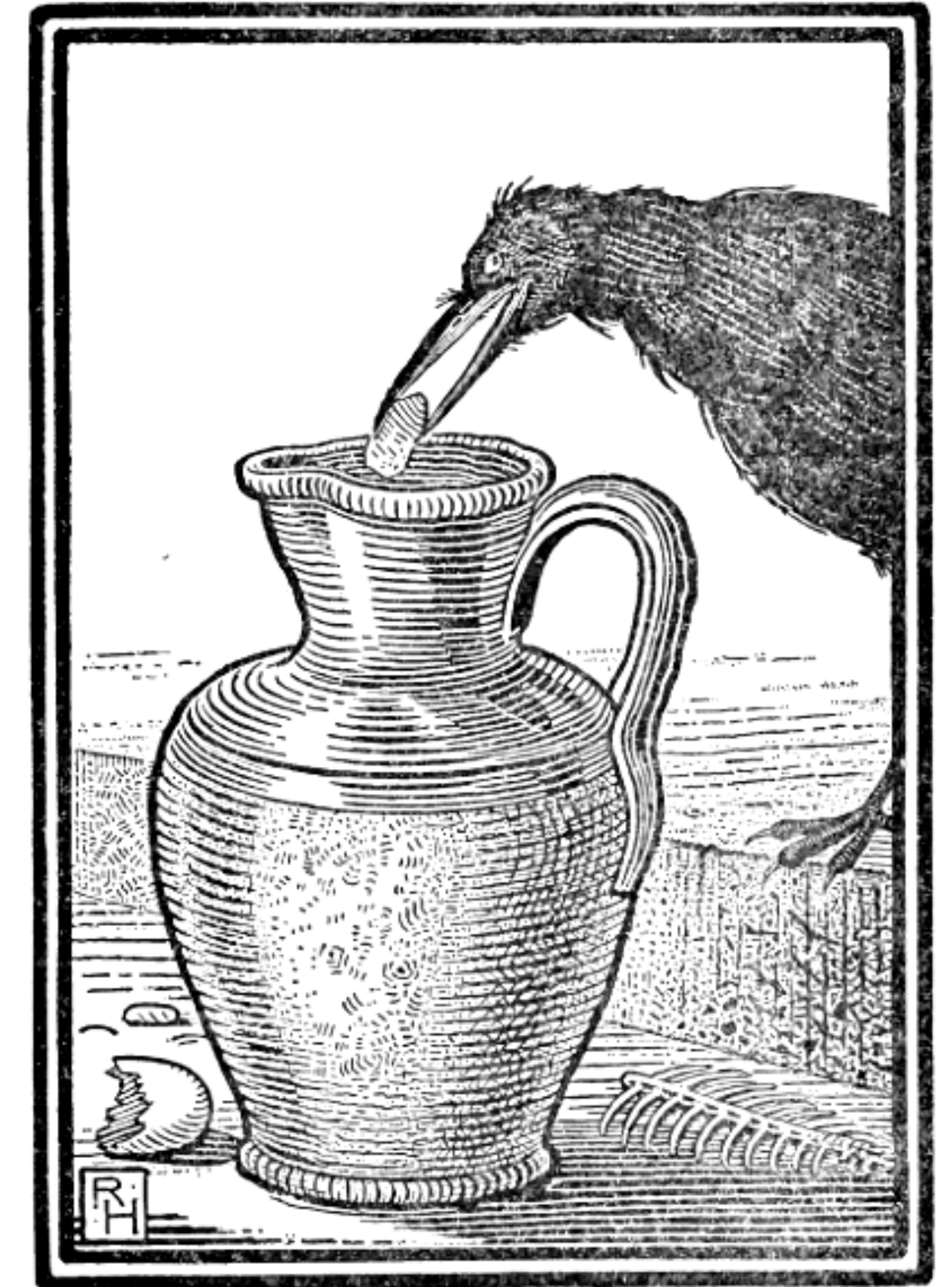
She looked around, found a pebble, and dropped it into the pitcher.

The water rose a little bit.

The crow was encouraged and continued to drop pebbles into the pitcher, one at a time, until the water rose up high enough for the crow to reach it with her beak.

The crow drank and was satisfied!

Moral: **“Little by little does the trick.”**



*Which representation is the **best**?*

*“The **table** is the best. It helps me keep track of the data and find the pattern.”*

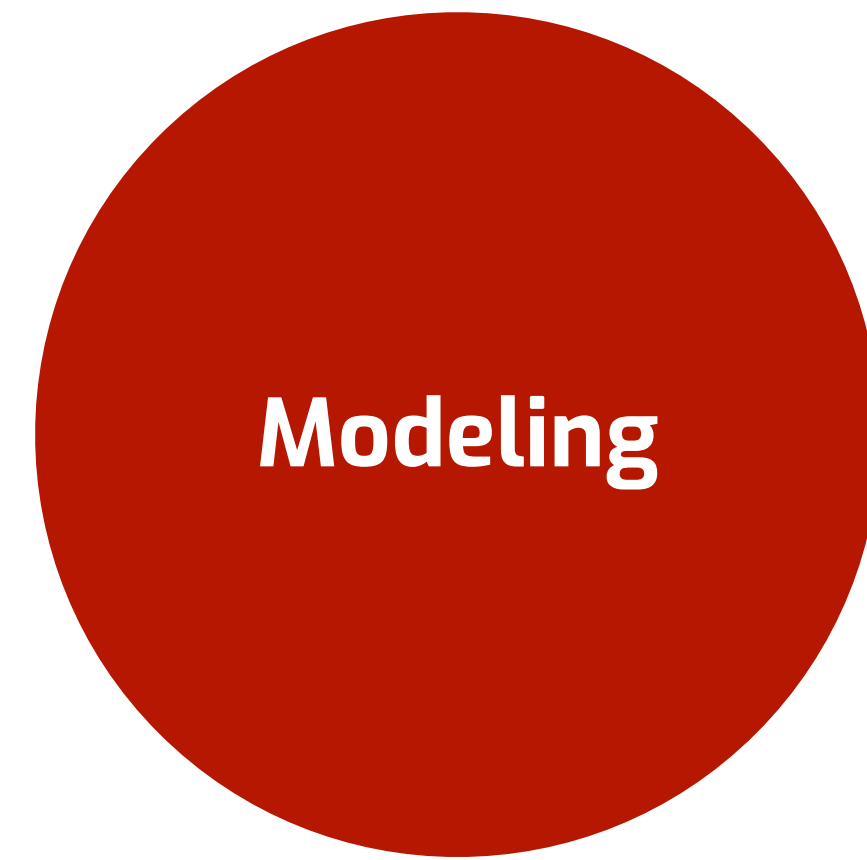
*“The **equation** is the best. It tells me the rate of change without me needing to calculate it. I can quickly solve it to figure out the number of pebbles that I’ll need.”*

*“The **graph** is the best. It shows the relationship between the variables right away.”*

*“You need to fill in a lot of rows in the **table** before you get to 100 mL.”*

*“The **equation** is unnecessary. I can use arithmetic, not algebra, to figure out how many pebbles it will take.”*

*“It’s difficult to sketch the **graph** accurately and read when y hits 100.”*



*How can I make predictions
about real-world phenomena?*

Act 1



TapintoTeenMinds.com

Act 2

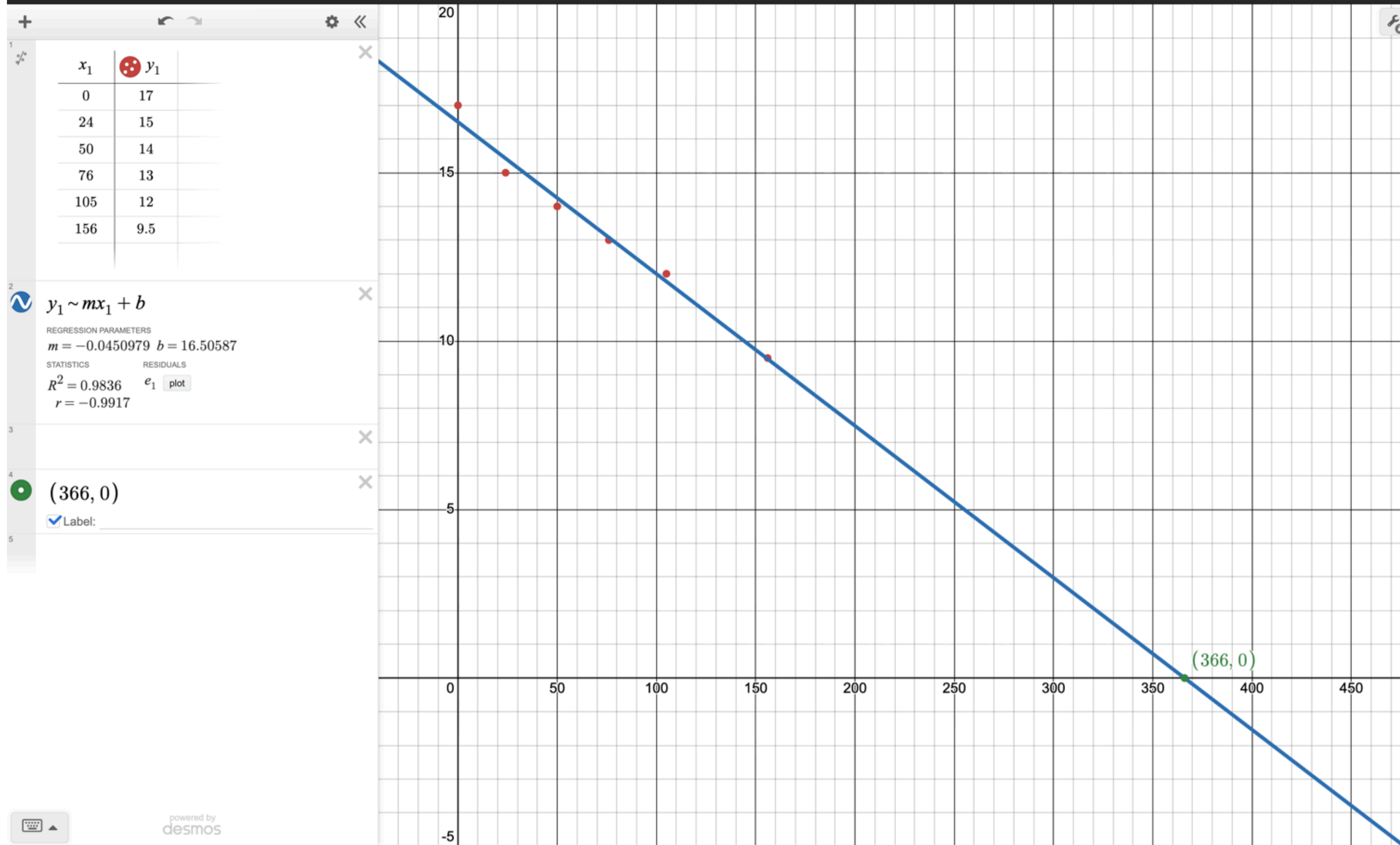


TapintoTeenMinds.com

Act 3

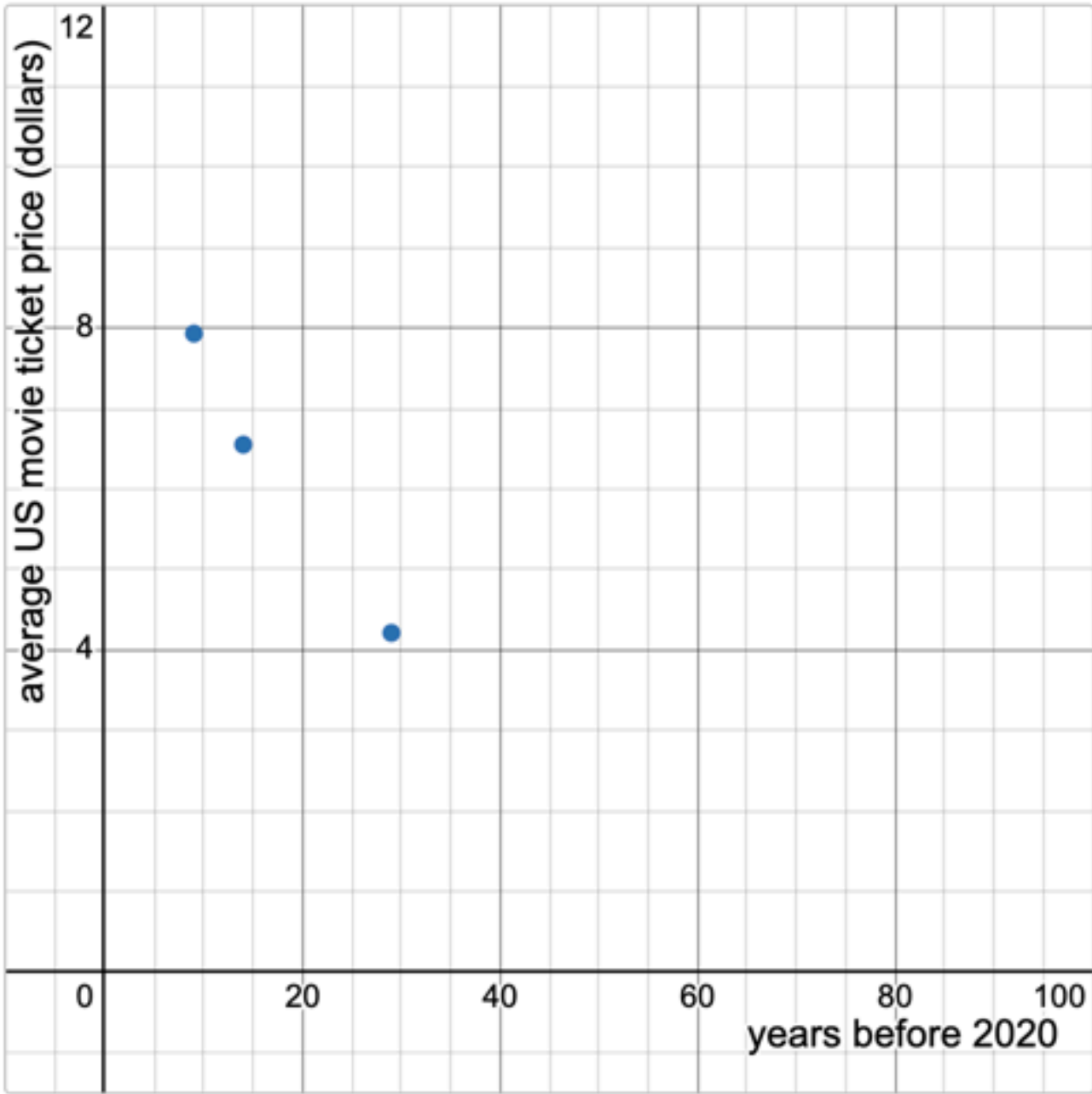


TapintoTeenMinds.com





Build a model.



The blue points represent average US movie ticket price for several years.

What kind of function will best fit the data?

After you make your selection, drag the red points to fit the function to the data.

- ☐ Linear
- ☐ Quadratic
- ☐ Exponential

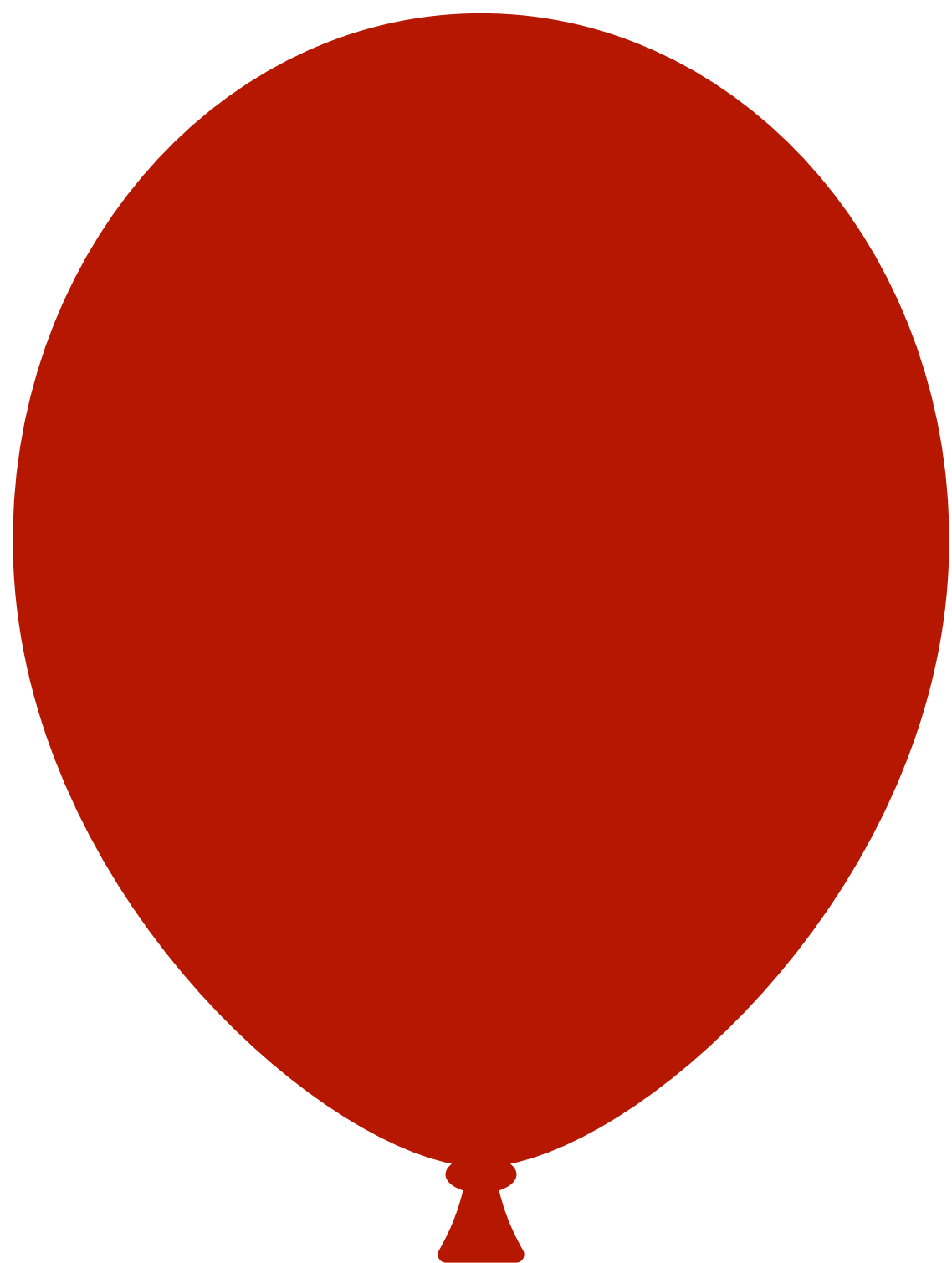
Teacher Moves

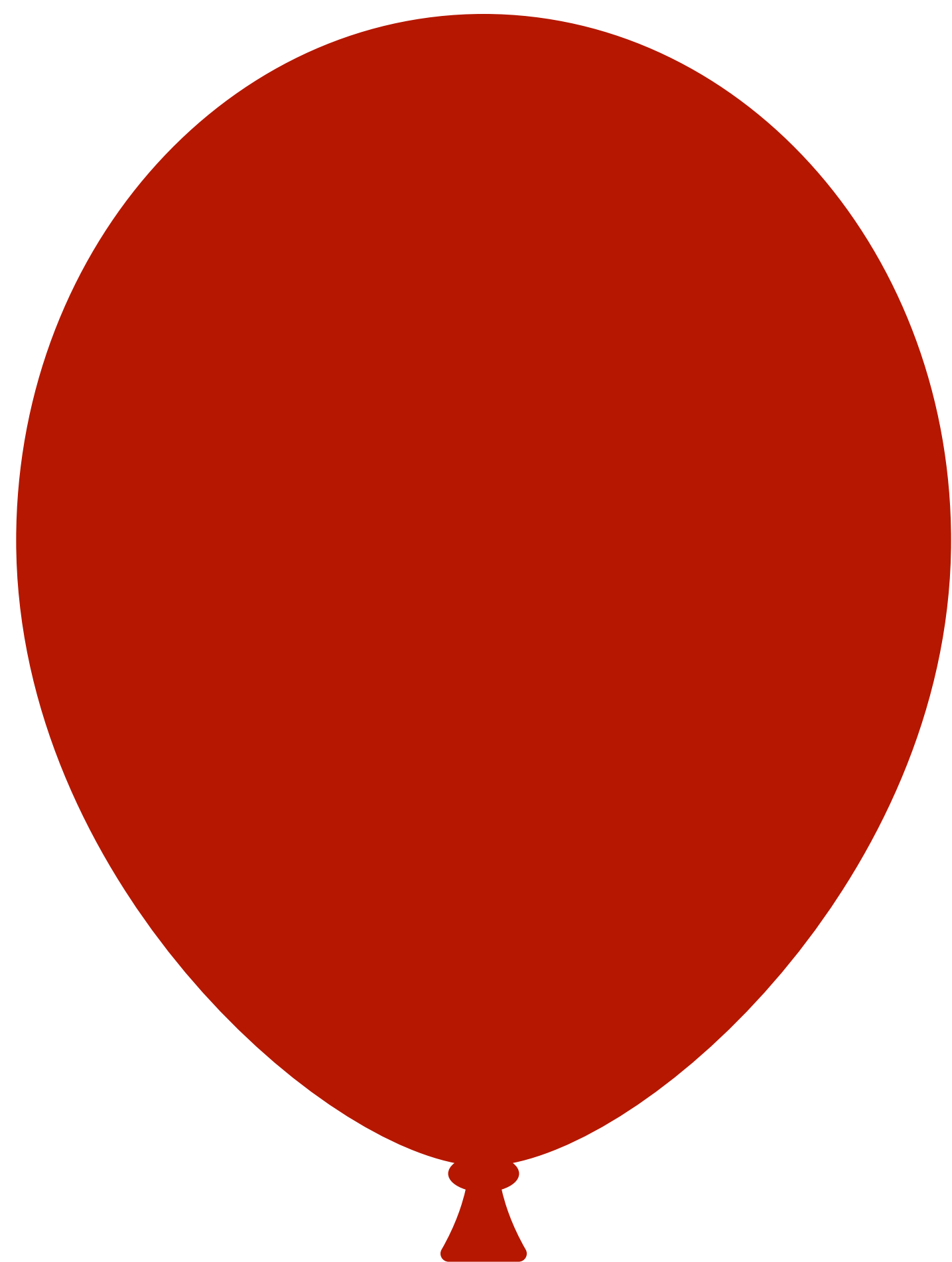
Use the teacher dashboard to see a visual summary of student responses.

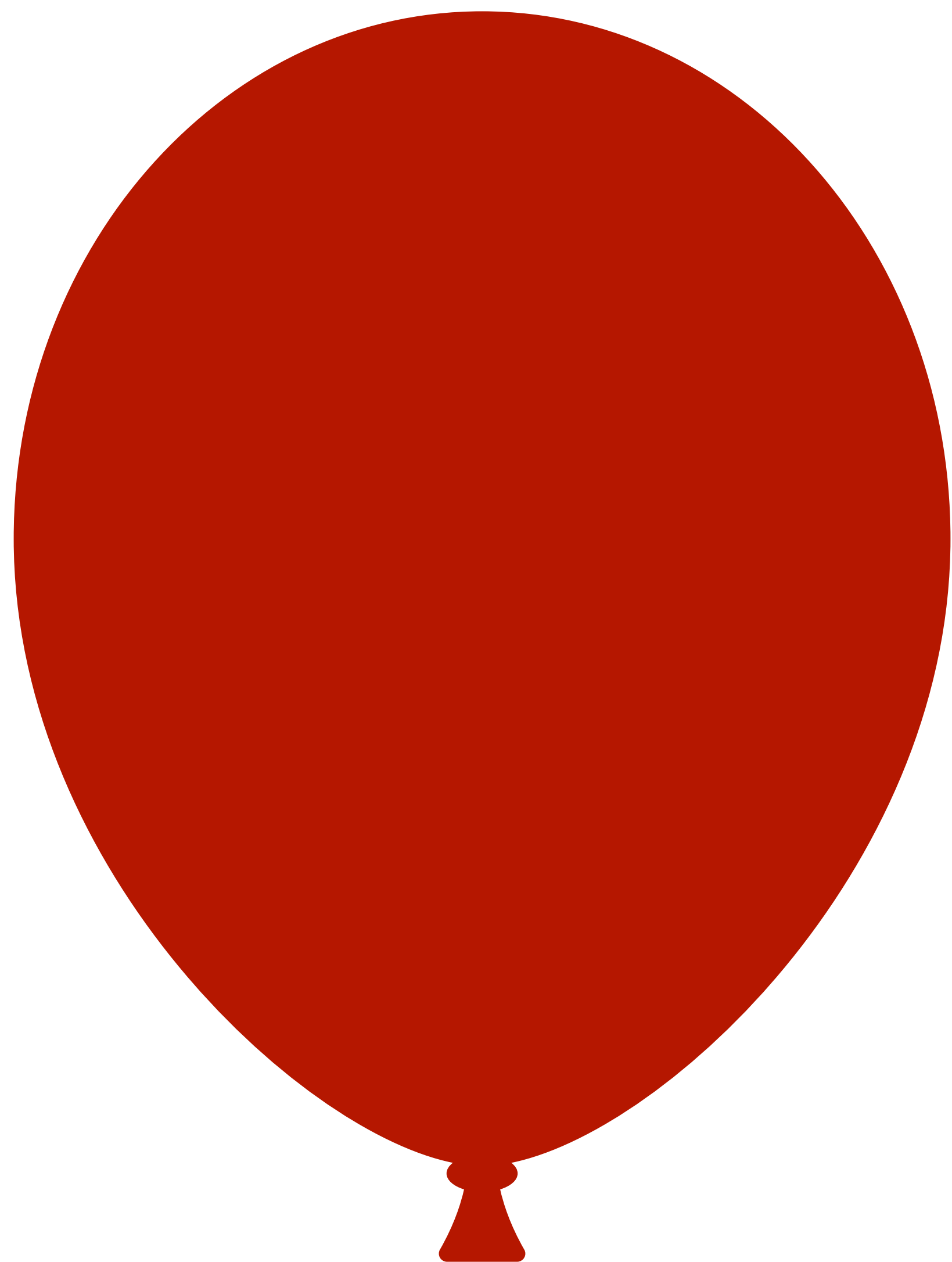
Before correcting students who select an inappropriate model, let them feel the "consequence" of their choice on the next screen.

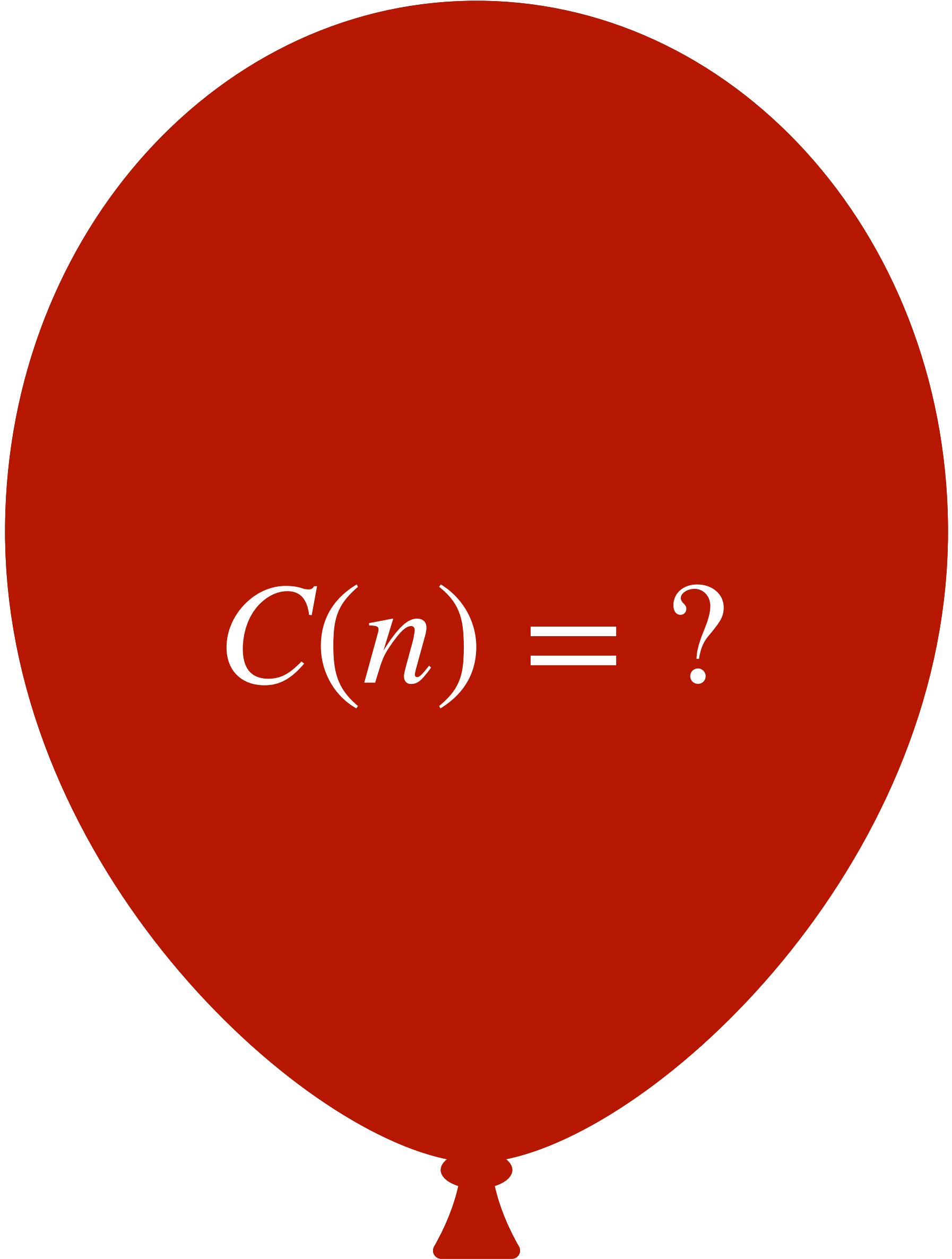
Dashboard Note: indicates that the student selected "Exponential" and that the model fits the data well.





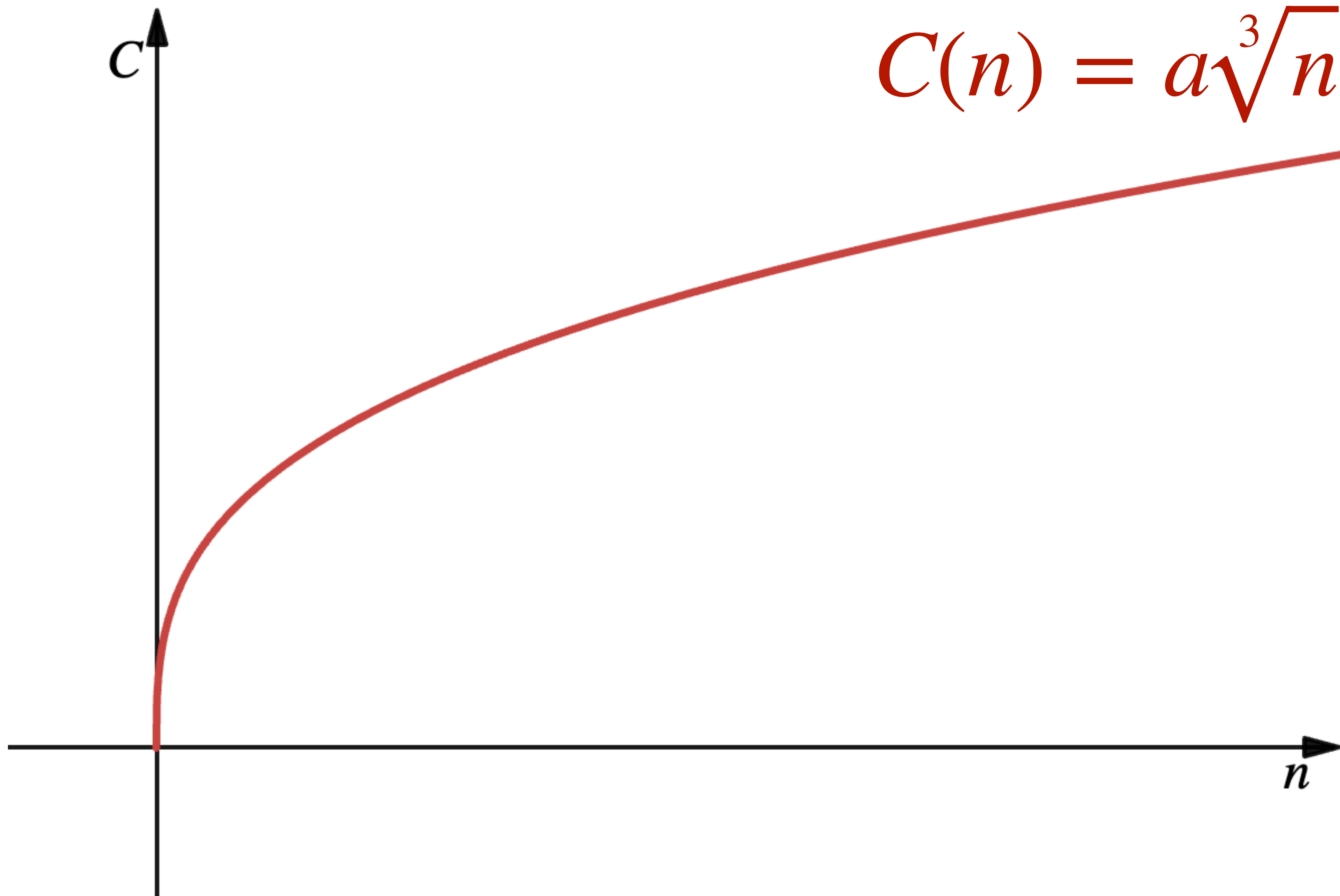






A large red balloon is centered on the page. It has a small knot at the bottom where a string would be attached. The balloon is a solid red color.

$$C(n) = ?$$



Which One Doesn't Belong?	chrishunter.ca/2017/11/01/alike-different-which-one-doesnt-belong-more/
What's the Function?	polypad.org/kNif7EN4EVXZvA
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