Instructional Routines for Teaching & Learning Mathematics

Summer Institute 2025

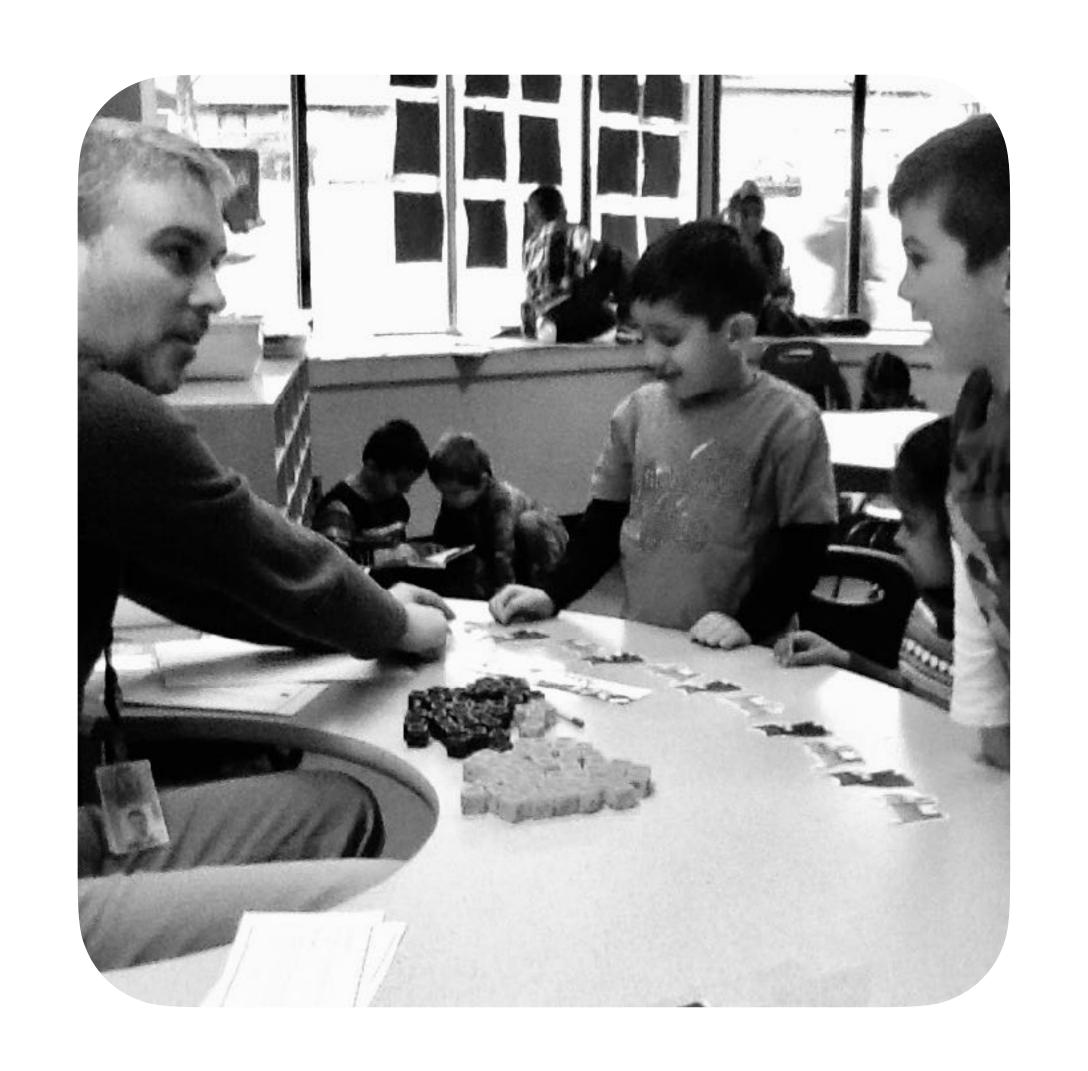


Chris Hunter

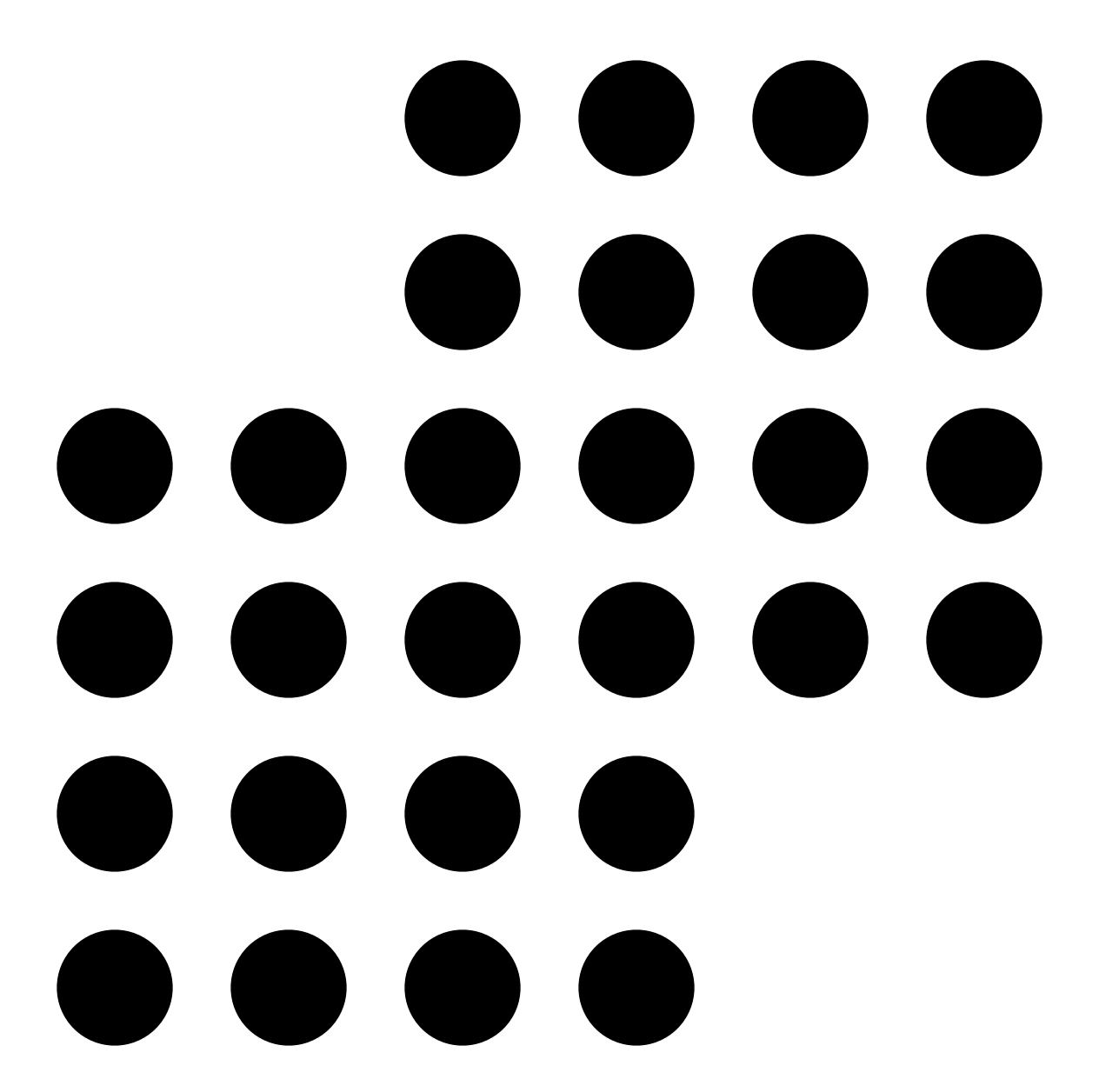
K-12 Numeracy Helping Teacher Surrey Schools

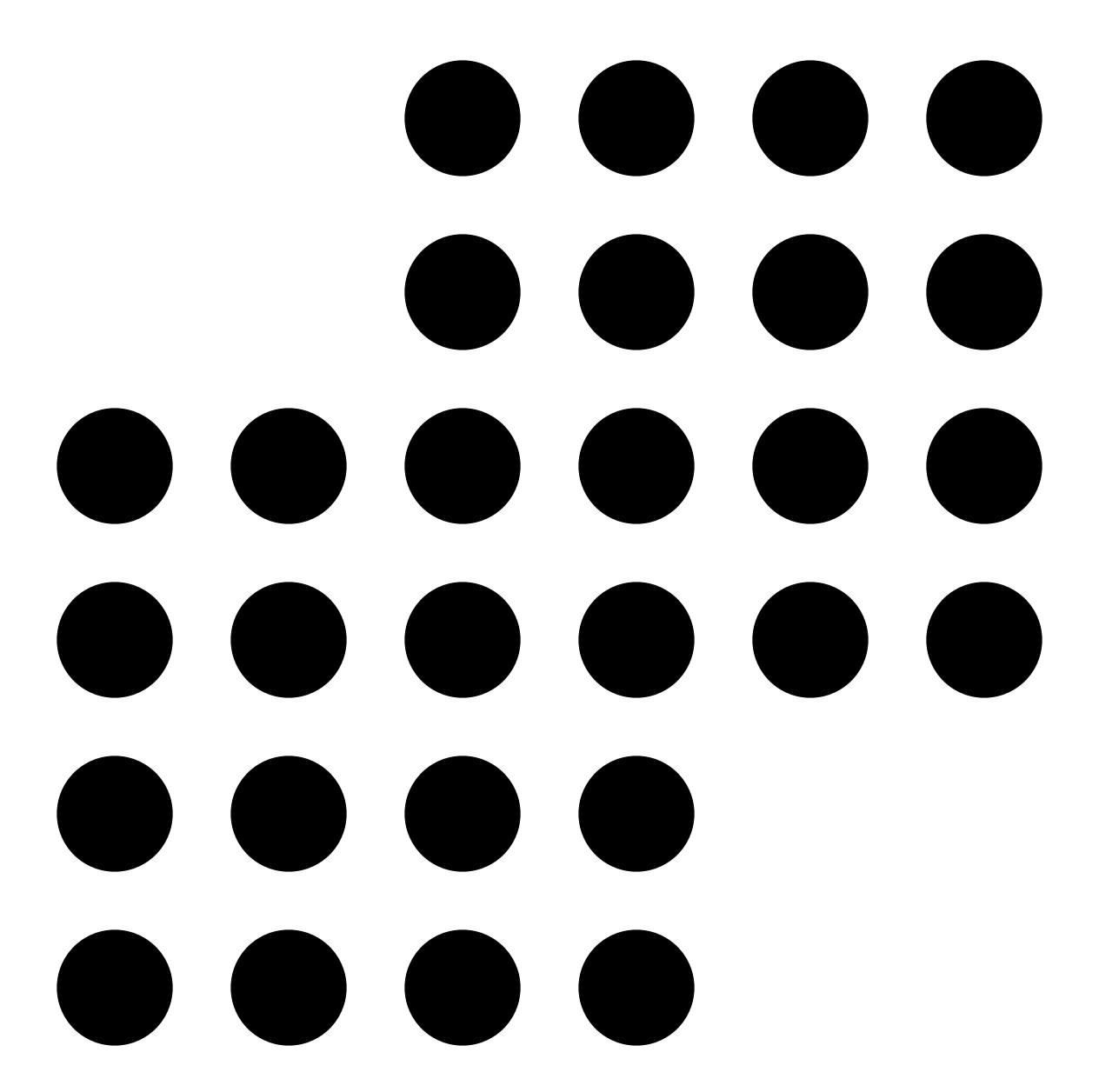
email: hunter_c@surreyschools.ca

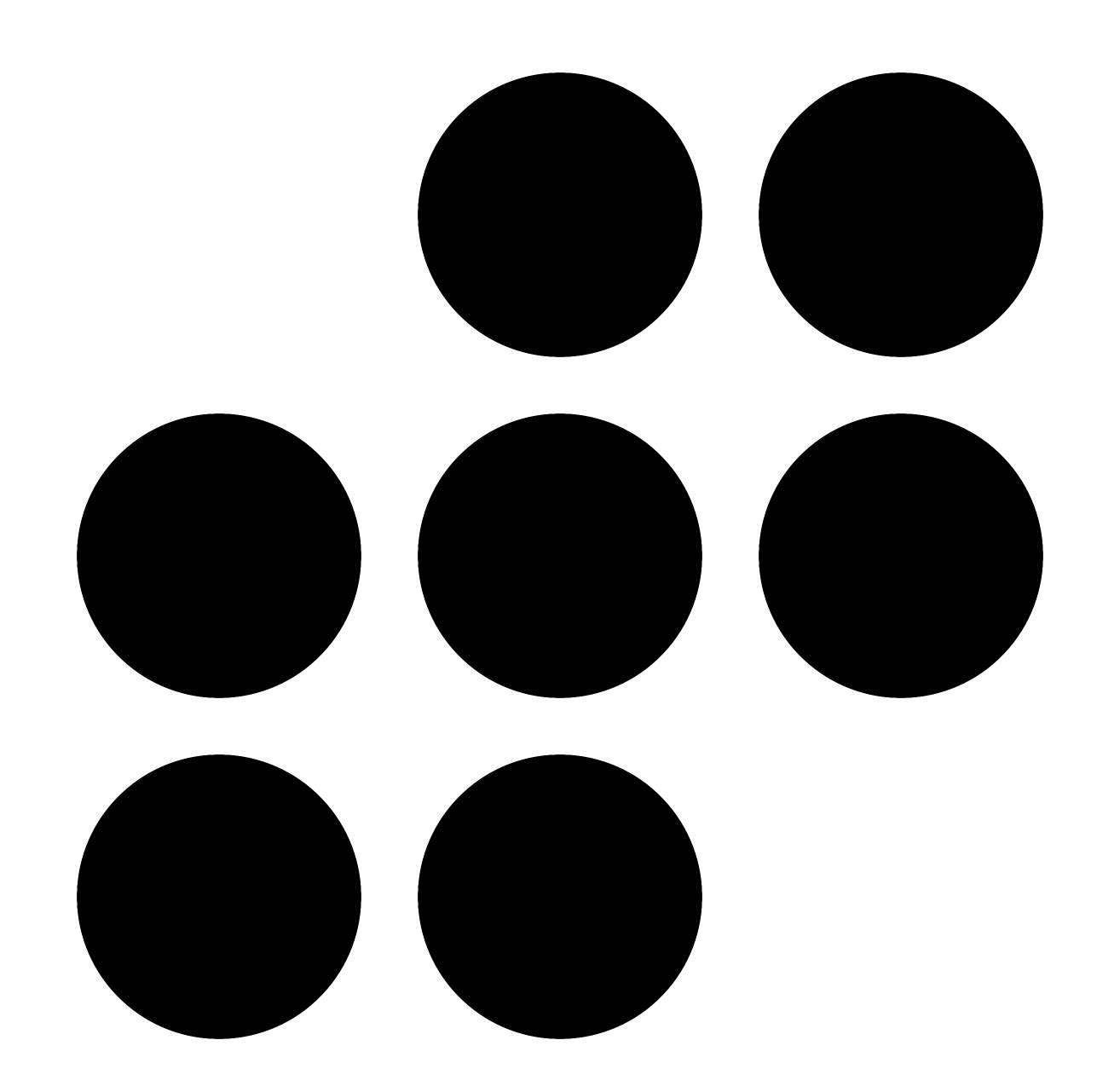
blog: chrishunter.ca









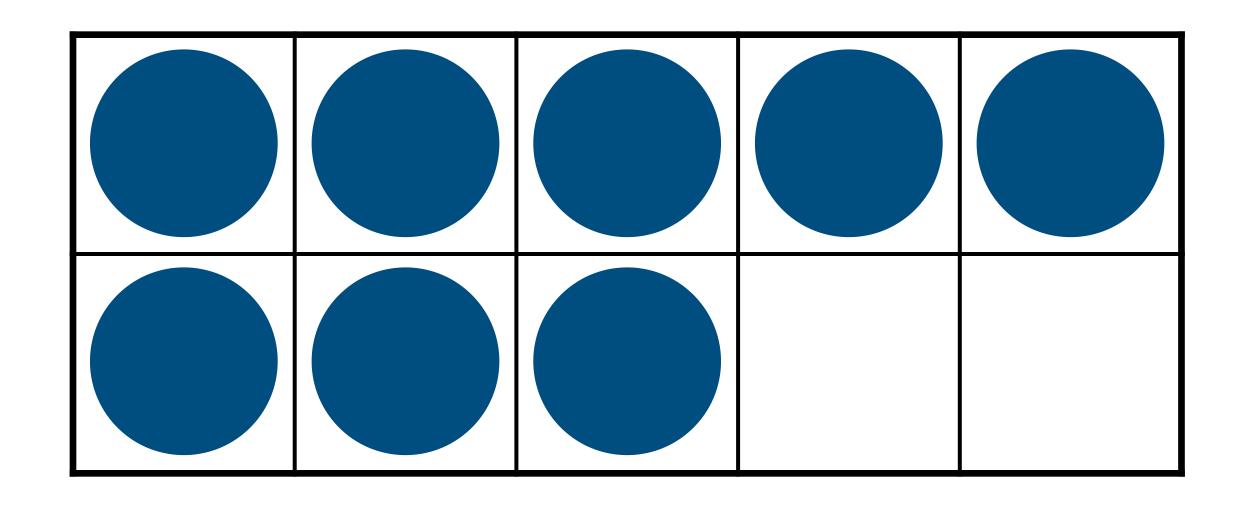


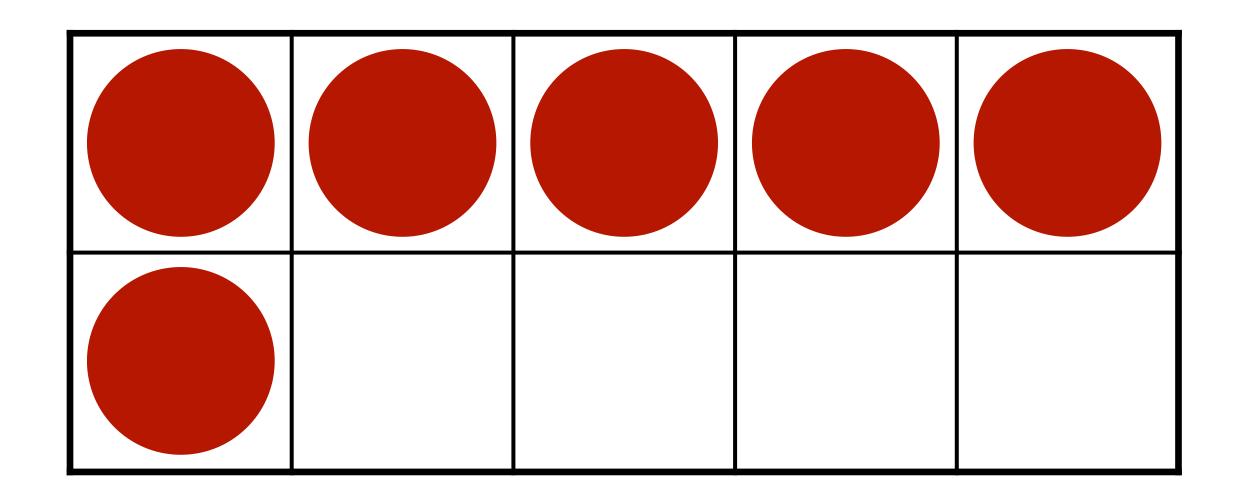
"The predictable structure lets students pay less attention to ['What is it that I'm supposed to be doing?," "What question will I be asked next?,' or 'How will things work today in the lesson?'] and more attention to the way in which they and their classmates are thinking about a particular math task.

For you as the teacher, the routines keep the flow of the mathematics instruction deliberately predictable so that, as you gain familiarity with them, you can better attend to the most unpredictable elements of your mathematics instruction: how your students are making sense of the mathematics."

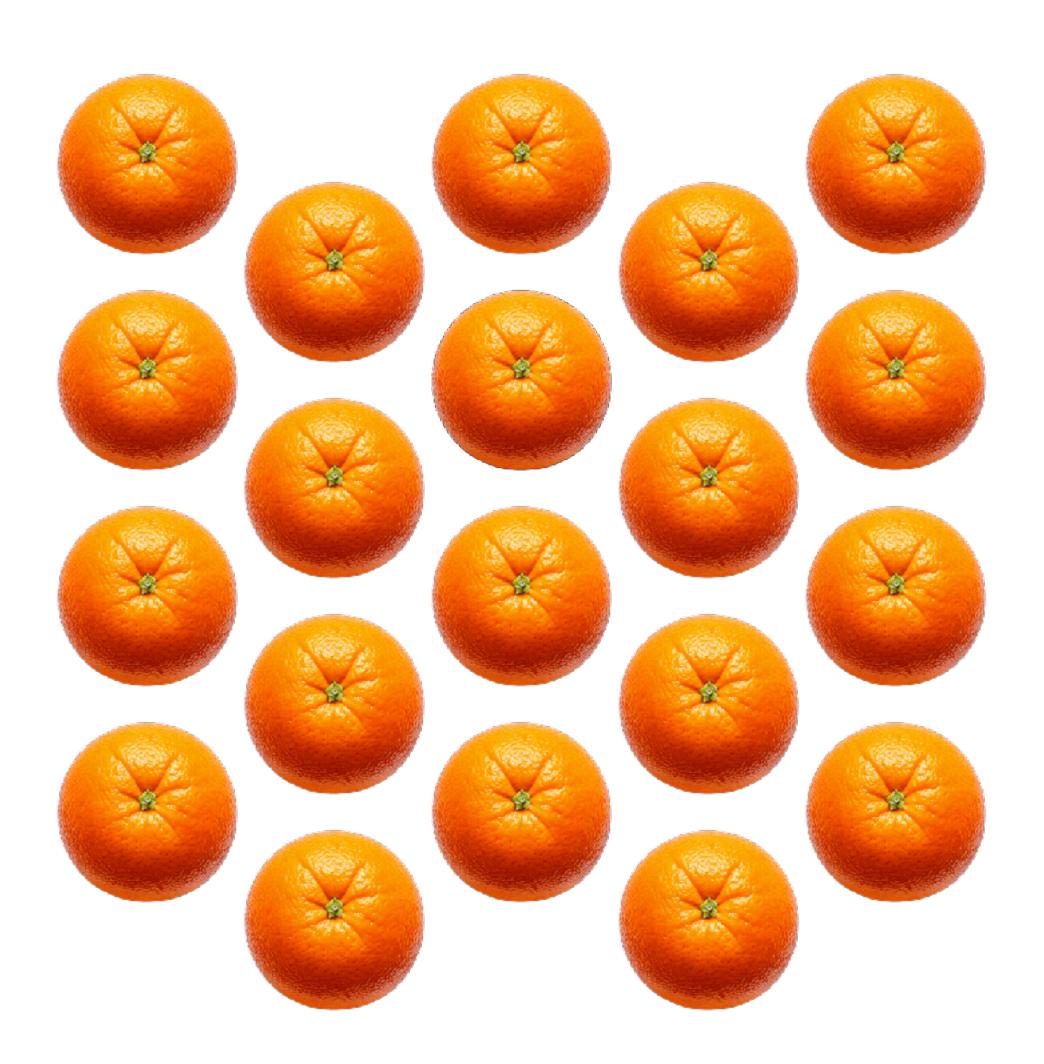
Quick Images

"No matter what grade you teach, even high school, so-called 'dot cards' (which may or may not have dots) are a great way to start your students on the path to mathematical reasoning. We say this because, from experience, we have realized that with dot cards, students only need to describe what they see—and people have many different ways of seeing!"









Instructional Routines for Teaching & Learning Mathematics

Summer Institute 2025

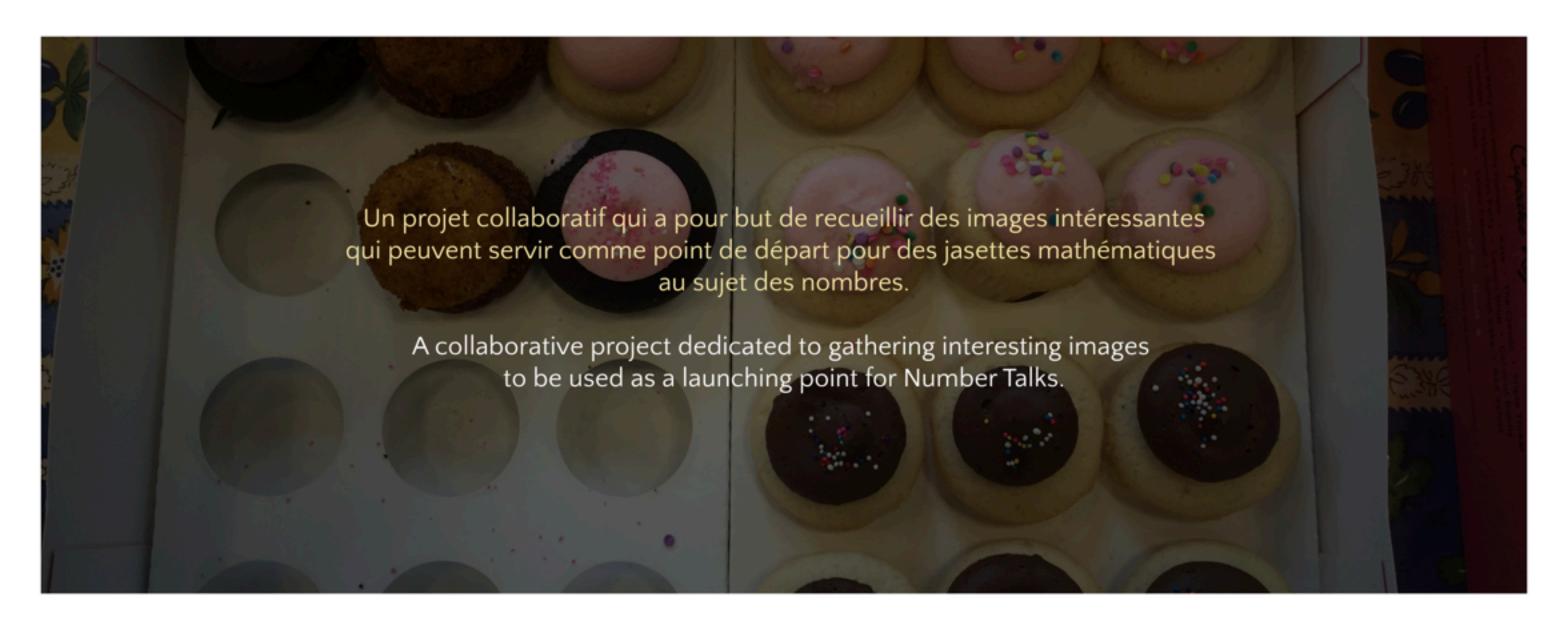




"Not only is 'What counts as one?' an important question, its answer changes based on your perspective, and so it offers opportunities for play. Children like to play; they need to play. Children find numbers wonderful, delightful, interesting and fun. Numbers constitute a playground for children's minds!"

NUMBER TALK IMAGES

ACCUEIL | HOME POINTS | DOTS PHOTOS SUITES | STRINGS ÉLÈVES | STUDENTS MORE..



En vedette / Featured...

Custom Number Talk Images

Créer vos propres images! Voici une ressource de Berkeley Everett. Offert en format PowerPoint ou Google Slides, vous n'avez qu'à modifier les diapositives afin de produire des images sur mesure.

You can create your own Number Talk Images thanks to Berkeley Everett! Using his shared PowerPoint or Google Slides templates, you simply edit/re-arrange images of kumquats, blueberries, nuts and toaster pastries.

Custom Number Talk Images Select and copy the images you want Paste onto background image Delete/rearrange for custom image (or mix/match groupings)

Steve Wyborney's Blog

Sharing Thoughts About Education

Subscribe

Home

Books ~

Courses

About

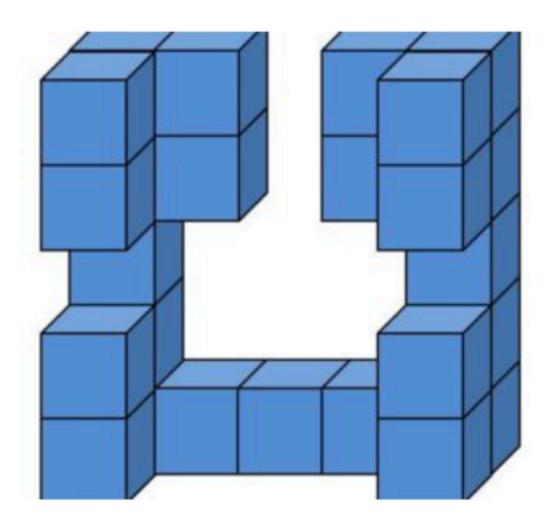
Contact

FAQ

Q

December 29, 2017

Cube Conversations

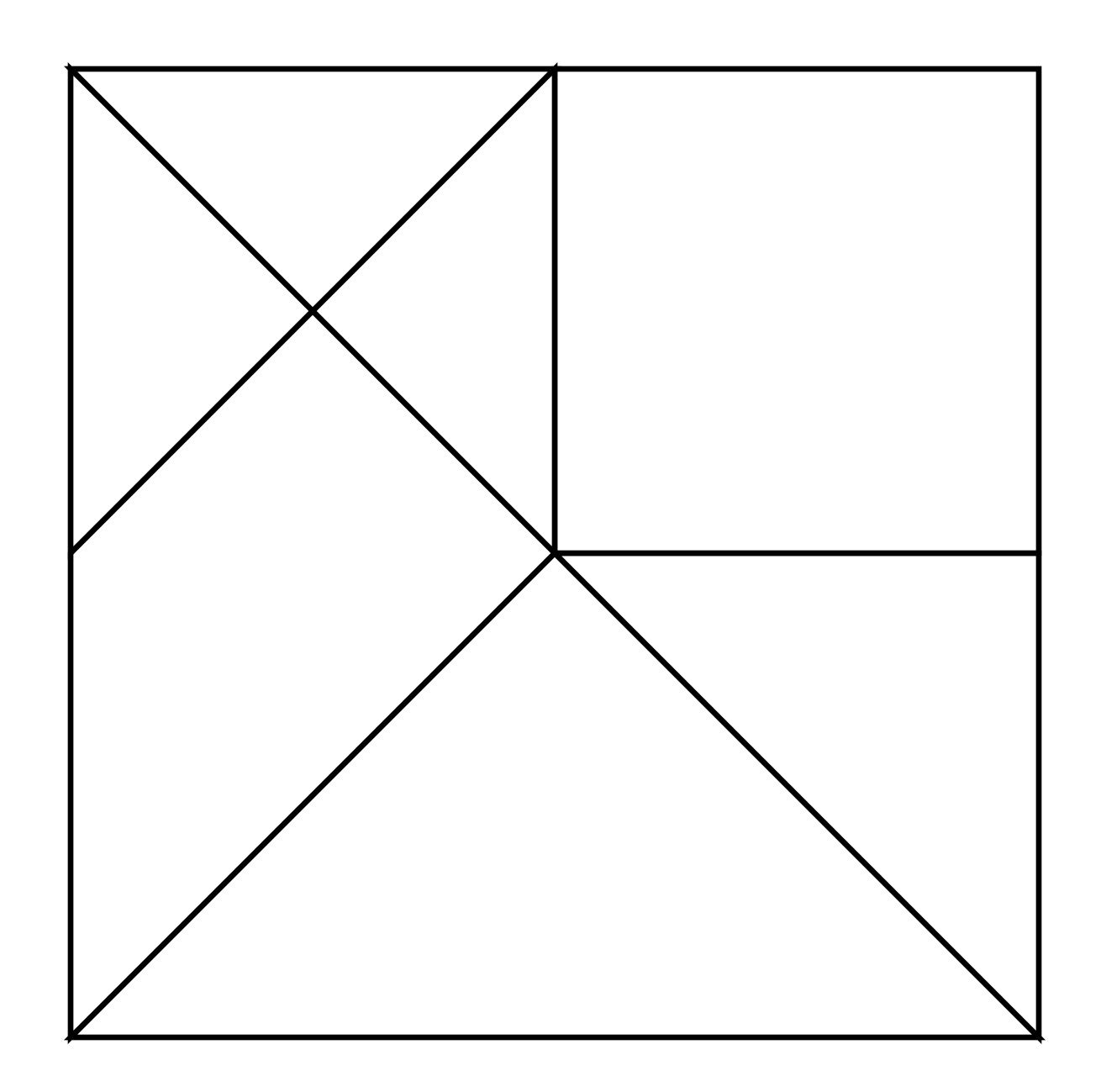


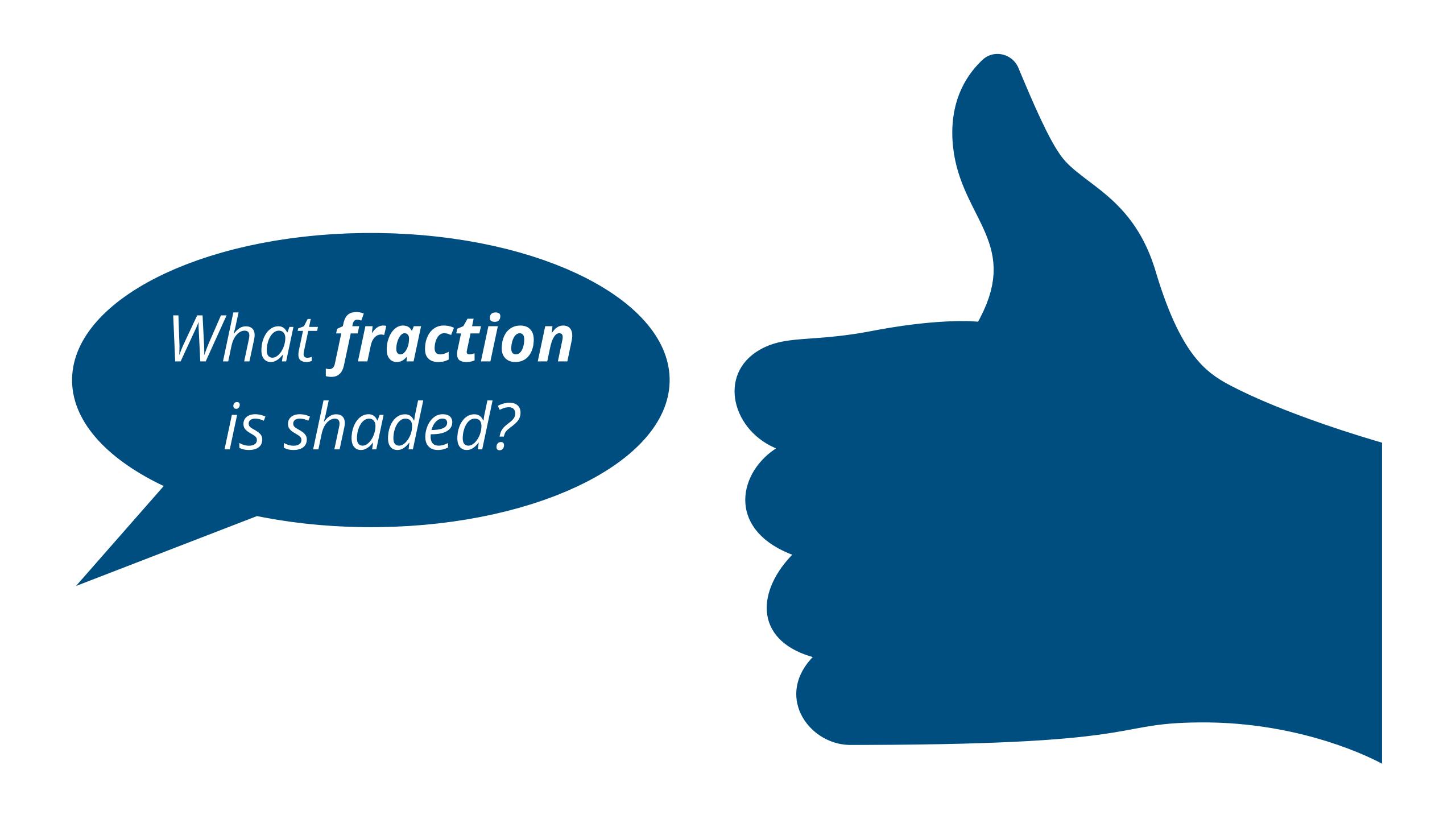
Categories

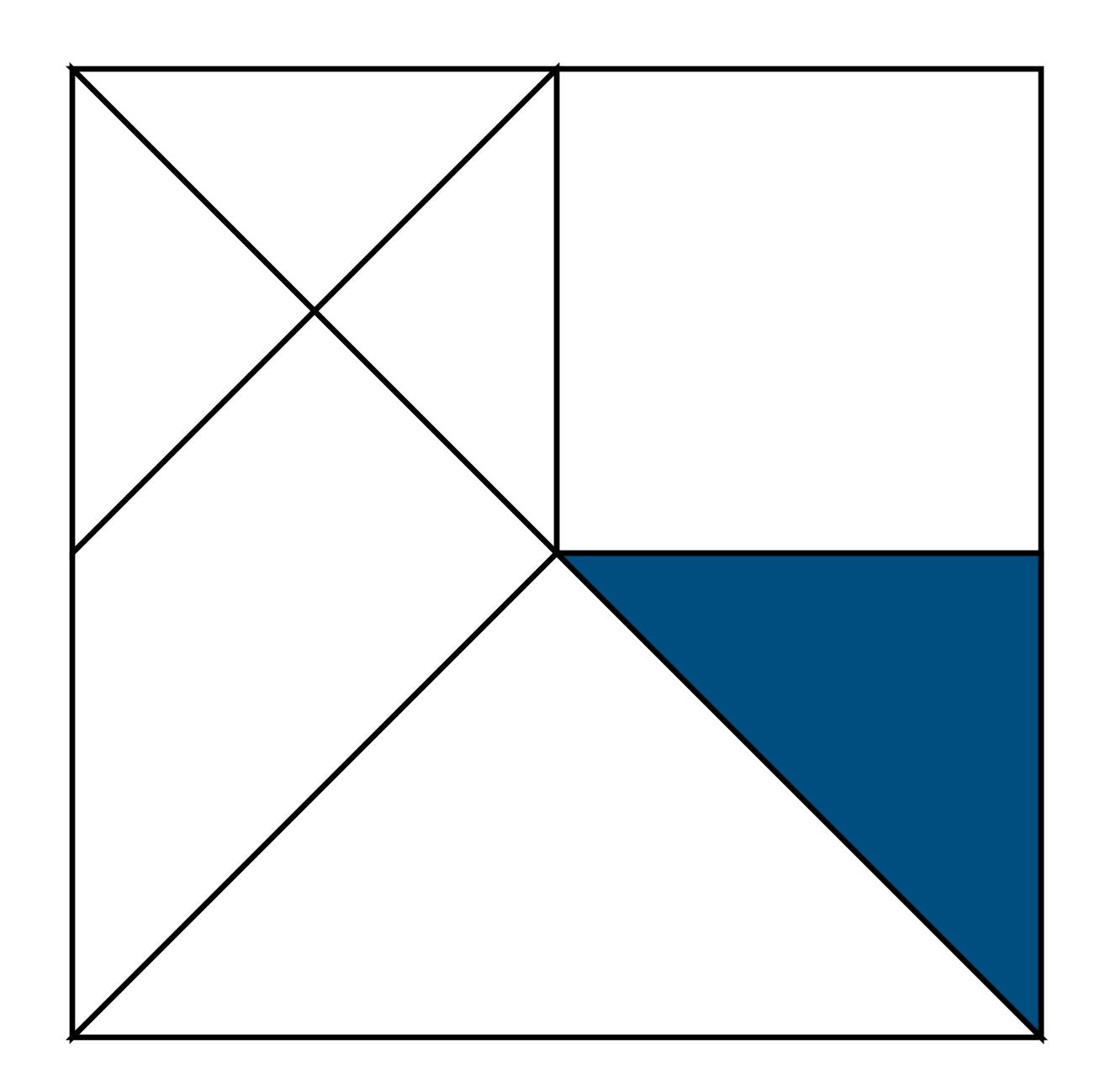
- <u>3-Container Estimation</u> <u>Routine</u> (1)
- Animated Posts (64)
- <u>Course</u> (1)
- <u>Cube Conversations</u> (3)
- <u>Dot Patterns</u> (4)
- Downloadables (29)
- <u>e-book</u> (1)
- Esti-Mysteries (11)
- Estimation (13)
- Estimation Clipboard (1)
- Google Slides (5)
- <u>Instructional Strategies</u> (66)
- <u>Leap Day</u> (1)
- Leaping Numbers (2)
- Math (68)
- Multiplication (2)
- Multiplication Course (2)
- Number Sense (10)

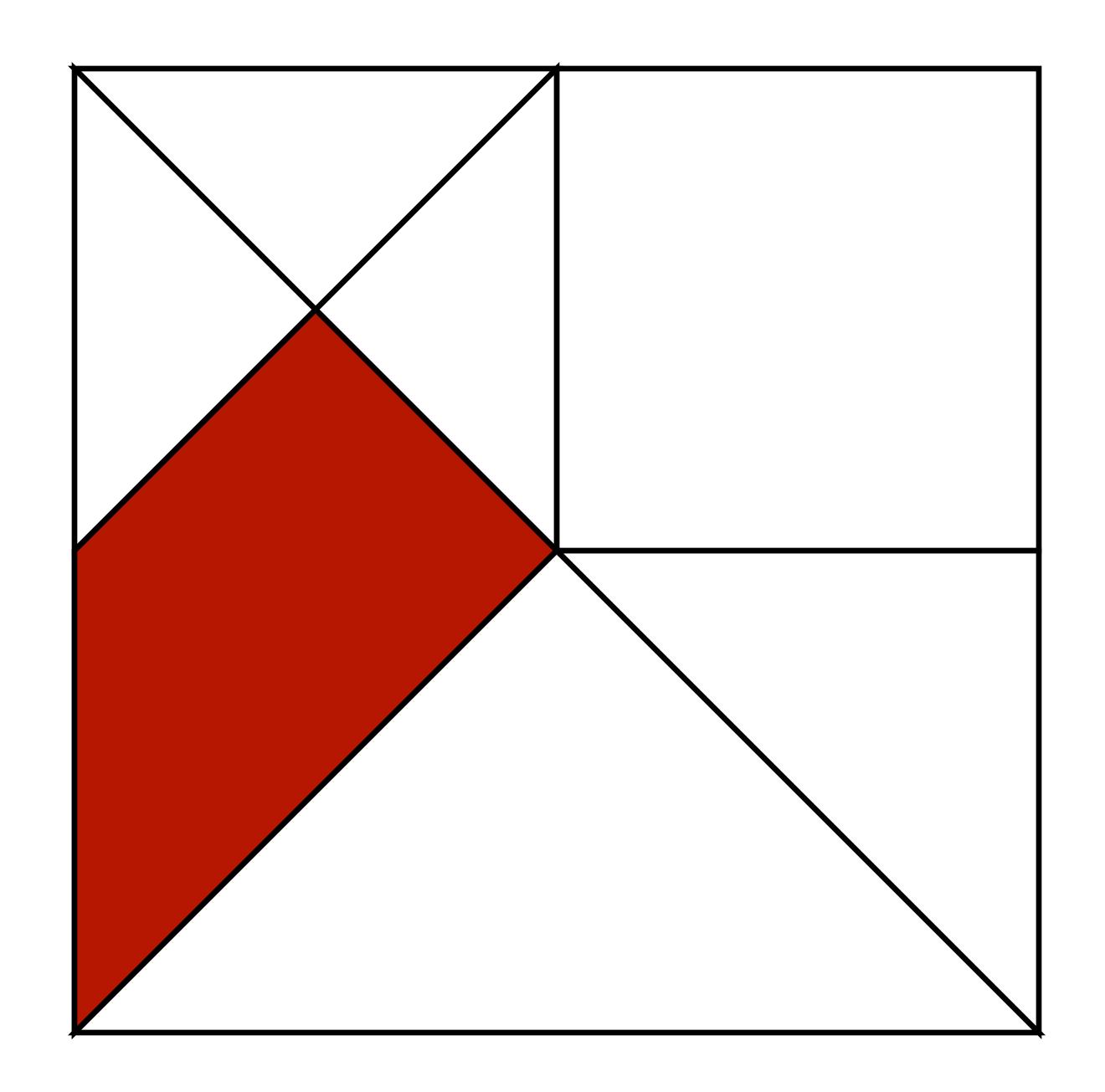


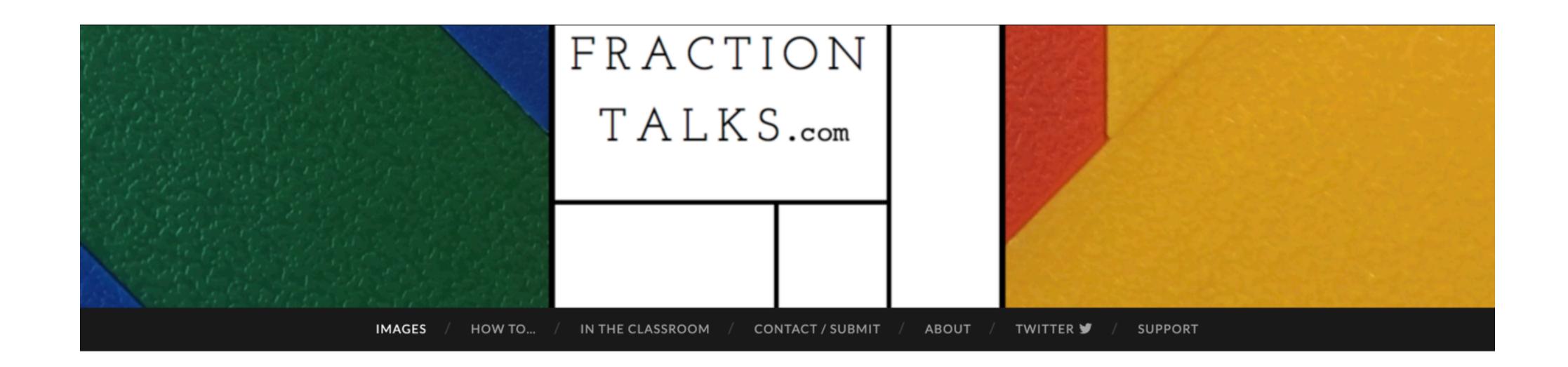
Fraction Talks

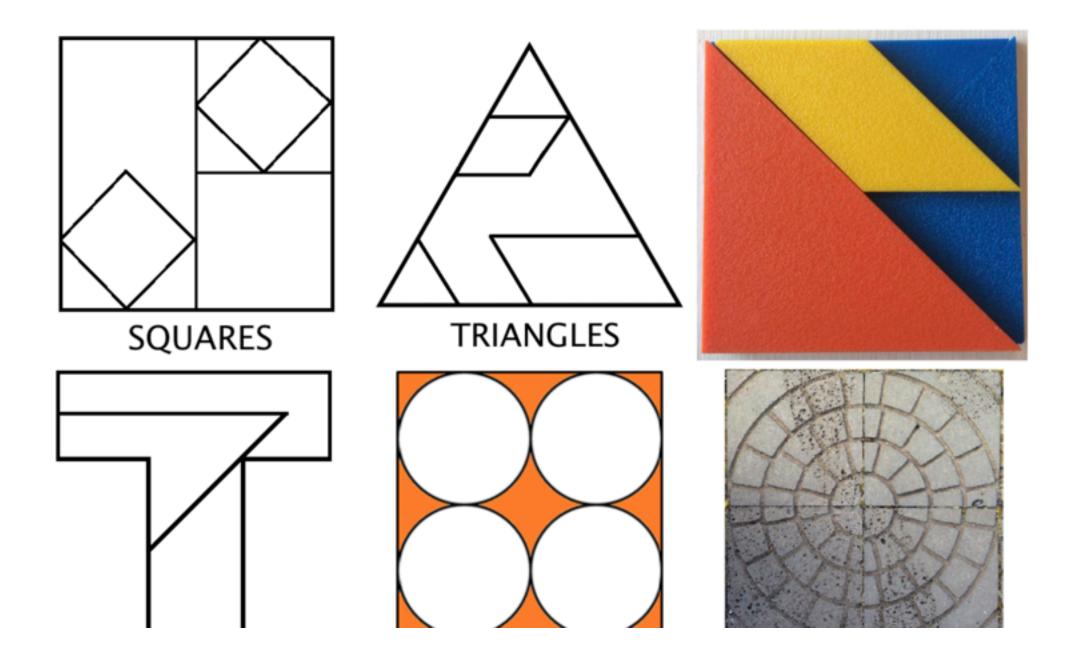








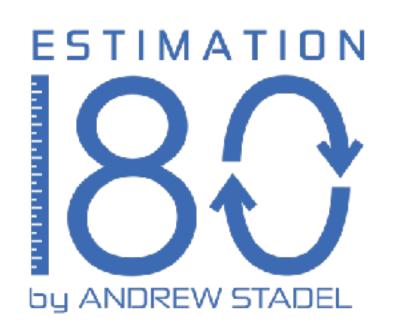




Can you shade a section with twice the area? Can you shade exactly one-quarter of the shape? Can you find all other sections that are the same size as ____? Can you find all sections that represent ? If the shaded section is worth ____, how big is each other section? What possible fractions can be shaded? Which section has the easiest area to find? What needs to be added to make the shaded section equal to ____? If the area of the shaded section is ____, what is the area of the whole shape? Shade ____ as many ways as possible.

Estimation 180

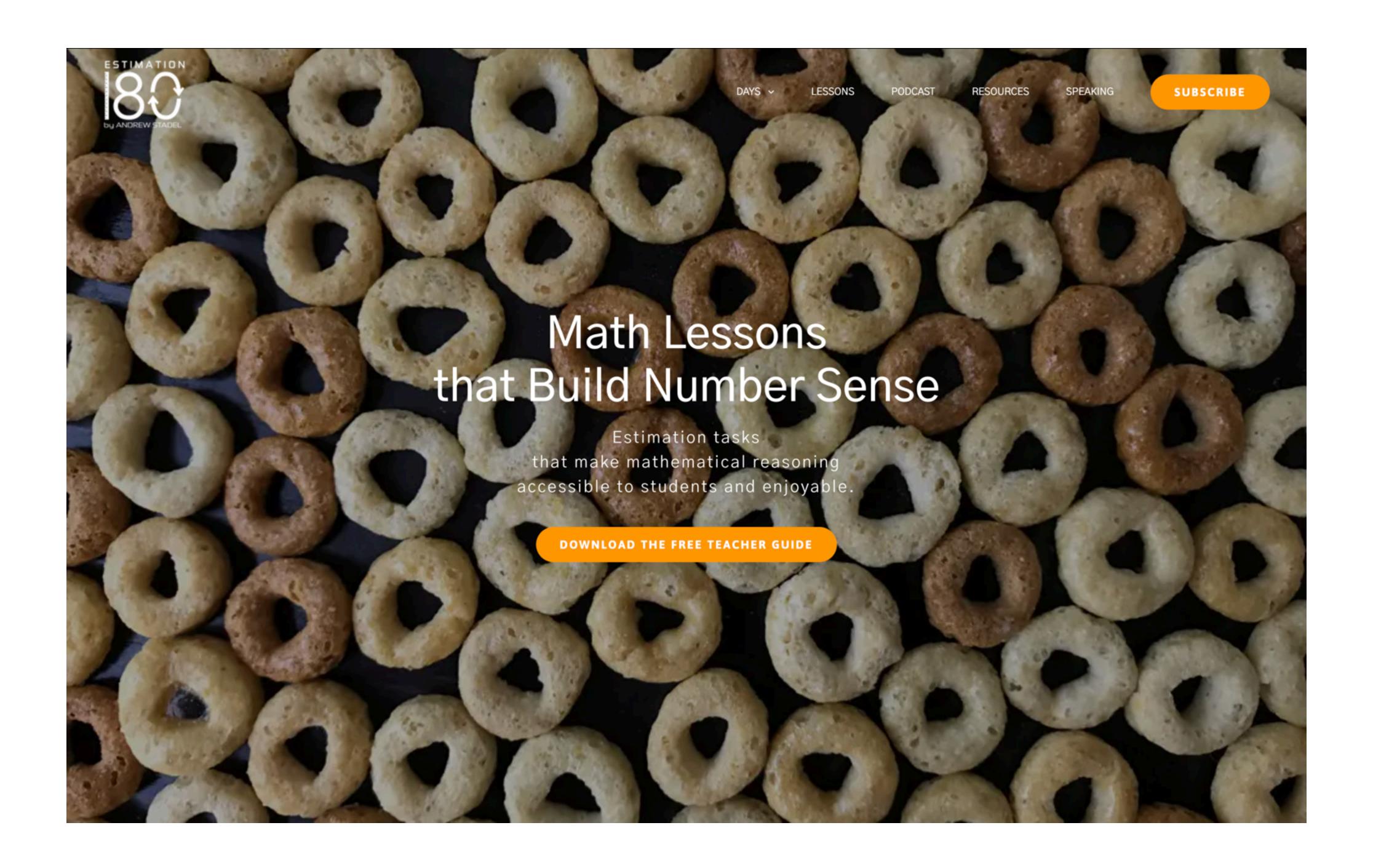












"For each challenge, students are asked to give an estimate they know is too low and another that is too high. These bounding estimates are so important. We're working toward the idea of a reasonable range of estimates, which is one of the most common ways we estimate in daily lives." "Also, students who are worried about estimating 'right' often feel much less nervous when asked for an answer they know is wrong because it's too low or too high. The bounding estimates are a great way to help tentative and struggling students enter a meaningful math discussion."

"Whether you use it daily or choose specific lessons to complement your curriculum, the most important thing you can do is focus on students' reasoning and arguments. Students need to learn that estimating involves strategy and is not the same as guessing. Class discussions around strategies, including reflecting on our estimates and refining our strategies, are powerful opportunities for students to build number sense and mathematical intuition in a variety of contexts."

Counting Collections

Today, you and your partner are going to count a collection, figure out how many you have in your collection, and show me a picture of how you counted.



"In Counting Collections, students have the opportunity to figure out how to count with a partner or partners; they get to navigate mathematics, their explanations, and others' ideas as they figure out how to work together."

Ca-Lishea served at the Houston Food Bank by putting together food boxes that go to senior citizens. Each box contains 26 meals. The boxes are loaded onto a pallet that holds 45 boxes. How many meals are there on the pallet?

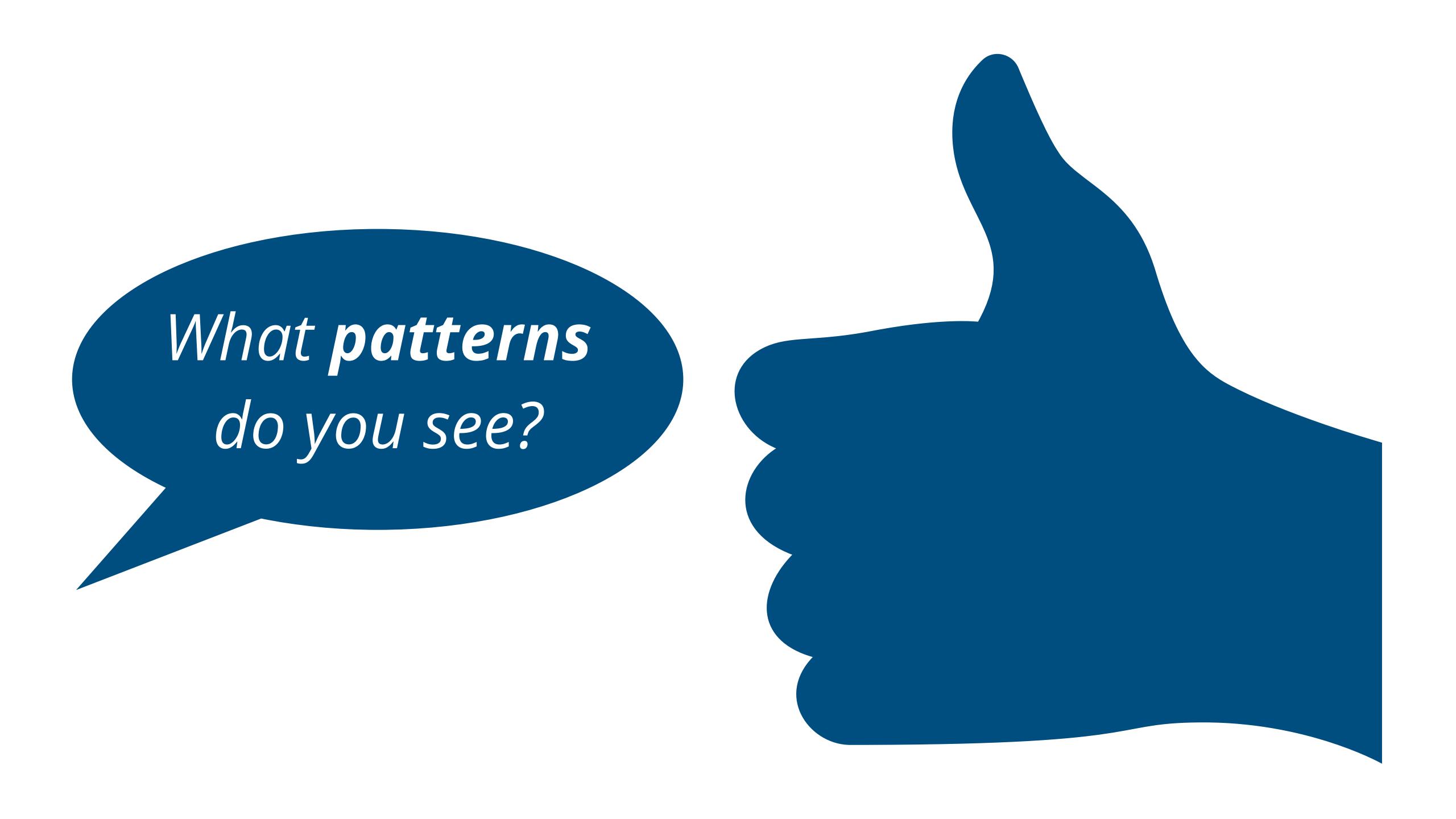
"When you're a grown-up, nobody says 'Please multiply these numbers.' You have to know when to do it. That's all that actually matters when you're a big person."

Marian Small OAME2024

Choral Counting

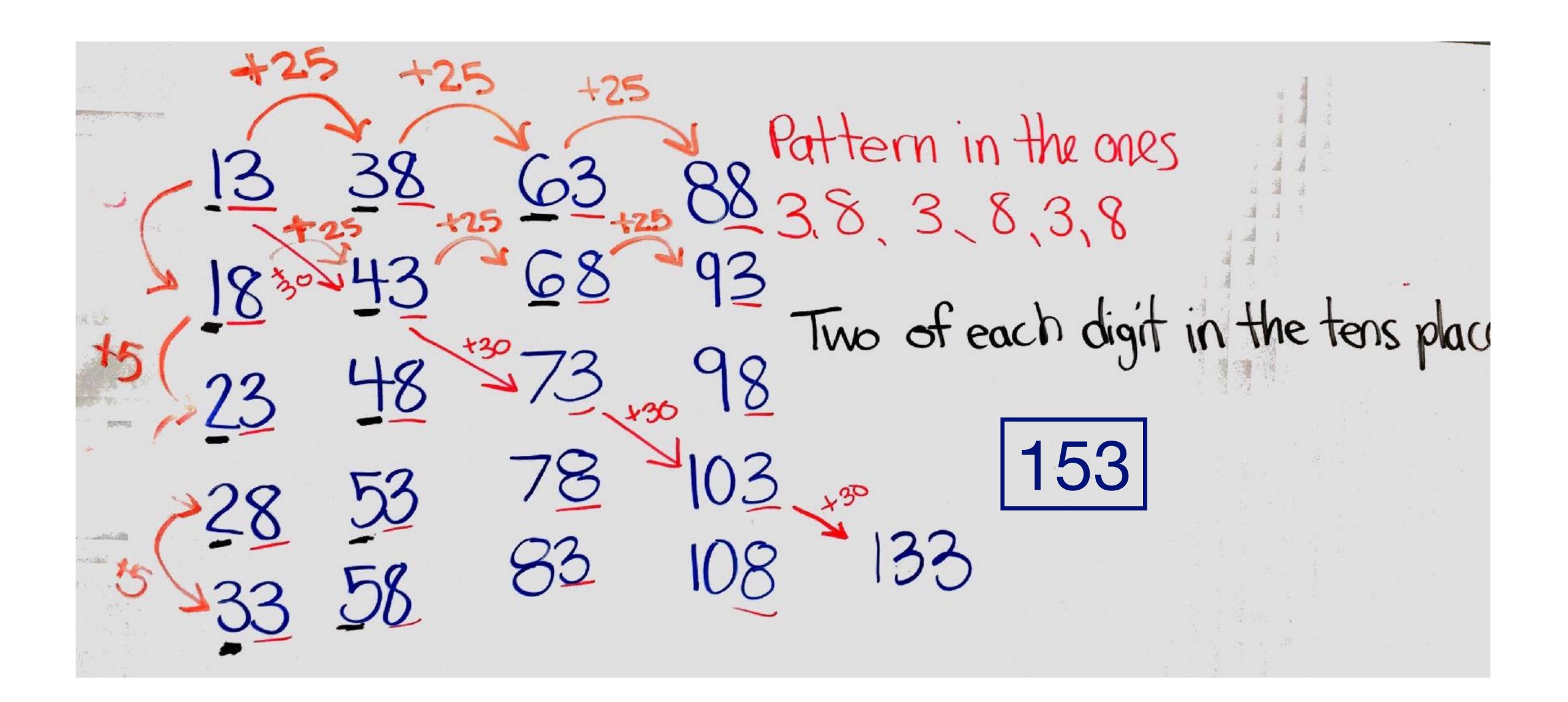
Counting [Forward] by [5s] Starting at [13]

13	38	63	88
18	43	68	93
23	48	73	98
28	53	78	103
33	58	83	108



Counting [Forward] by [5s] Starting at [13]

13	38	63	88
18	43	68	93
23	48	73	98
28	53	78	103
33	58	83	108



"In Choral Counting, students support one another often in the whole-group setting to count, to see relationships and patterns, to build on someone else's idea, and to ask different kinds of questions of the mathematics."

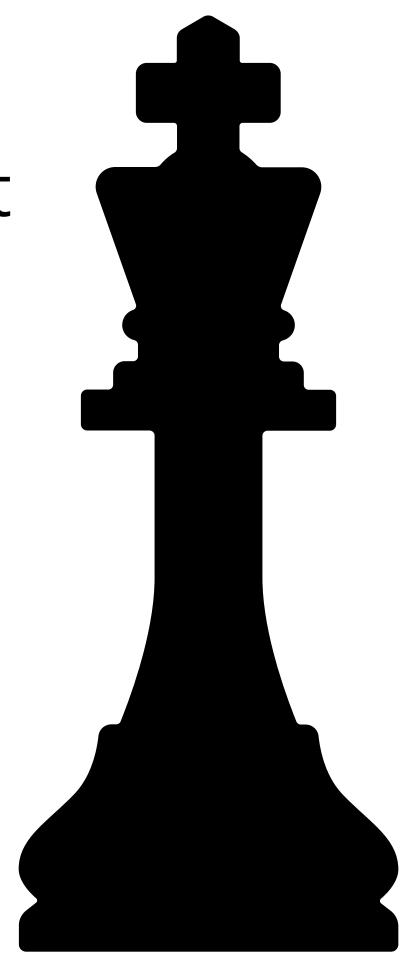
Number Talks

"Simply defined, number talks are five- to fifteen-minute classroom conversations around **purposely crafted computation** problems that are solved mentally."

56 - 29

Subtraction Strategies

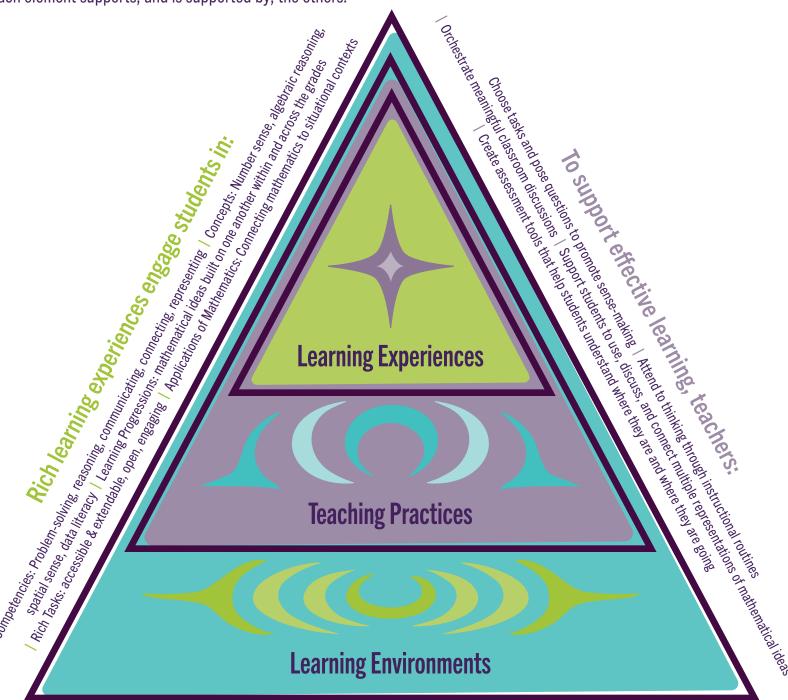
- 1. Round the subtrahend to a multiple of ten and adjust
- 2. Decompose the subtrahend
- 3. Add instead
- 4. Same difference
- 5. Break apart by place



Numeracy Framework K-12 Surrey Schools LEADERSHIP IN LEARNING



The nested nature of the triangles in this diagram communicates that the three elements of Surrey Schools' Numeracy Framework—rich learning experiences, effective teaching practices, and inclusive learning environments—are interwoven. Each element supports, and is supported by, the others.



An inclusive learning environment is one in which learners demonstrate:

Acceptance, respect, and support for each other | Willingness to work together | Reliance on and responsibility for others' learning A view of themselves as mathematicians | Confidence and persistence in problem-solving Appreciation for diverse voices, cultures, and lived experiences

Shaping Rich Learning Experiences

- Aim to develop students' abilities to engage in mathematical competencies as well as their
- Encourage students to see math as a coherent connected whole
- Draw on the knowledge, experience, and background of students
- Allow all students to participate in and benefit from carefully chosen problems, tasks, and activities

Implementing Effective Teaching Practices

- Engage students in sense-making through the active doing of mathematics
- Provide opportunities for collaboration, communication, and reflection
- Develop procedural fluency through conceptual understanding
- Promote a positive disposition in mathematics
- Gather and analyze evidence to determine next steps in student learning

Building Inclusive Learning Environments

- Create classroom communities in which all learners belong
- Recognize that learning is closely tied to students' identities
- Inspire students to see mathematics as joyful, playful, creative and collaborative
- Make explicit connections to Indigenous ways of knowing and being

Acceptance, respect, and support for each other | Willingness to work together | Reliance on and responsibility for others' learning | A view of themselves as mathematicians | Confidence and persistence in problem-solving | Appreciation for diverse voices, cultures, and lived experiences

The include to a continue of the continue of the term will be a continued and the continue of the continue of

Shaping Rich Learning Experiences

- Aim to develop students' abilities
 to engage in mathematical
 competencies as well as their
 understanding of mathematical content
- Encourage students to see math as a coherent connected whole
- Draw on the knowledge, experience, and background of students
- Allow all students to participate in and benefit from carefully chosen problems, tasks, and activities

Implementing Effective Teaching Practices

- Engage students in sense-making through the active doing of mathematics
- Provide opportunities for collaboration, communication, and reflection
- Develop procedural fluency through conceptual understanding
- Promote a positive disposition in mathematics
- Gather and analyze evidence to determine next steps in student learning

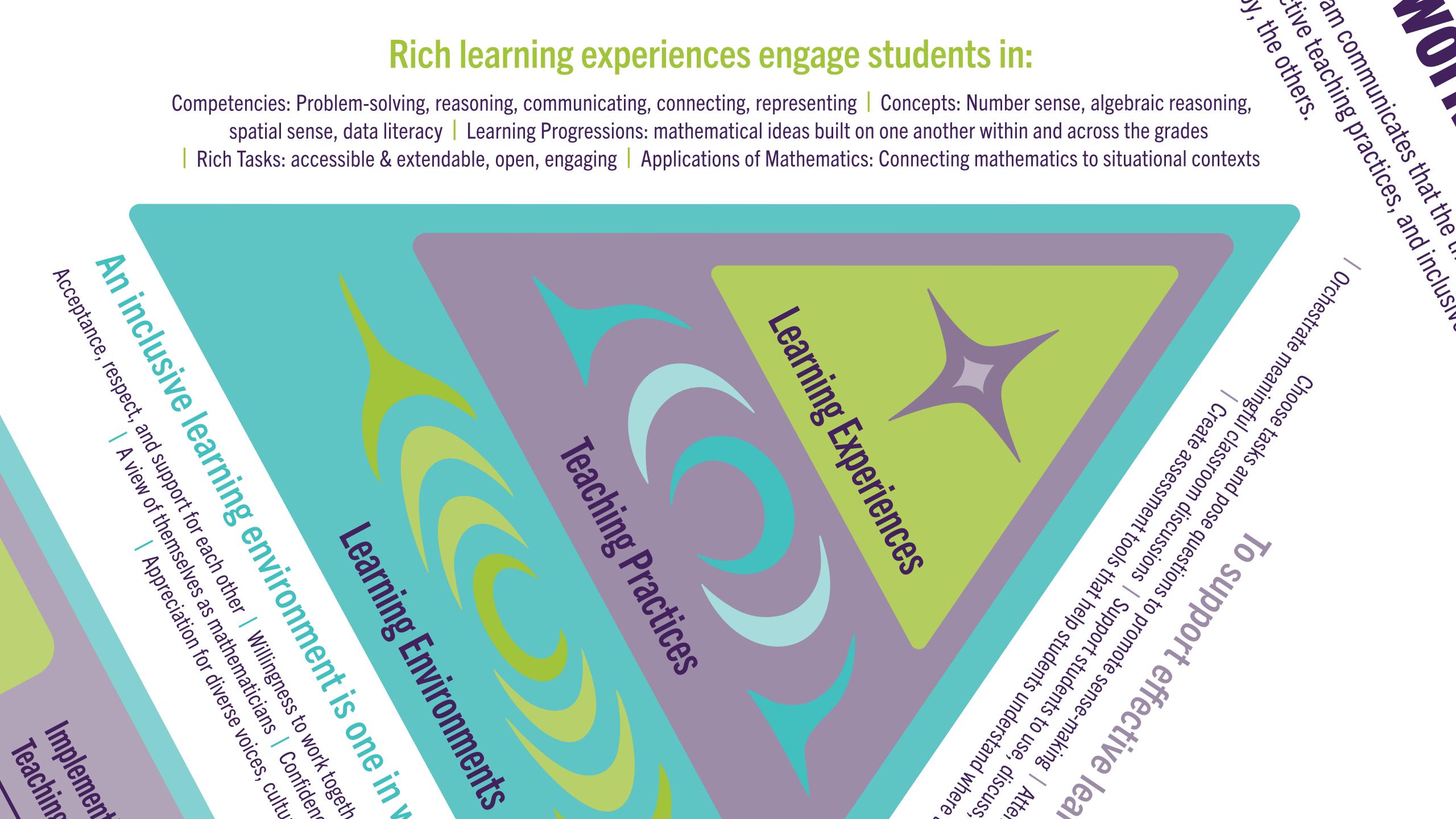
Building Inclusive Learning Environments

- Create classroom communities in which all learners belong
- Recognize that learning is closely tied to students' identities
- Inspire students to see mathematics as joyful, playful, creative and collaborative
- Make explicit connections to Indigenous ways of knowing and being

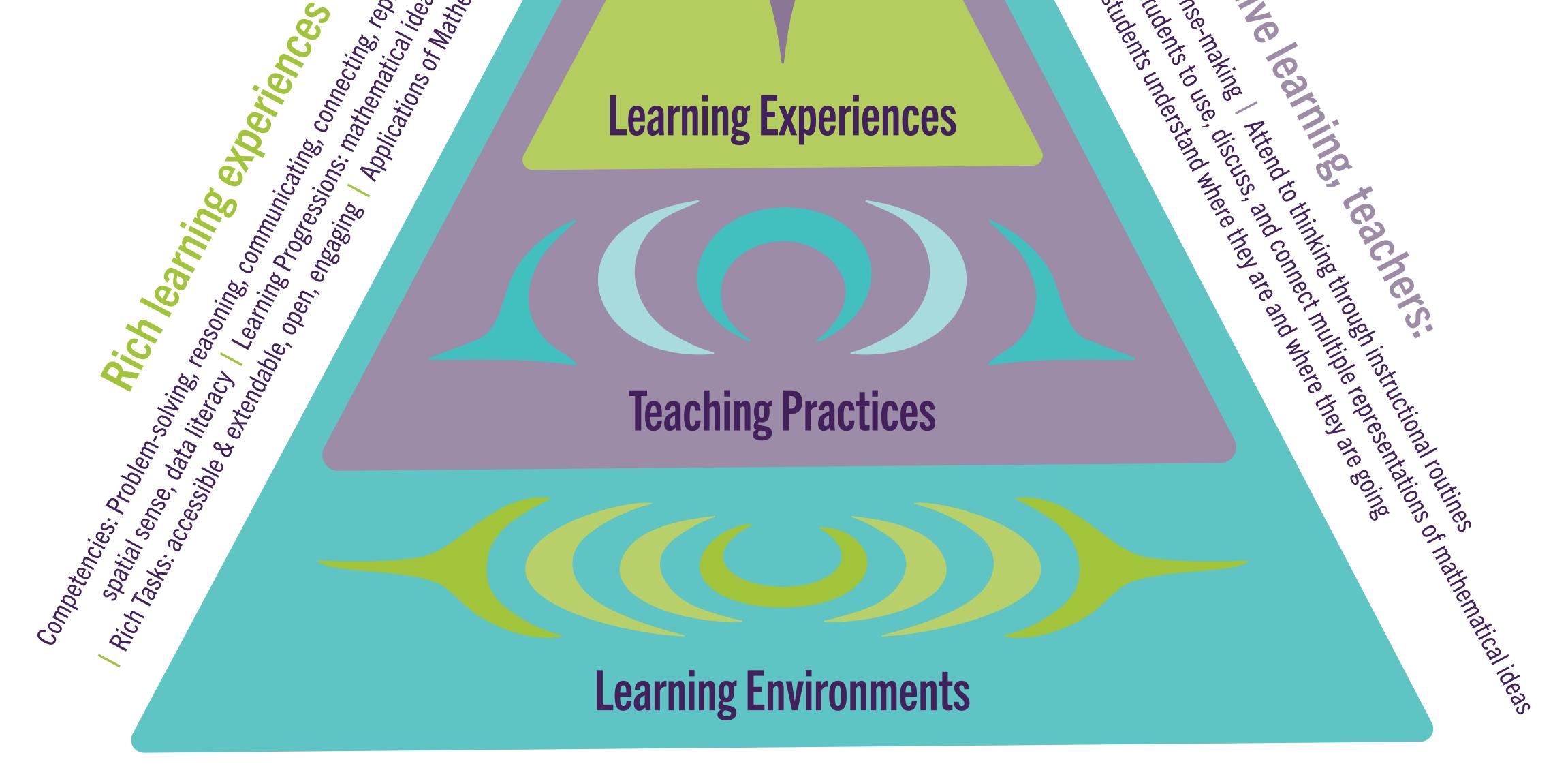
We are deeply grateful to artist Elinor Atkins from the qwa:n\u00e4'\u00e4n (Kwantlen) and N\u00e4e?kepmx (Shakan) First Nations for her artistic vision and expression of geometric Coast Salish designs. With trigons, circles, ovals, and crescents, Coast Salish design elements shape the Morning Star and the all-seeing Coast Salish Eyes of this land. In their harmony, we are reminded of the beauty of connection and the wisdom of place.

Rich learning experiences engage students in:

y, the others. Competencies: Problem-solving, reasoning, communicating, connecting, representing | Concepts: Number sense, algebraic reasoning, spatial sense, data literacy | Learning Progressions: mathematical ideas built on one another within and across the grades Rich Tasks: accessible & extendable, open, engaging | Applications of Mathematics: Connecting mathematics to situational contexts



L'ESTITUTE MACTICOS, AND INCHESIN To support effective learning, teachers: Choose tasks and pose questions to promote sense-making | Attend to thinking through instructional routines Orchestrate meaningful classroom discussions | Support students to use, discuss, and connect multiple representations of mathematical ideas Create assessment tools that help students understand where they are and where they are going Inment is one in which learners demonstrate. SHORIDO BUDIRINIS OF SHEMBURDING GOM IN SHORIDO STORE OF SHORIDO SHORIDO SHORIDO HOUR HARM SHORIS OF SHEMBURDING HOURS H Willipeness to work together / Reliance on and responsibility for others' learning e others. SHOO BIOHENIS OF SOIFFINGHEN ON THE SHOOL OF STANDARD Learning Experiences Edition of the same of the sam Learning Environments 500



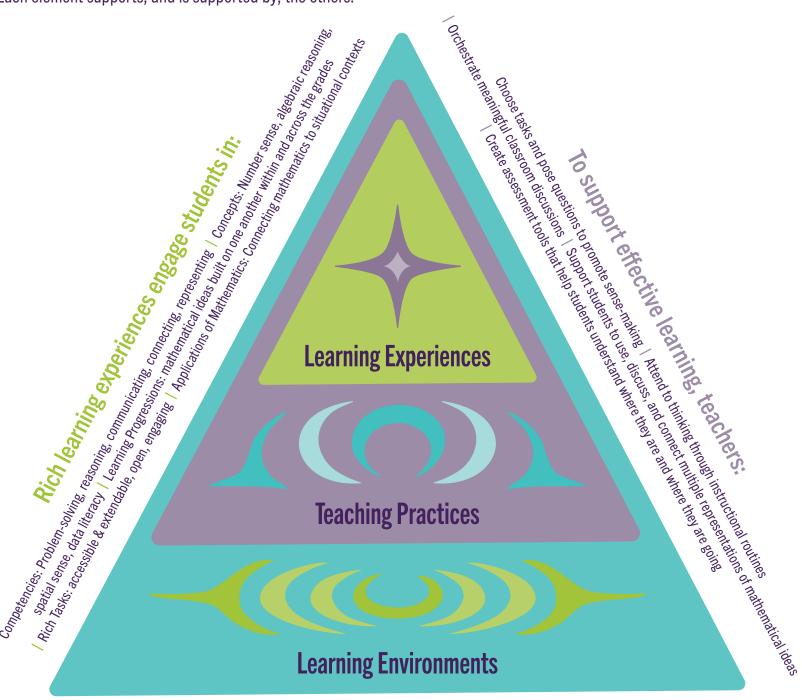
An inclusive learning environment is one in which learners demonstrate:

Acceptance, respect, and support for each other | Willingness to work together | Reliance on and responsibility for others' learning | A view of themselves as mathematicians | Confidence and persistence in problem-solving | Appreciation for diverse voices, cultures, and lived experiences

Numeracy Framework K-12 Surrey Schools LEADERSHIP IN LEARNING



The nested nature of the triangles in this diagram communicates that the three elements of Surrey Schools' Numeracy Framework—rich learning experiences, effective teaching practices, and inclusive learning environments—are interwoven. Each element supports, and is supported by, the others.



An inclusive learning environment is one in which learners demonstrate:

Acceptance, respect, and support for each other | Willingness to work together | Reliance on and responsibility for others' learning A view of themselves as mathematicians | Confidence and persistence in problem-solving Appreciation for diverse voices, cultures, and lived experiences

Shaping Rich Learning Experiences

- Aim to develop students' abilities to engage in mathematical competencies as well as their
- Encourage students to see math as a coherent connected whole
- Draw on the knowledge, experience, and background of students
- Allow all students to participate in and benefit from carefully chosen problems, tasks, and activities

Implementing Effective Teaching Practices

- Engage students in sense-making through the active doing of mathematics
- Provide opportunities for collaboration, communication, and reflection
- Develop procedural fluency through conceptual understanding
- Promote a positive disposition in mathematics
- Gather and analyze evidence to determine next steps in student learning

Building Inclusive Learning Environments

- Create classroom communities in which all learners belong
- Recognize that learning is closely tied to students' identities
- Inspire students to see mathematics as joyful, playful, creative and collaborative
- Make explicit connections to Indigenous ways of knowing and being



Strategies: How You Mess with the Numbers **Models:** How You Show Your Thinking

		Strategies - How You Mess with the Numbers					
		Remove to a Friendly Number	Remove a Friendly Number	Remove a Friendly Number - Over	Find the Distance (Difference)	Constant Difference (Equivalent Difference)	
Models - How You Show Your Thinking	Splitting	56 - 29 $56 6 23$ $50 20$ $30 - 3 = 27$	$56 - 29$ $56 \ 20 \ 9$ $36 \ 9$ 6 $30 - 3 = 27$				
	Equations	56 - 29 $= 56 - 6 - 23$ $= 50 - 23$ $= 50 - 20 - 3$ $= 30 - 3$ $= 27$	56 - 29 $= 56 - 20 - 9$ $= 36 - 9$ $= 36 - 6 - 3$ $= 30 - 3$ $= 27$	56 - 29 $56 - 30 = 26$ $26 + 1 = 27$ $56 - 29$ $= 56 - (30 - 1)$ $= (56 - 30) + 1$ $= 26 + 1$ $= 27$	29 + 1 = 30 $30 + 20 = 50$ $50 + 6 = 56$ $1 + 20 + 6 = 27$	56 - 29 +1 +1 57 - 30 = 27 $56 + 1 = 57 -29 + 1 = -30 27$	
SW .	Open Number Line	3 20 6 27 30 50 56	3 6 20 27 30 36 56	1 30 1 56	20 + 1+6 = 27 29 4950 56	27 11 2930 5657	

1. Round the subtrahend to a multiple of ten and adjust

$$56-29$$

$$= 56-6-23$$

$$= 50-23$$

$$= 50-20-3$$

$$= 30-3$$

$$= 27$$

$$56 - 29$$

$$= 56 - 20 - 9$$

$$= 36 - 9$$

$$= 36 - 6 - 3$$

$$= 30 - 3$$

$$= 27$$

$$56 - 29$$
 $56 - 30 = 26$
 $26 + 1 = 27$

$$56 - 29$$

$$= 56 - (30 - 1)$$

$$= (56 - 30) + 1$$

$$= 26 + 1$$

$$= 27$$

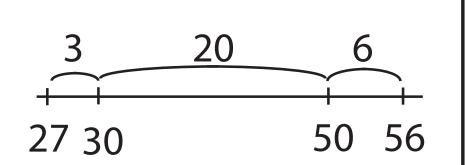
$$29 + 1 = 30$$
 $30 + 20 = 50$
 $50 + 6 = 56$
 $1 + 20 + 6 = 27$

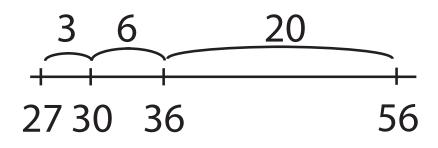
$$56 - 29$$
 $+ 1 + 1$
 $57 - 30 = 27$

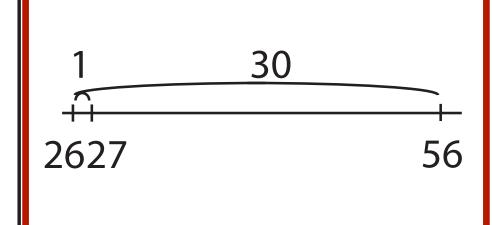
$$56 + 1 = 57$$

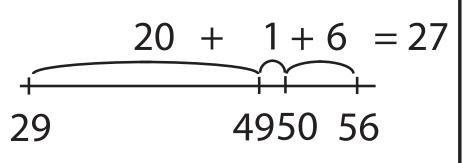
$$-29 + 1 = -30$$

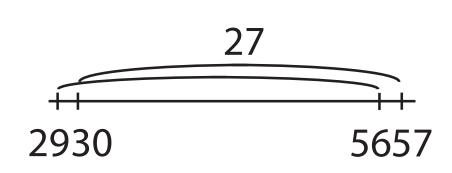
$$27$$











2. Decompose the subtrahend

$$56 - 29$$

$$= 56 - 6 - 23$$

$$= 50 - 23$$

$$= 50 - 20 - 3$$

$$= 30 - 3$$

$$= 27$$

$$56 - 29$$

$$= 56 - 20 - 9$$

$$= 36 - 9$$

$$= 36 - 6 - 3$$

$$= 30 - 3$$

$$= 27$$

$$56 - 29$$
 $56 - 30 = 26$
 $26 + 1 = 27$
 $56 - 29$

$$56 - 29$$

$$= 56 - (30 - 1)$$

$$= (56 - 30) + 1$$

$$= 26 + 1$$

$$= 27$$

$$29 + 1 = 30$$
 $30 + 20 = 50$
 $50 + 6 = 56$

1 + 20 + 6 = 27

$$56 + 1 = 57$$

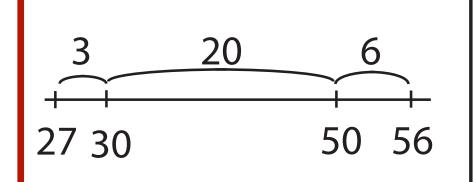
$$-29 + 1 = -30$$

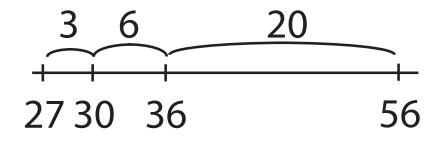
$$27$$

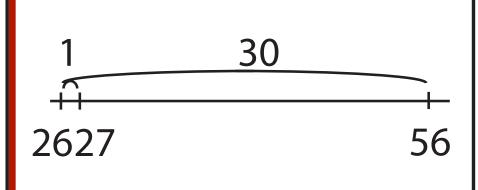
56 - 29

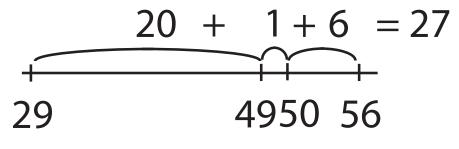
+1 +1

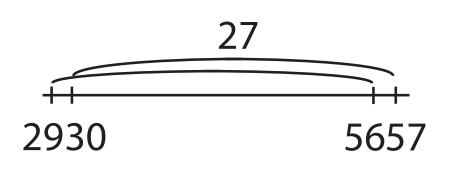
57 - 30 = 27











3. Add instead

$$56 - 29$$

$$= 56 - 6 - 23$$

$$= 50 - 23$$

$$= 50 - 20 - 3$$

$$= 30 - 3$$

$$= 27$$

$$56 - 29$$

$$= 56 - 20 - 9$$

$$= 36 - 9$$

$$= 36 - 6 - 3$$

$$= 30 - 3$$

$$= 27$$

$$56 - 29$$
 $56 - 30 = 26$
 $26 + 1 = 27$

$$56-29$$

$$= 56-(30-1)$$

$$= (56-30)+1$$

$$= 26+1$$

$$= 27$$

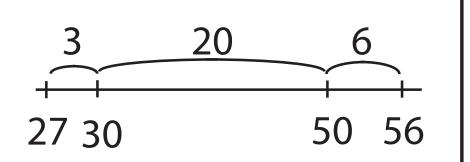
$$29 + 1 = 30$$
 $30 + 20 = 50$
 $50 + 6 = 56$
 $1 + 20 + 6 = 27$

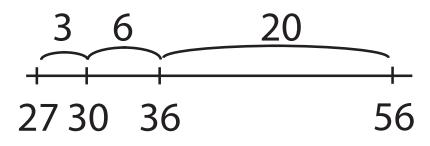
$$56 - 29$$
 $+ 1 + 1$
 $57 - 30 = 27$

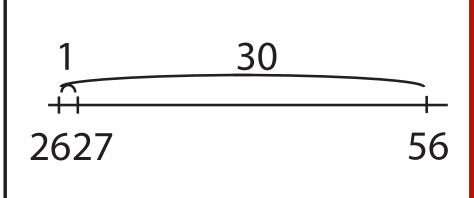
$$56 + 1 = 57$$

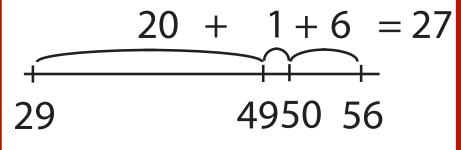
$$-29 + 1 = -30$$

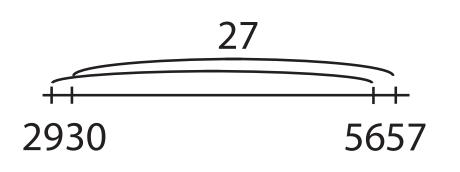
$$27$$











4. Same difference

$$56 - 29$$

$$= 56 - 20 - 9$$

$$= 36 - 9$$

$$= 36 - 6 - 3$$

$$= 30 - 3$$

$$= 27$$

$$56 - 29$$

 $56 - 30 = 26$
 $26 + 1 = 27$
 $56 - 29$
 $= 56 - (30 - 1)$
 $= (56 - 30) + 1$

= 26 + 1

= 27

$$29 + 1 = 30$$

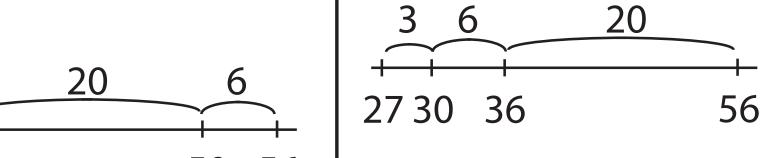
 $30 + 20 = 50$
 $50 + 6 = 56$
 $1 + 20 + 6 = 27$

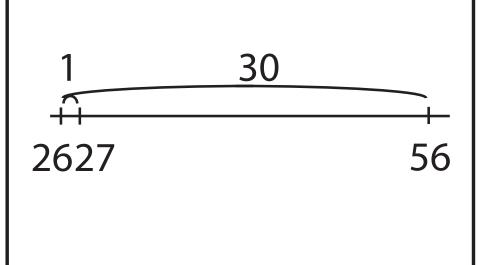
$$56 - 29$$
 $+ 1 + 1$
 $57 - 30 = 27$

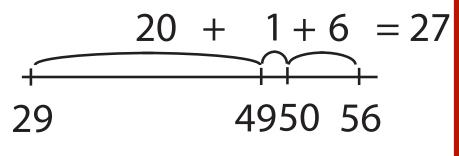
$$56 + 1 = 57$$

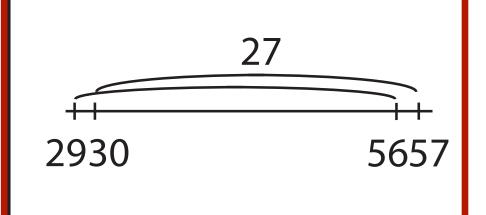
$$-29 + 1 = -30$$

$$27$$







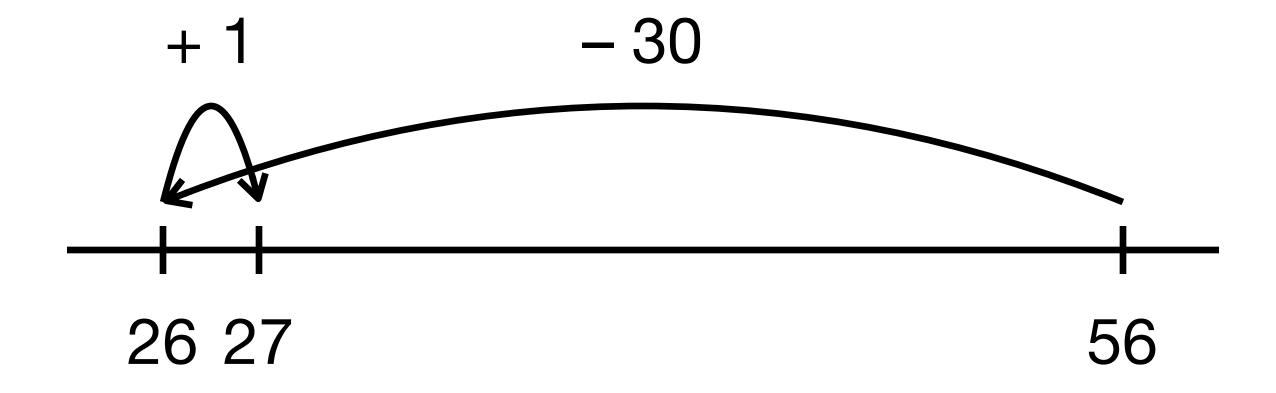


Number Strings

"Simply defined, number talks are five- to fifteen-minute classroom conversations around **purposely crafted computation** problems that are solved mentally."

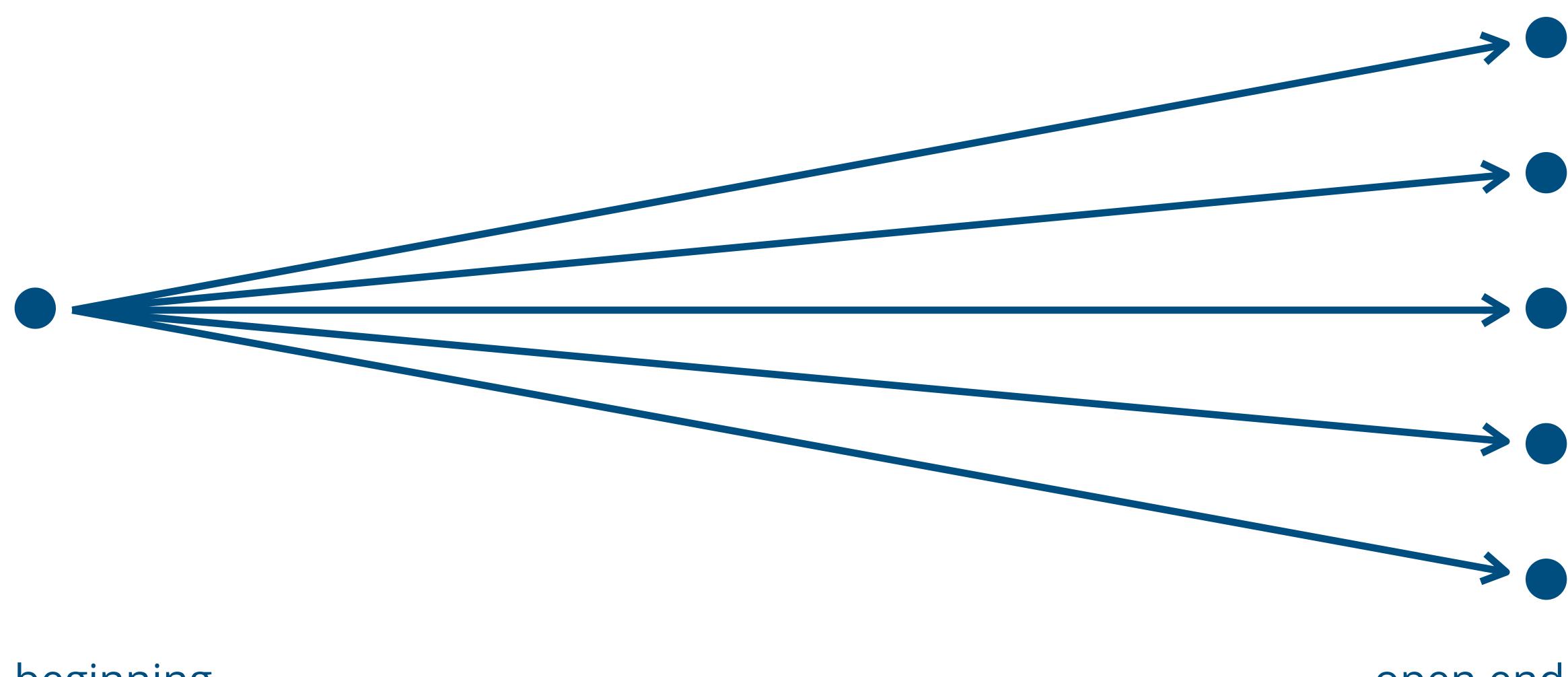
56 - 29

```
23 - 10
```



Open Middle

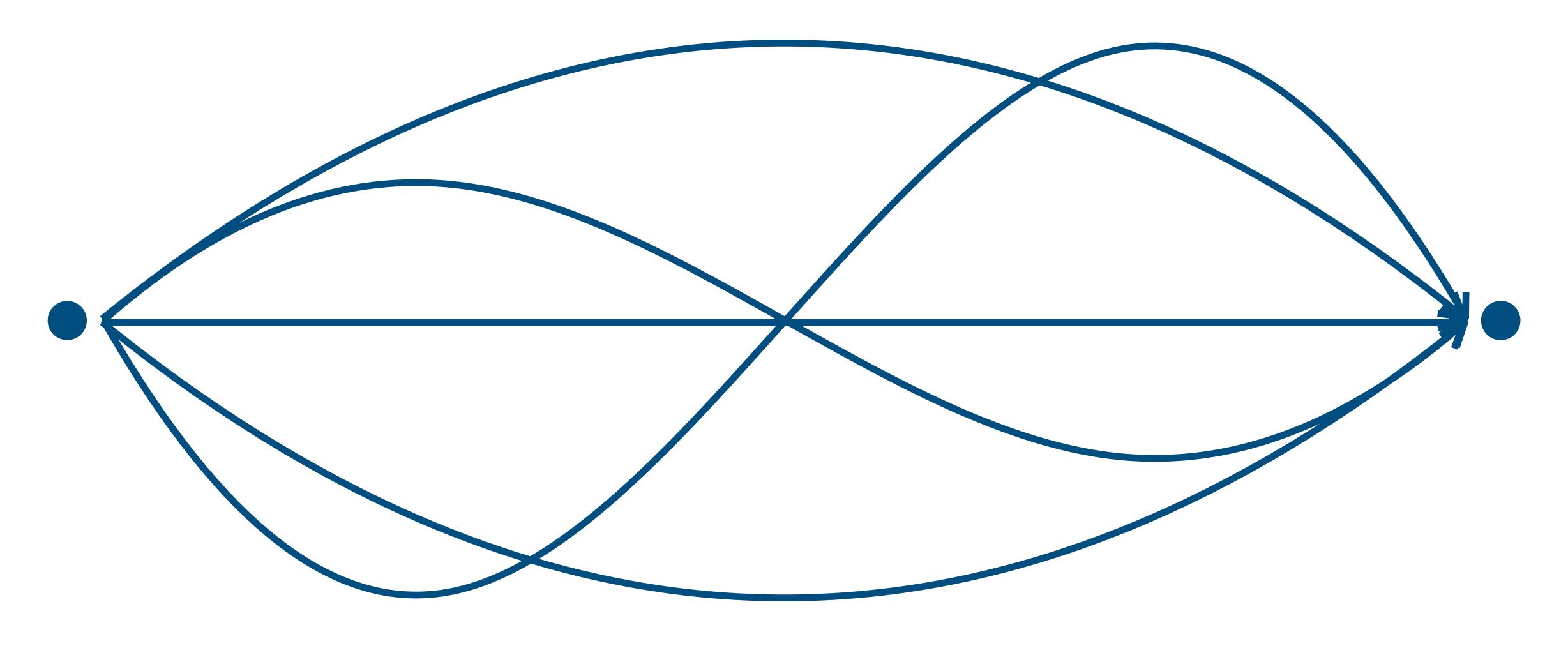




beginning

open end

Meyer, D. (2014). Video games and making math more like things students like. [Video]



beginning

open middle

closed end



0. + 0.

 1
 2
 3
 4
 5
 6
 7
 8
 9



5 6 7 8 9

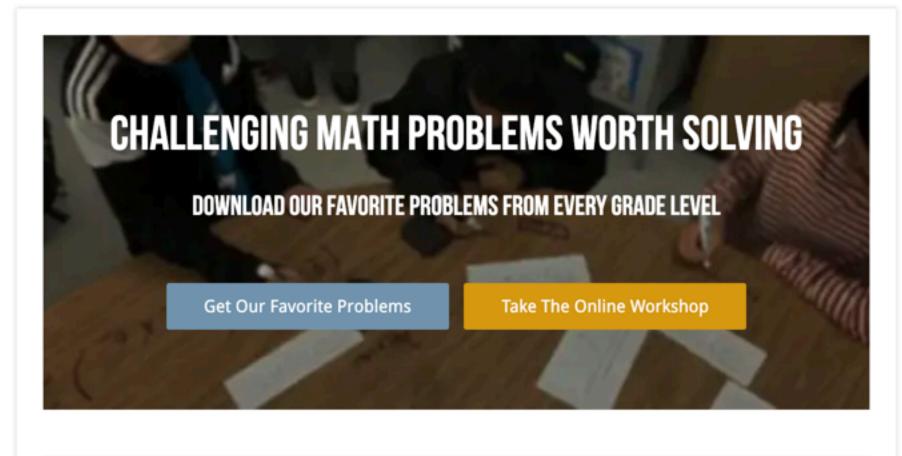
"I came to understand that when I asked students superficial questions, I got superficial information back about what they knew."

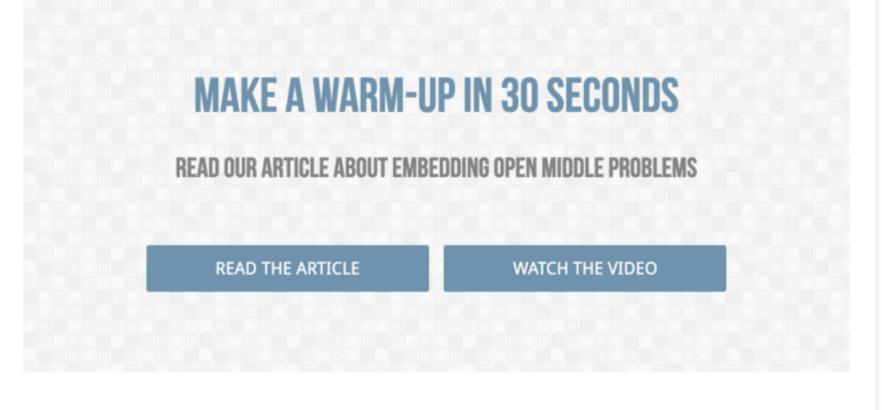


Take The Online Workshop

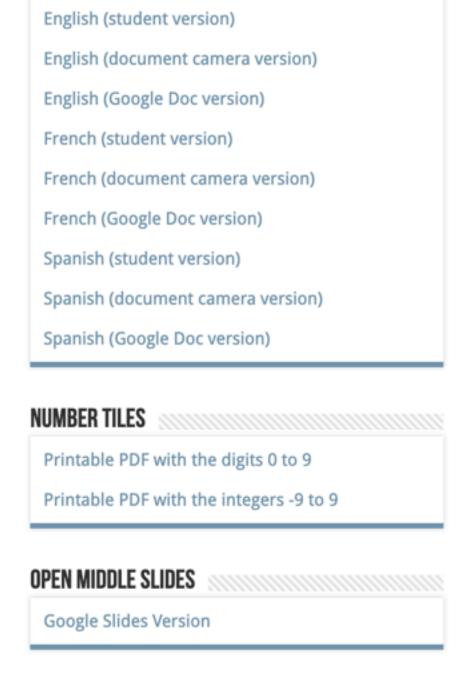
Q

Home Kinder ▼ 1st Gr ▼ 2nd Gr ▼ 3rd Gr ▼ 4th Gr ▼ 5th Gr ▼ 6th Gr ▼ 7th Gr ▼ 8th Gr ▼ High School ▼ About ▼ Submit 🕮 English ▼





I NOKING END AN ODEN MIDDI E BOOK?



Search

OPEN MIDDLE STICKERS

Get an Open Middle sticker

OPEN MIDDLE WORKSHEET

Wanted Number

Wanted Number

It is a 2-digit number. It is an odd number. It is less than 40. The number contains one prime digit. It is a number with no repeating digits. An even number is in the 10s place. It is a prime number. Its digits add up to 11. It is a number between 25 and 30.

Which One Doesn't Belong?

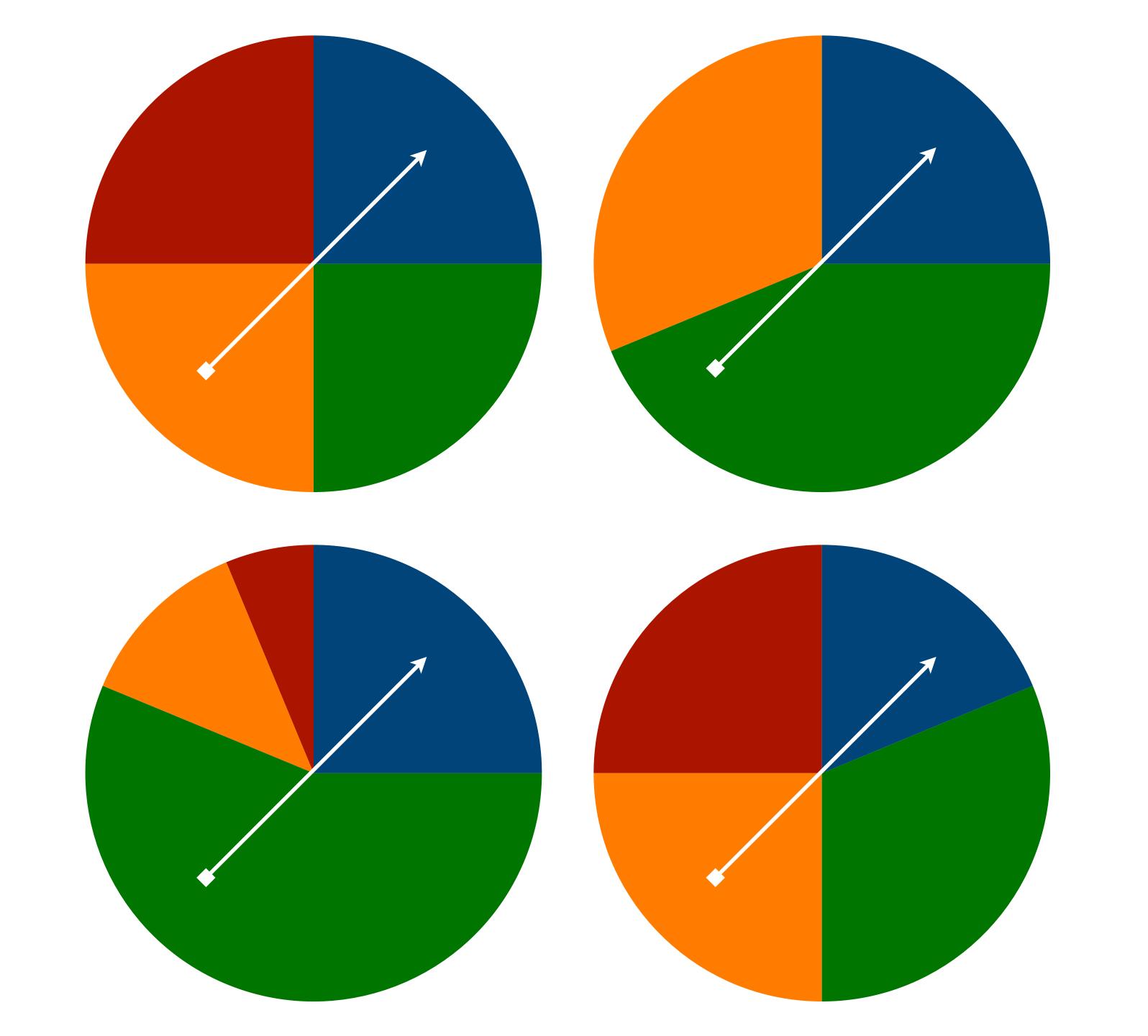
does not belong because...

What makes ____ different from the others is...

Only has

All have except





5, 8, 11, 14, ...

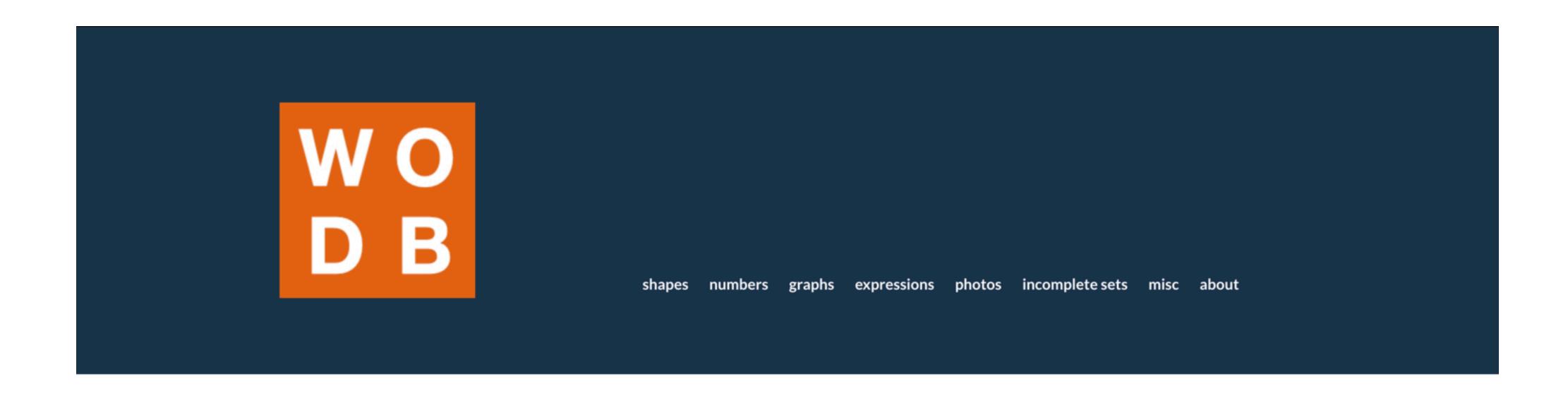
4, 7, 10, 13, ...

5, 9, 13, 17, ...

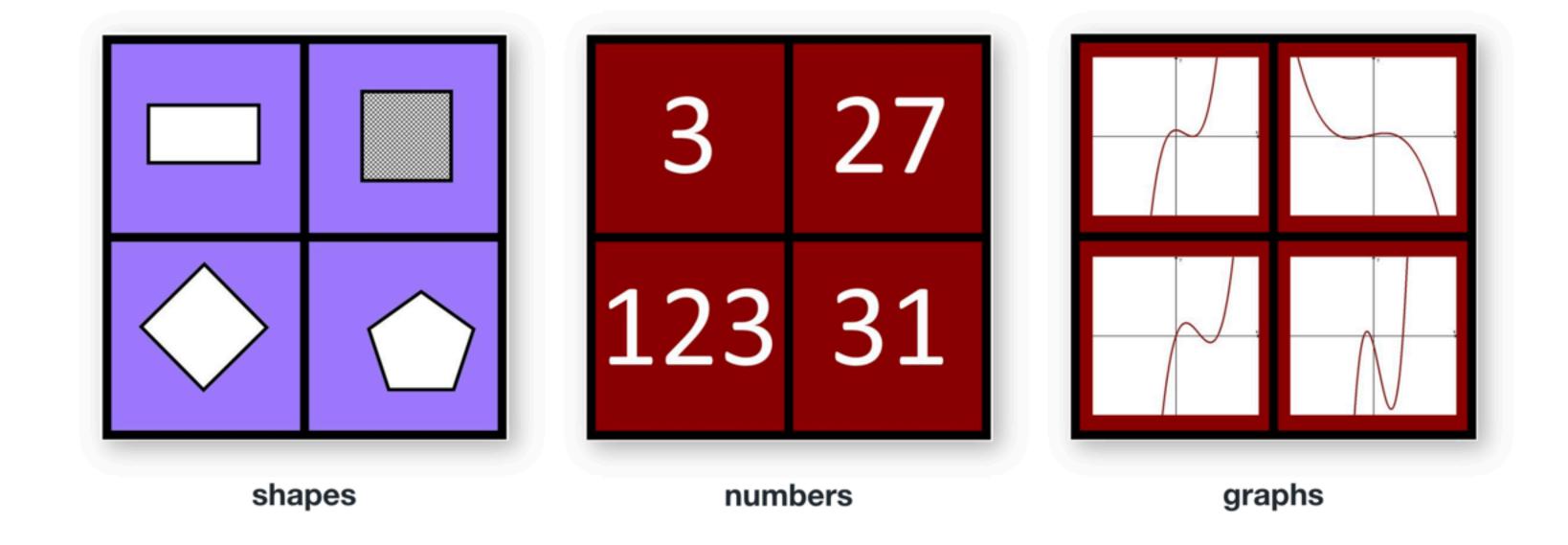
"All choices are correct, which shifts the focus to justification. Which One Doesn't Belong? isn't about guessing the right answer; it's about expressing mathematical relationships precisely in order to communicate with others."

"When children look for sameness and difference; when they work hard to put their ideas into words; when they evaluate whether somebody else's justification makes sense; when they wonder What if [...]?—in all these cases, children engage in real mathematical thinking."

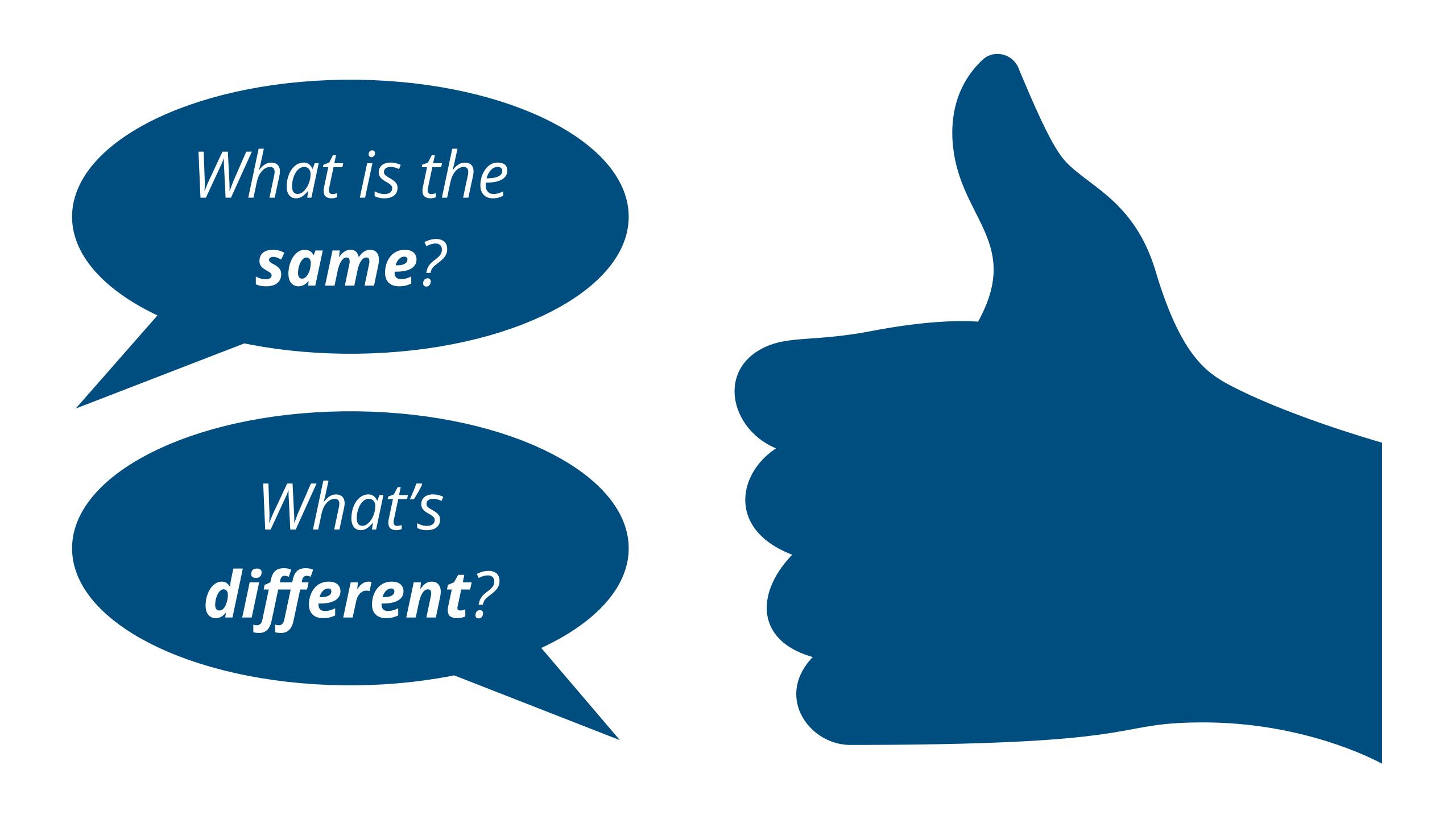
"The use of sentence frames was critical to support students who are feeling anxious about what to say, as well as students who have difficulty getting started. They also support students who have challenges with social cues. [...] A sentence frame can give permission to get started, and help students know that they are on the right track."

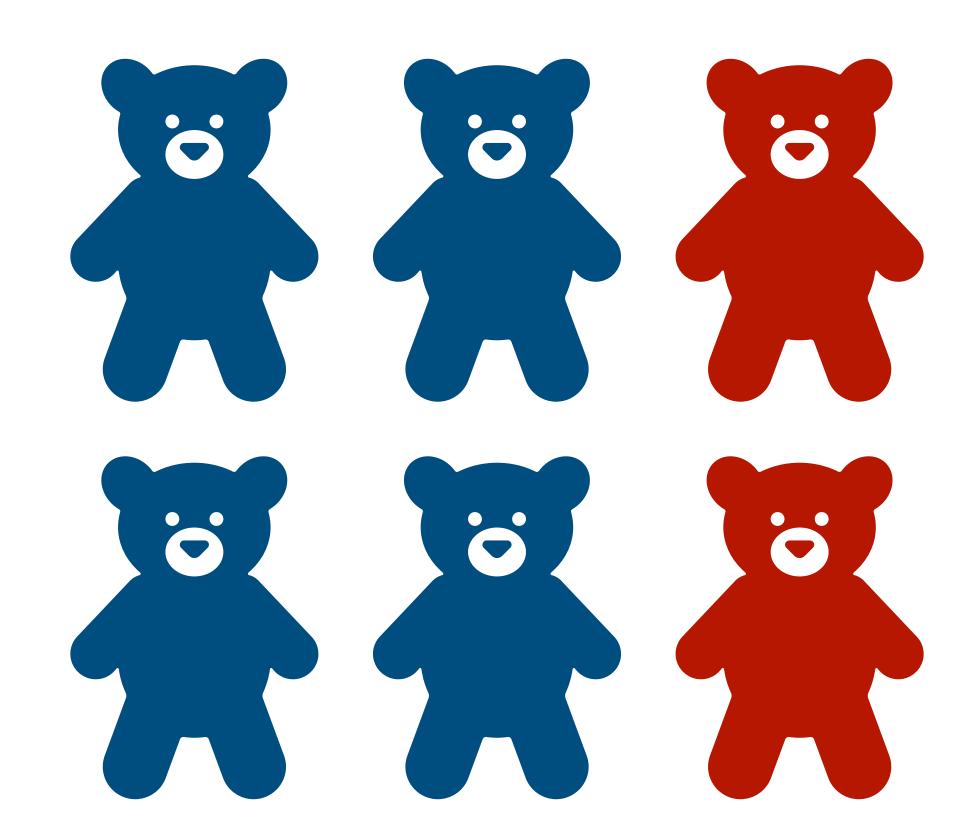


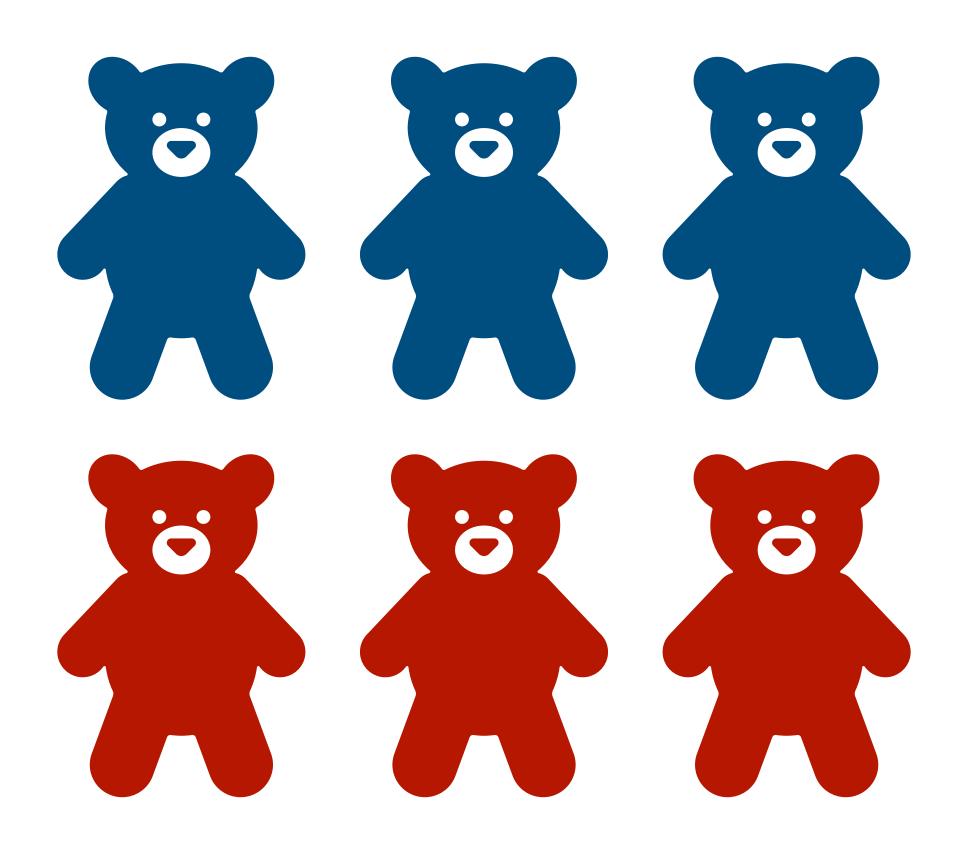
Which One Doesn't Belong?

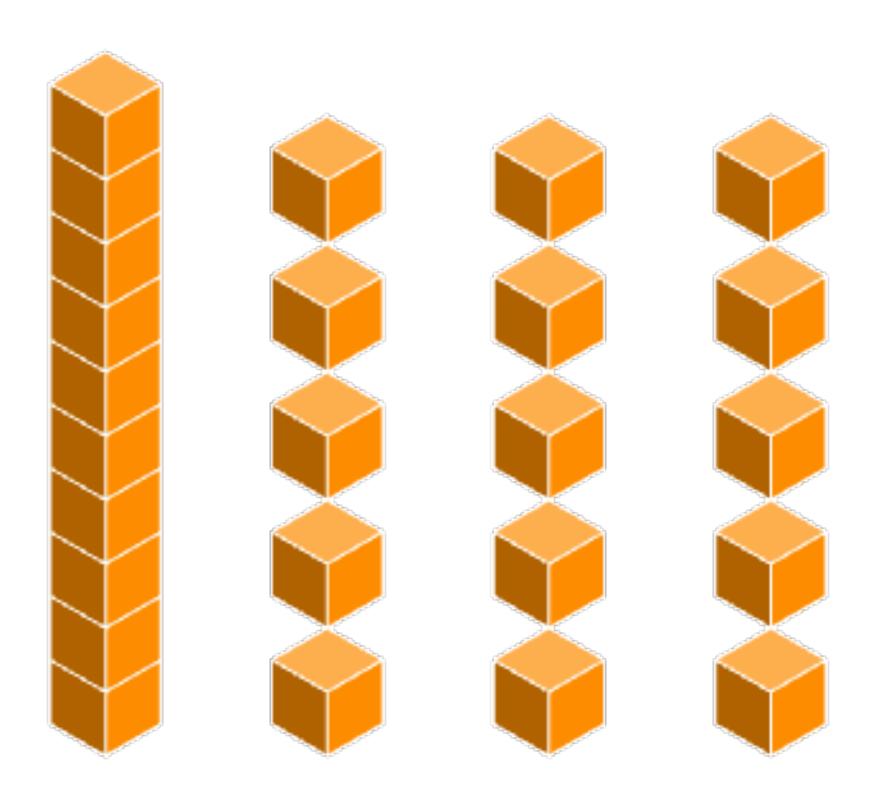


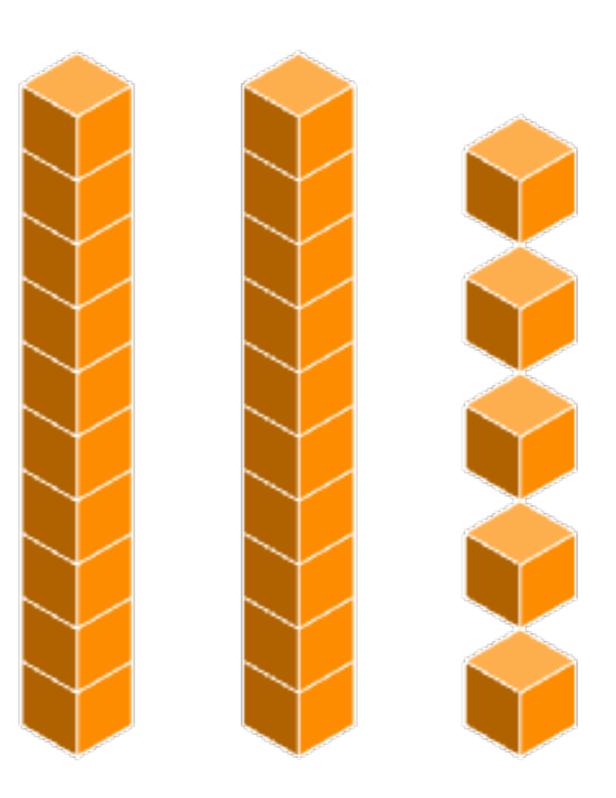
Same and Different

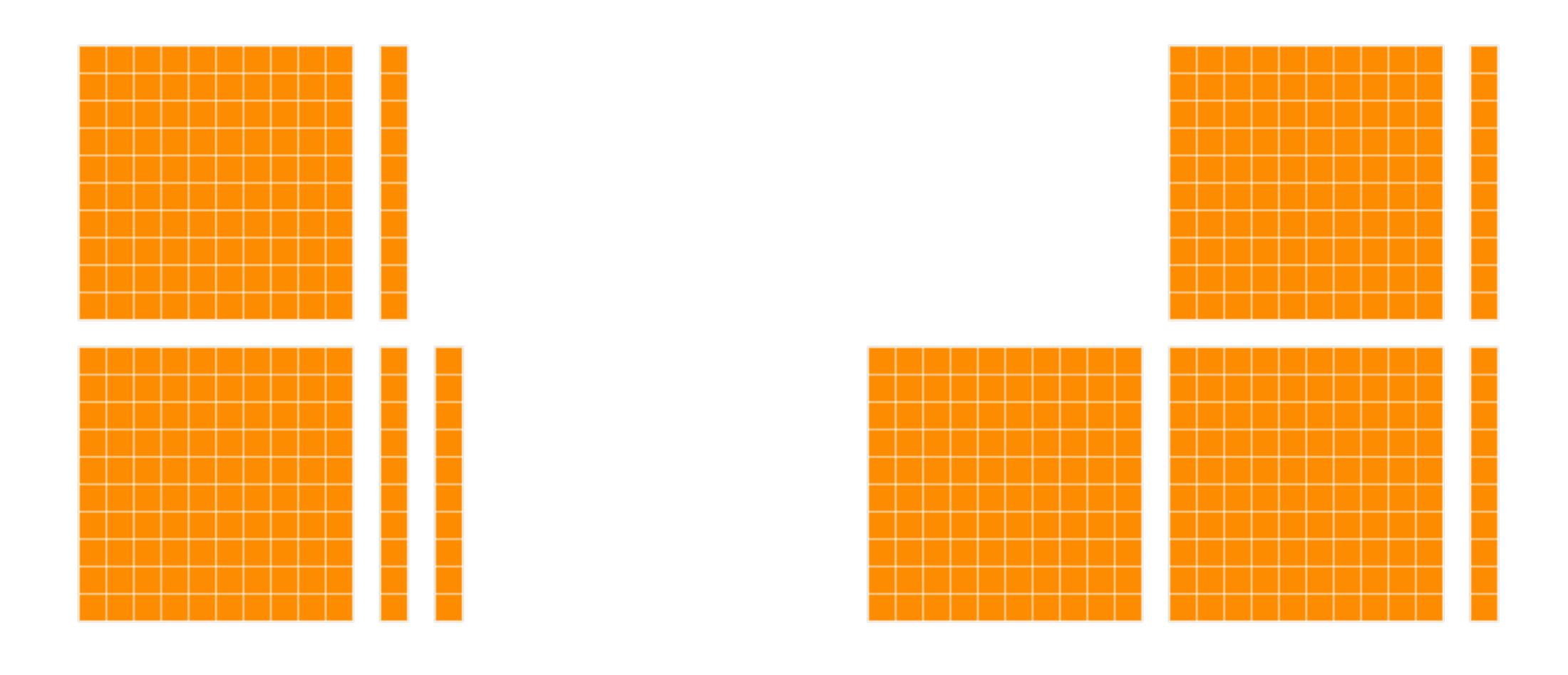




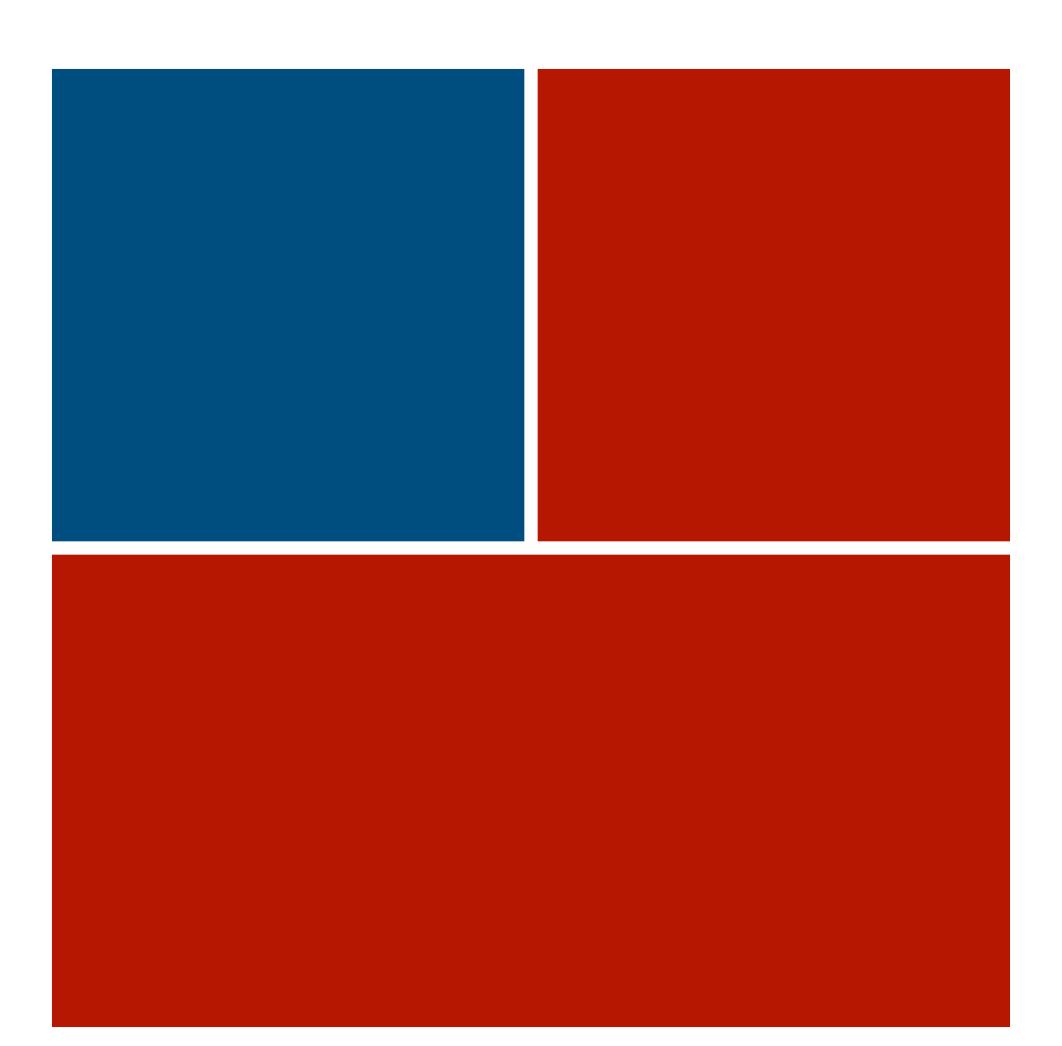


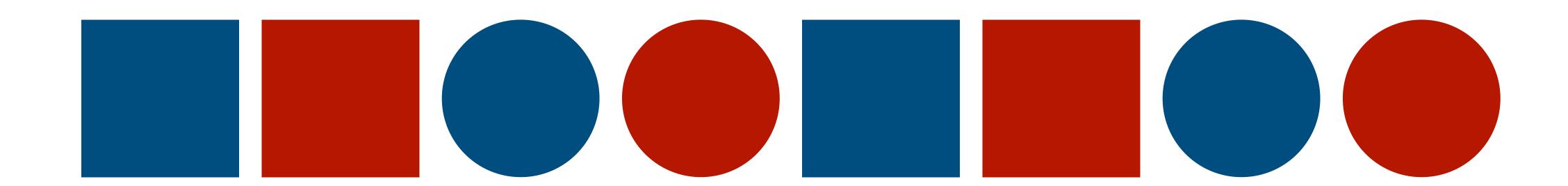


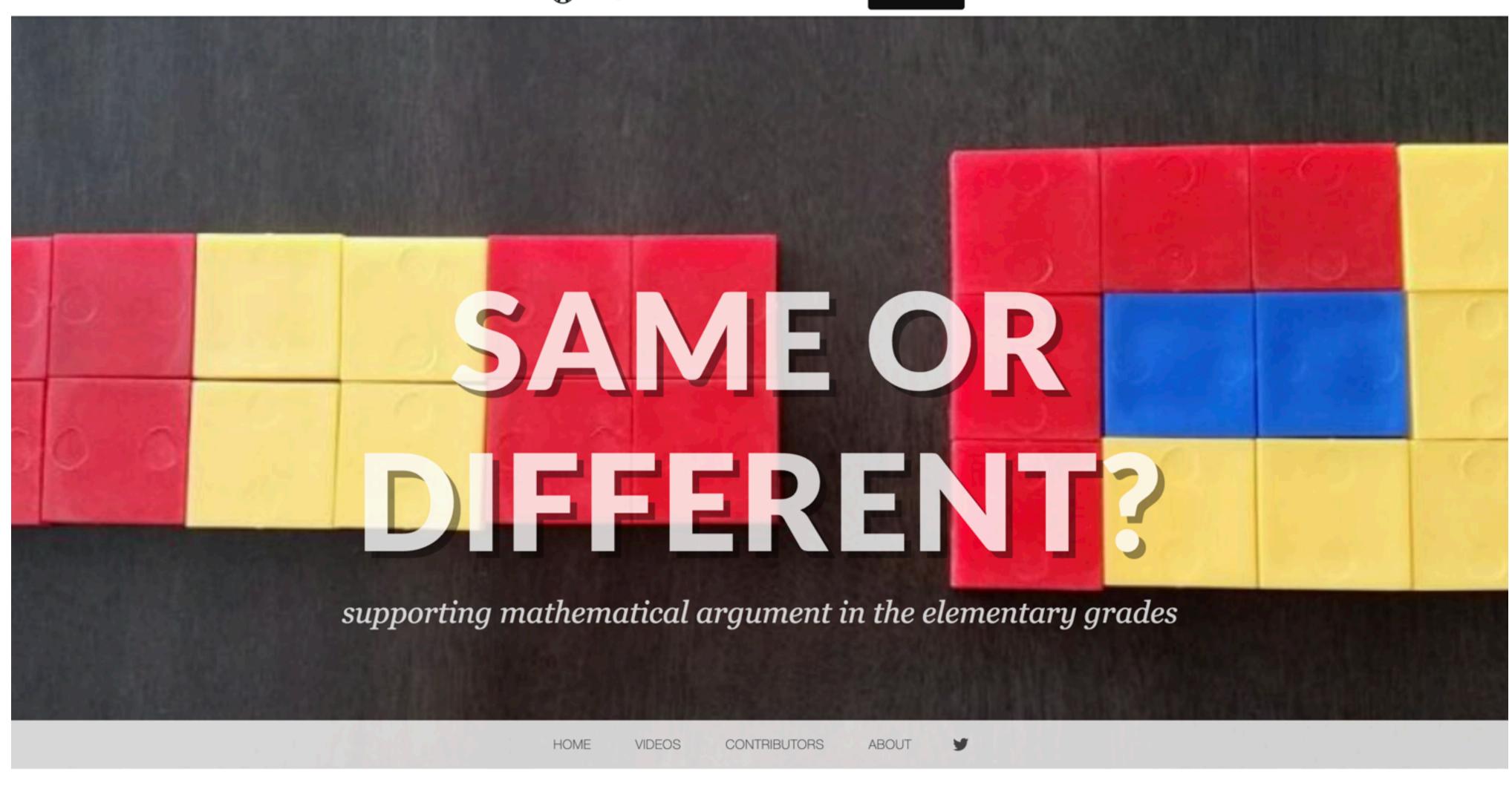












WELCOME!



Developing Grayscale Thinking

ABOUT EARLY NUMERACY ADDITION/SUBTRACTION MULTIPLICATION/DIVISION MEASUREMENT PLACE VALUE FRACTIONS, RATIOS, ETC. GEOMETRY ALGEBRA HIGH SCHOOL T-SHIRTS

Same But Different™ is a powerful routine for use in math classrooms. The images on this website can be used for teaching a way of thinking: grayscale thinking, categorical thinking; helping students to build a network of ideas and an approach for learning and thinking about mathematics.

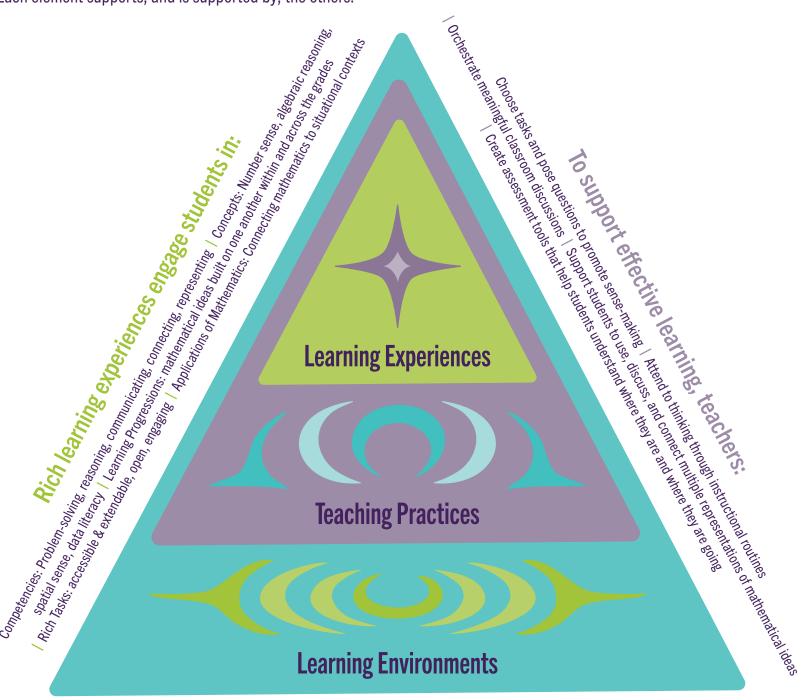
GET FREE STUDENT PAGES

LEARN MORE

Numeracy Framework K-12 Surrey Schools LEADERSHIP IN LEARNING



The nested nature of the triangles in this diagram communicates that the three elements of Surrey Schools' Numeracy Framework—rich learning experiences, effective teaching practices, and inclusive learning environments—are interwoven. Each element supports, and is supported by, the others.



An inclusive learning environment is one in which learners demonstrate:

Acceptance, respect, and support for each other | Willingness to work together | Reliance on and responsibility for others' learning A view of themselves as mathematicians | Confidence and persistence in problem-solving Appreciation for diverse voices, cultures, and lived experiences

Shaping Rich Learning Experiences

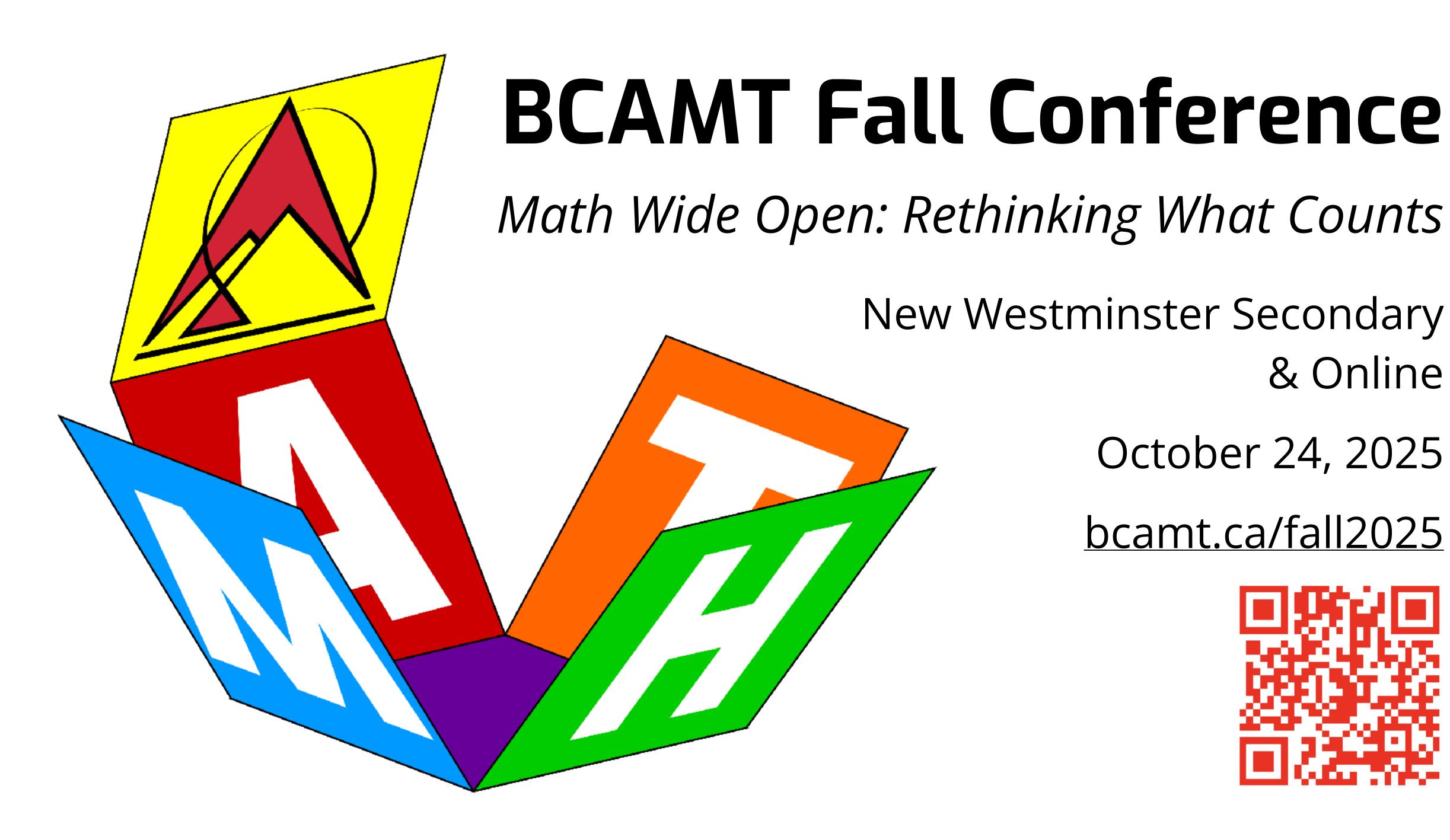
- Aim to develop students' abilities to engage in mathematical competencies as well as their
- Encourage students to see math as a coherent connected whole
- Draw on the knowledge, experience, and background of students
- Allow all students to participate in and benefit from carefully chosen problems, tasks, and activities

Implementing Effective Teaching Practices

- Engage students in sense-making through the active doing of mathematics
- Provide opportunities for collaboration, communication, and reflection
- Develop procedural fluency through conceptual understanding
- Promote a positive disposition in mathematics
- Gather and analyze evidence to determine next steps in student learning

Building Inclusive Learning Environments

- Create classroom communities in which all learners belong
- Recognize that learning is closely tied to students' identities
- Inspire students to see mathematics as joyful, playful, creative and collaborative
- Make explicit connections to Indigenous ways of knowing and being

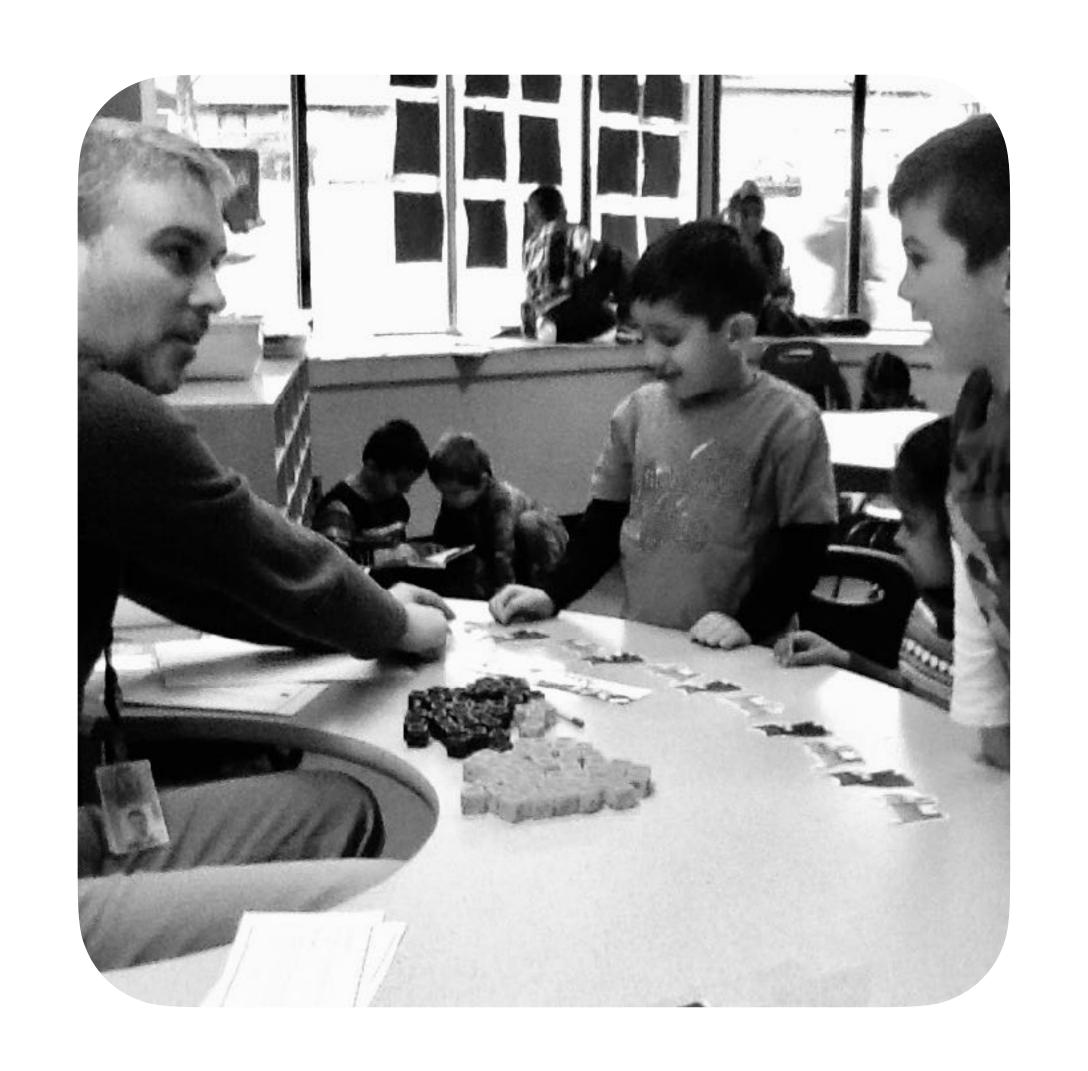


Chris Hunter

K-12 Numeracy Helping Teacher Surrey Schools

email: hunter_c@surreyschools.ca

blog: chrishunter.ca





INTRODUCTION

After a successful spring 2022 professional learning series with Dr. Marian Small, the Coast Metro Consortium invited educators from the Lower Mainland Math Contacts (LMMC) group to develop an elementary math framework to support teachers in the Coast Metro region in the teaching and assessment of elementary mathematics. A team of teachers

